

MATHEMATICS



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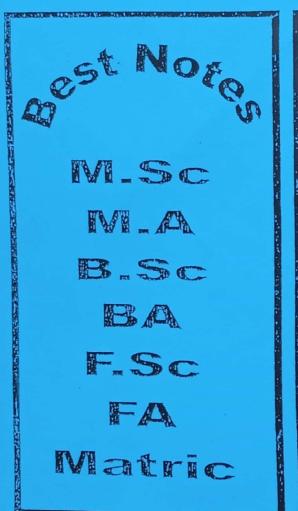
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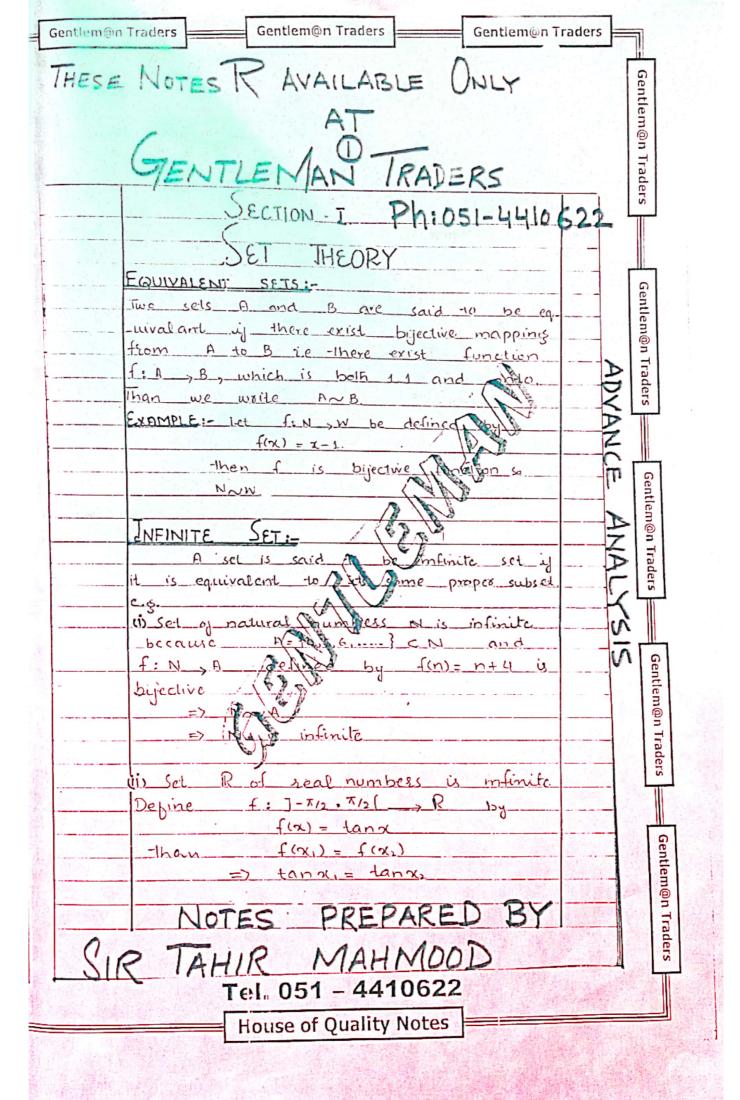


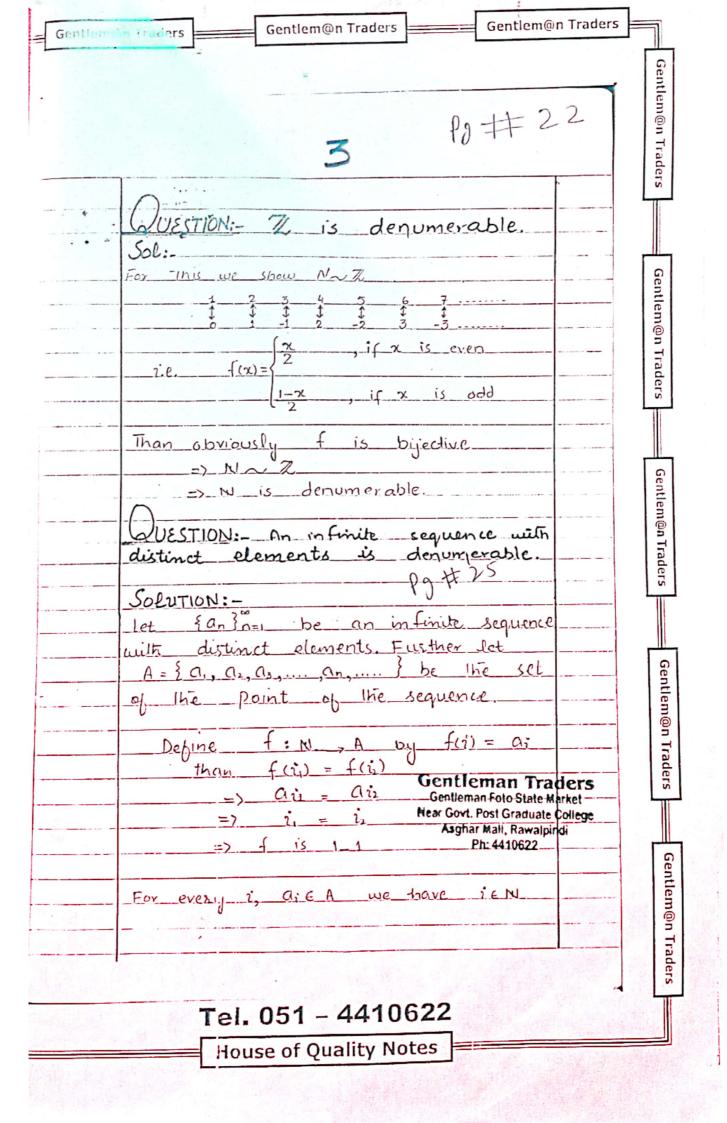
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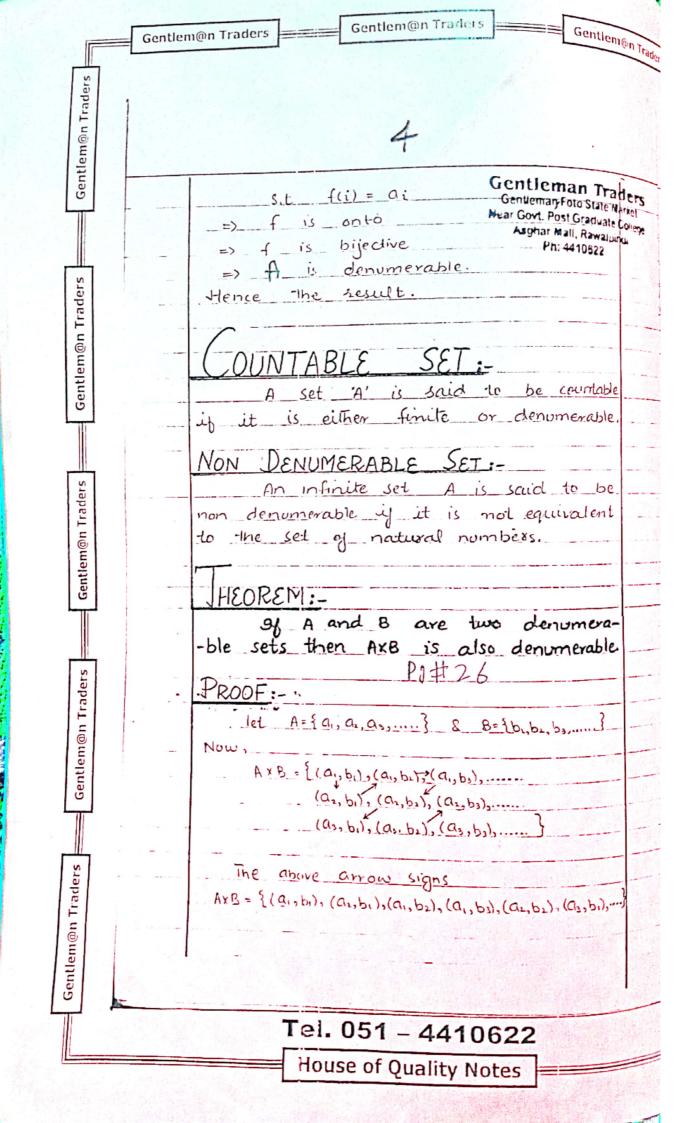
Digital Foto Copier
Mobile Connection
International Fax
Spiral Binding
Mobile Cards
Calling Cards
Color Copier
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Gifts

Gentleman Foto Stat Market Near Govt Post Graduate College Asghar Mall

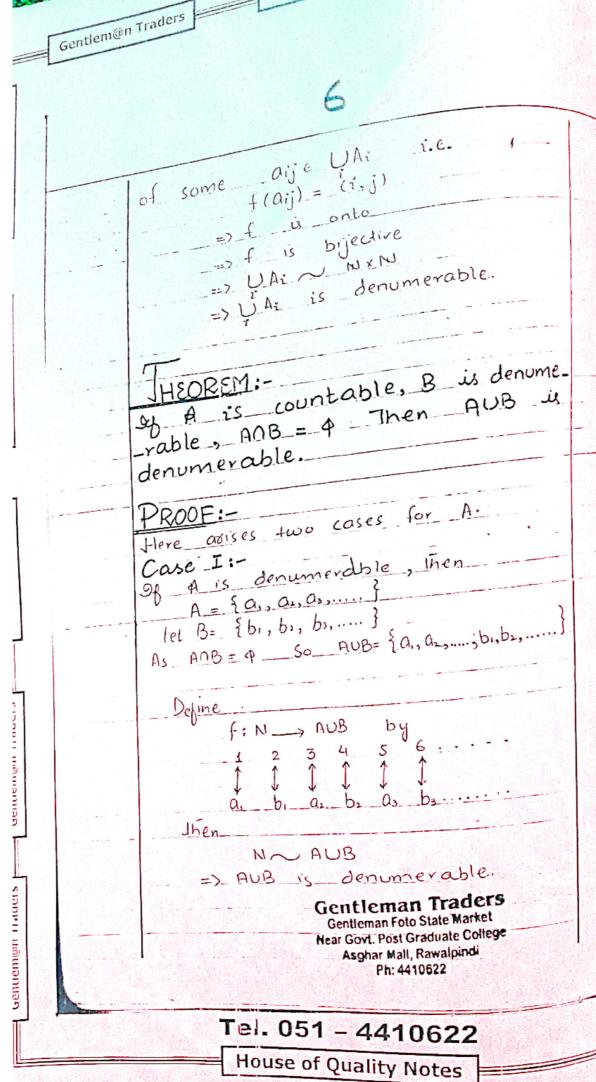
Rawalpindi - Tel. 051-4410622

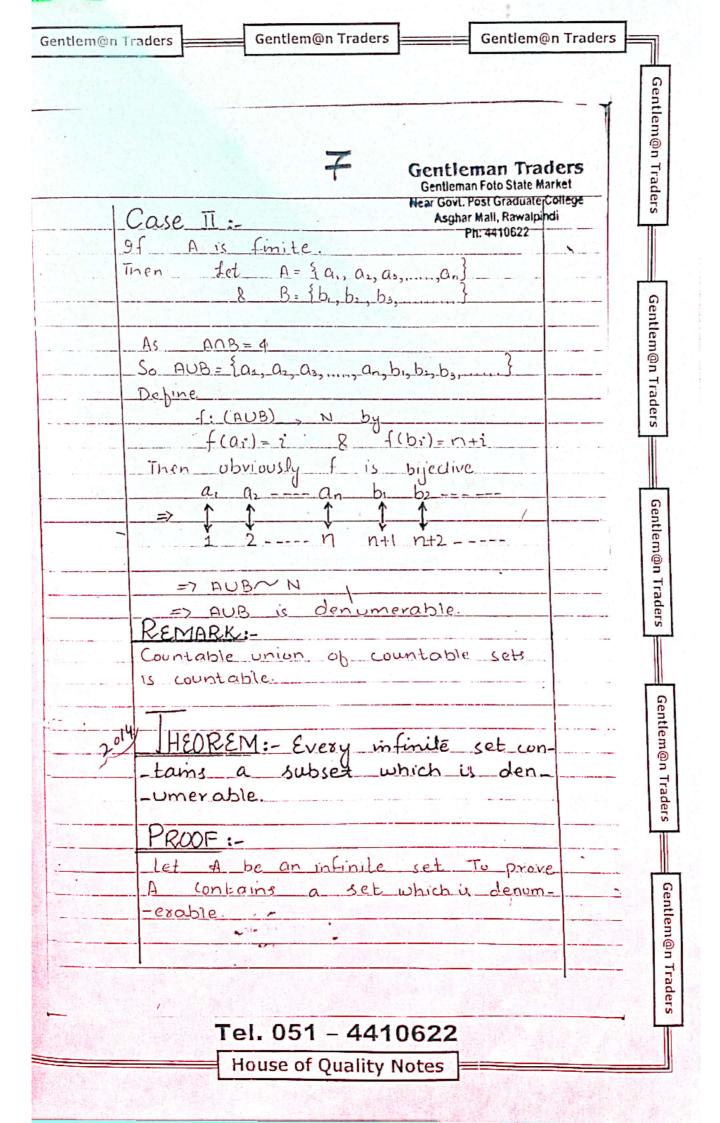


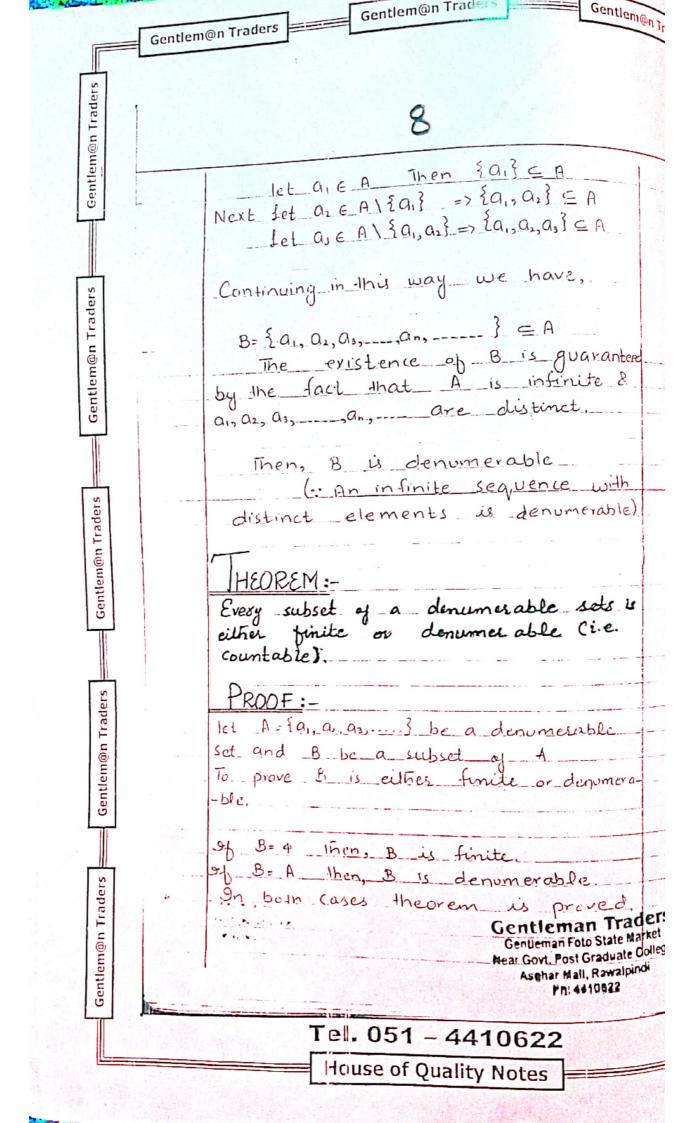




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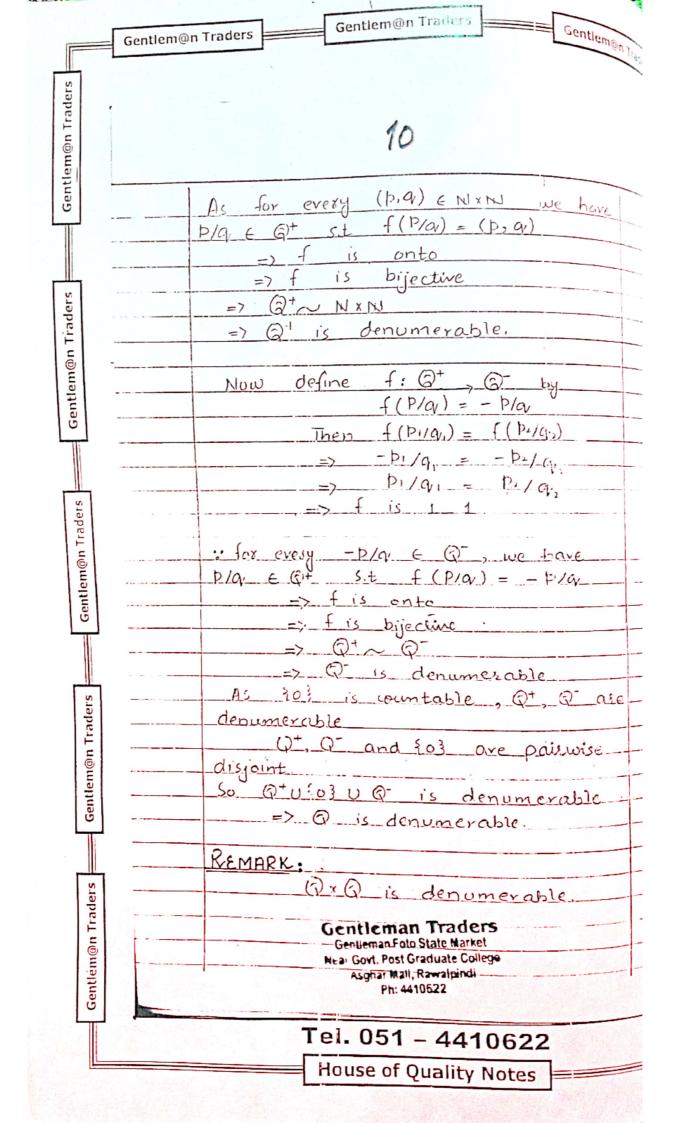


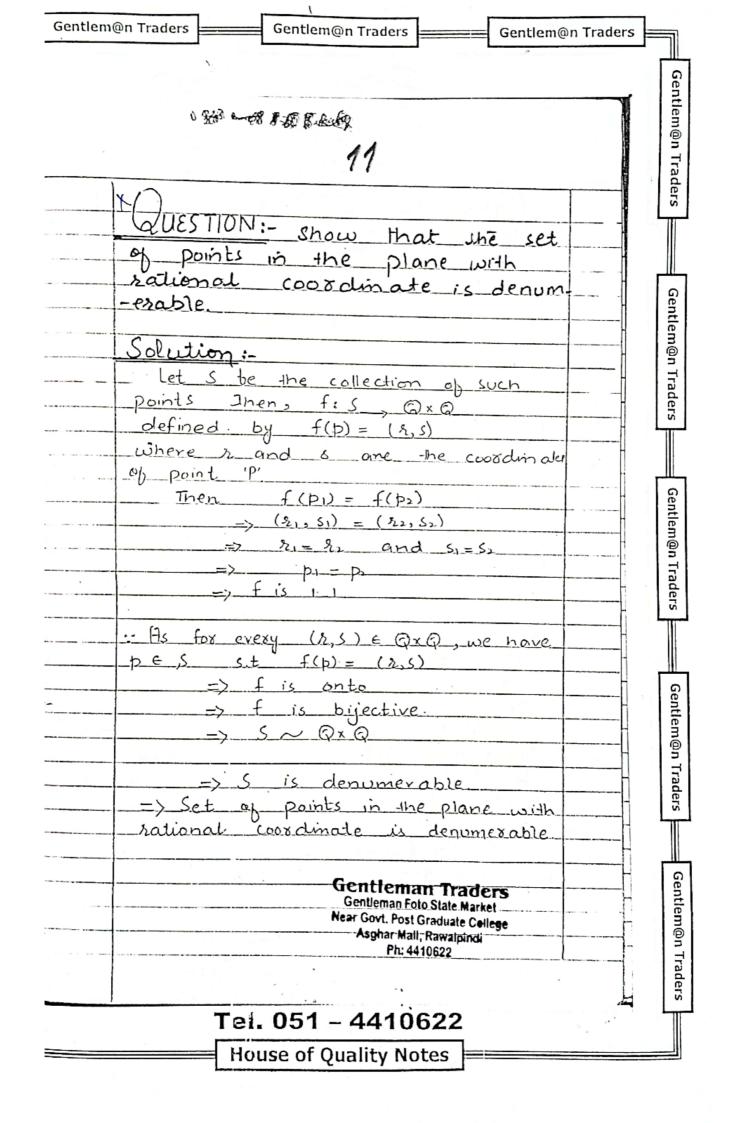
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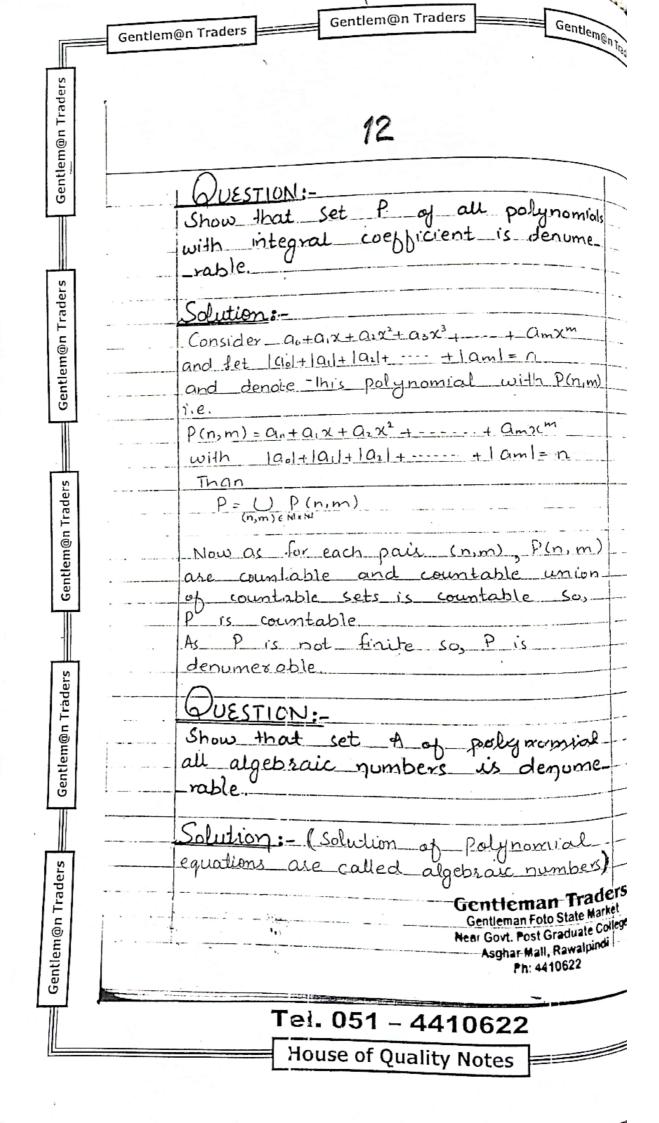
| 91 BCA and B # 4 Ihen, let air & B, air & B\ {air}, air & B\ {air, air}, | |
|--|--------|
| => ai, ai, ai, EB Of B is finite then, theorem is -proved. | |
| 96 B is infinite then, B= {ai1, ai2, ai3,} Then B is denumerable. Hence theorem is proved. | |
| J.M.P QUESTION:- Set of Rational number is denumerable. | |
| Solution: _ We know that @ = @ + U {o} U @ - | |
| Define $f: \bigcirc + \longrightarrow N \times N \longrightarrow by$ $f(P/Q_1) = (P_1/Q_2)$ $= P(P_1/Q_1) = P(P_2/Q_2)$ | |
| $= (p_1, q_1) = (p_2, q_2)$ $= (p_1, q_2)$ $= (p_2, q_2)$ $= (p_2, q_2)$ | |
| Gentleman Tra Gentleman Foto State I Near Govt. Post Graduate Asghar Mall, Rawalp Ph: 4410622 | Market |

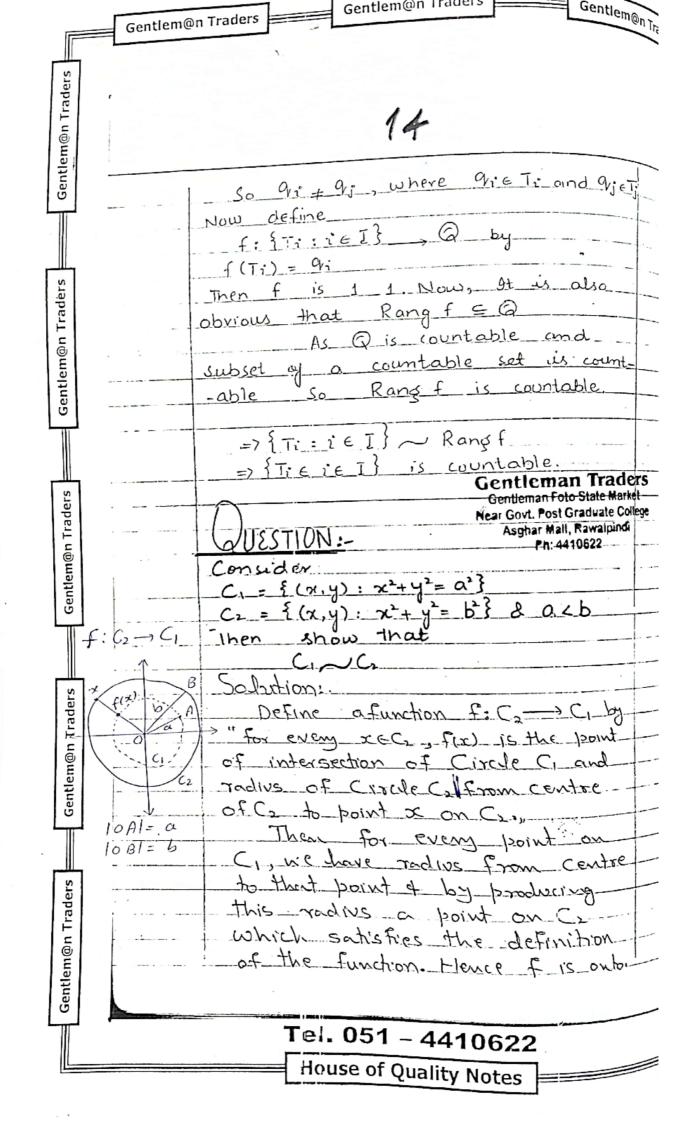
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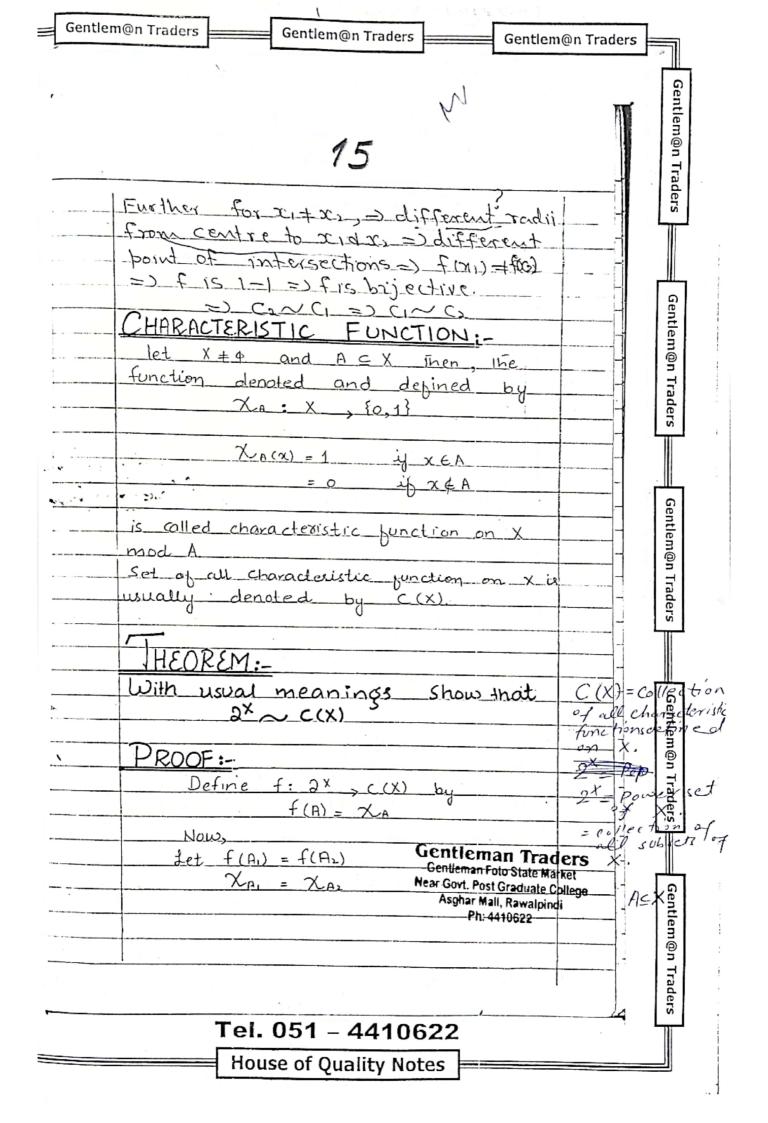
House of Quality Notes

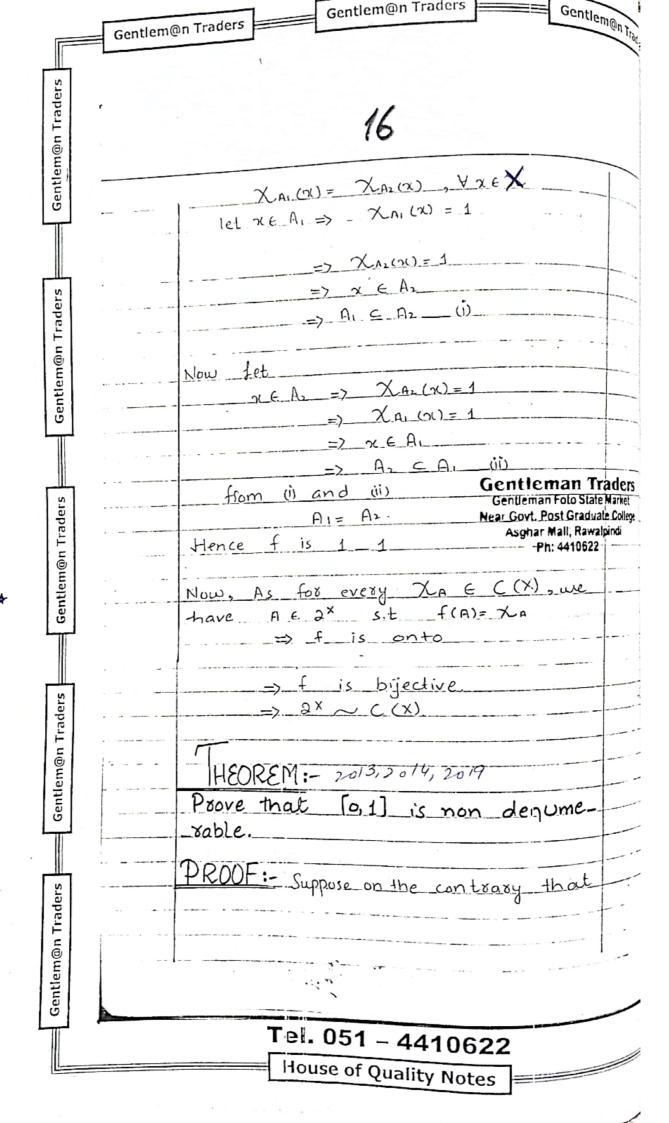


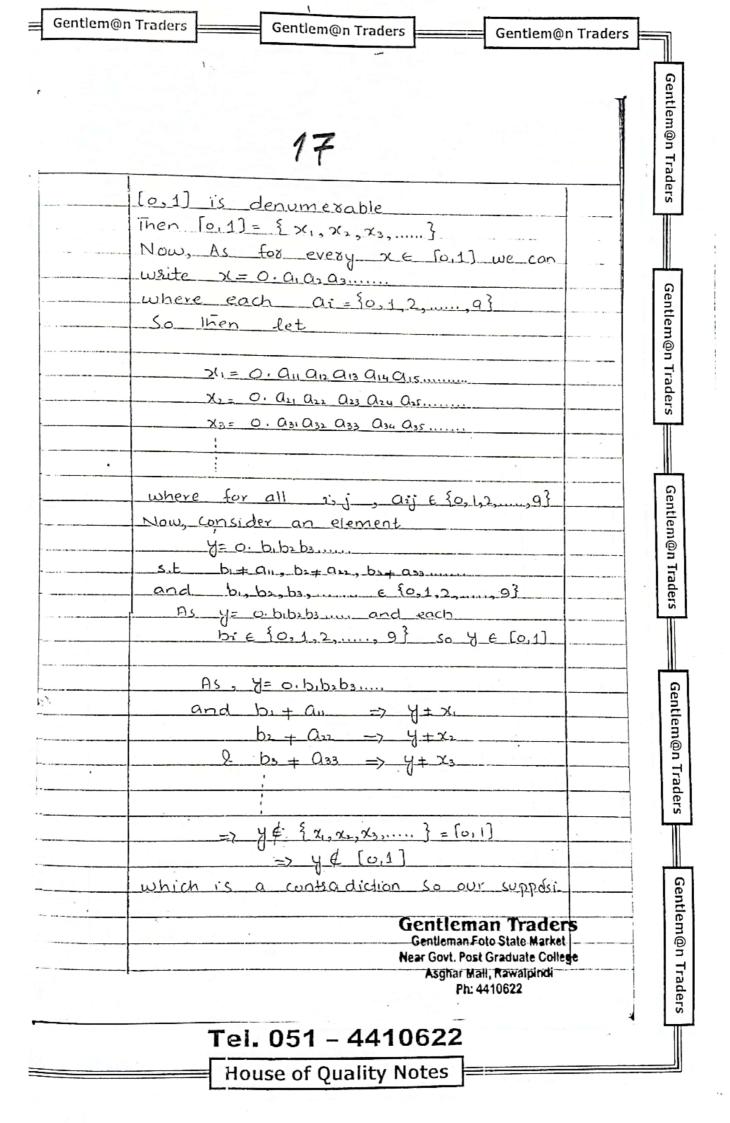


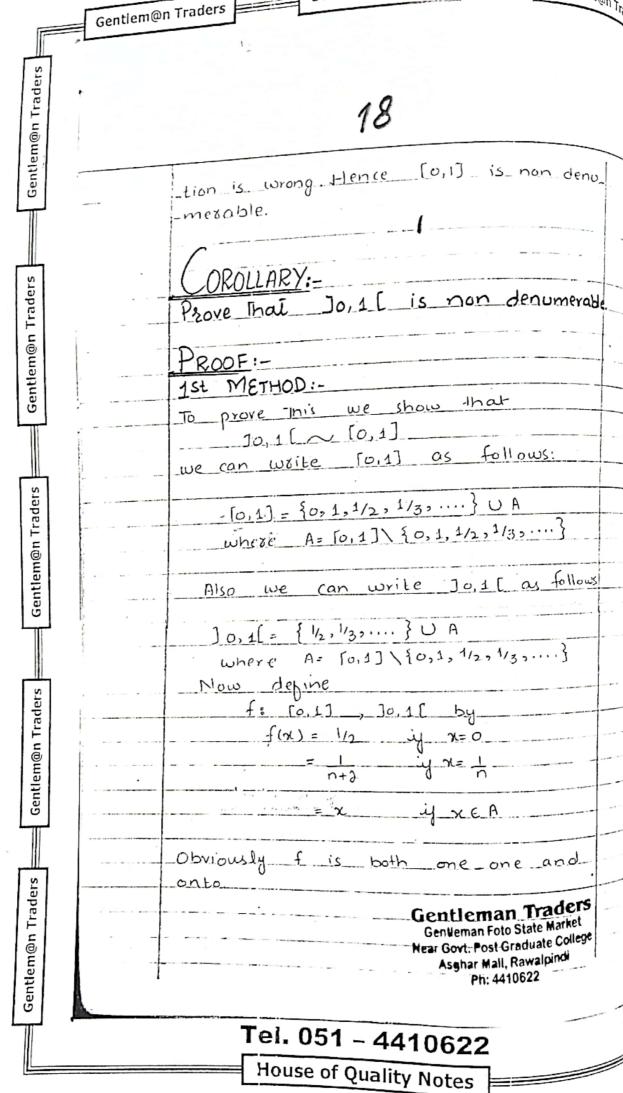


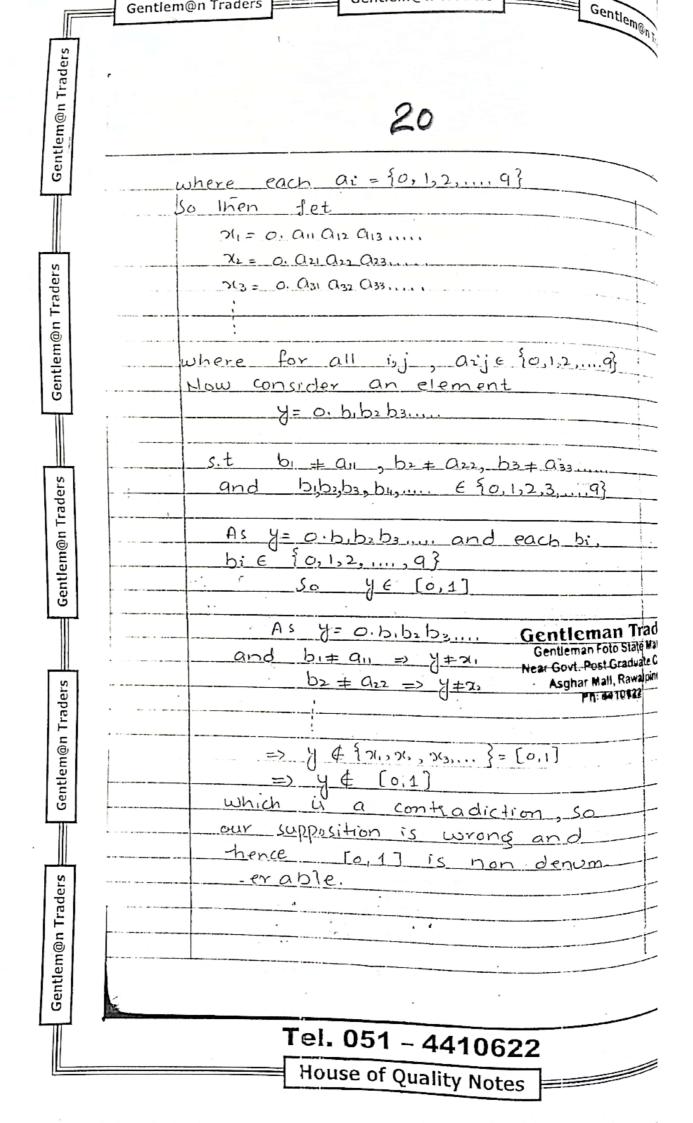


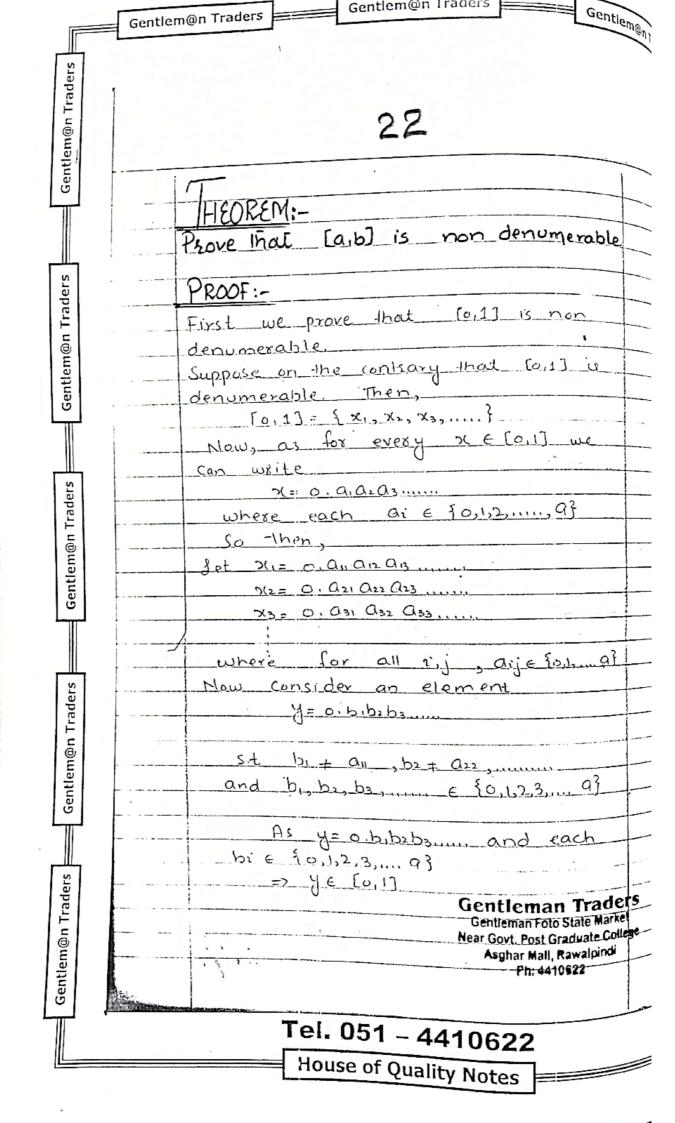


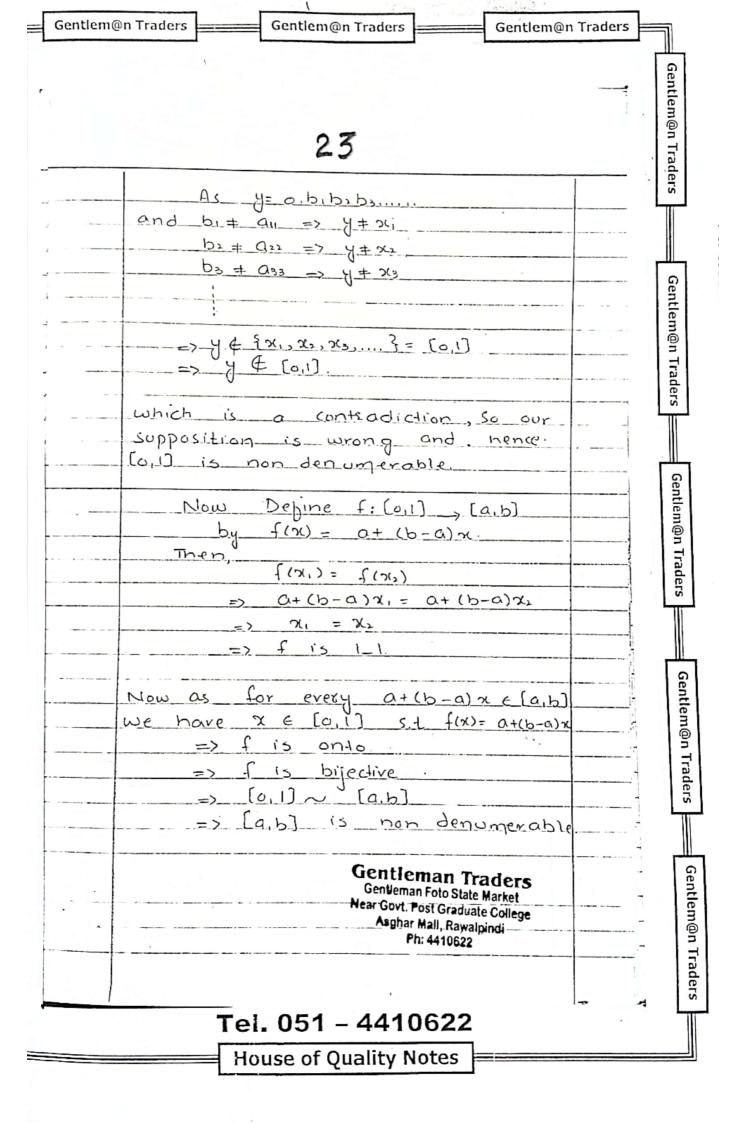


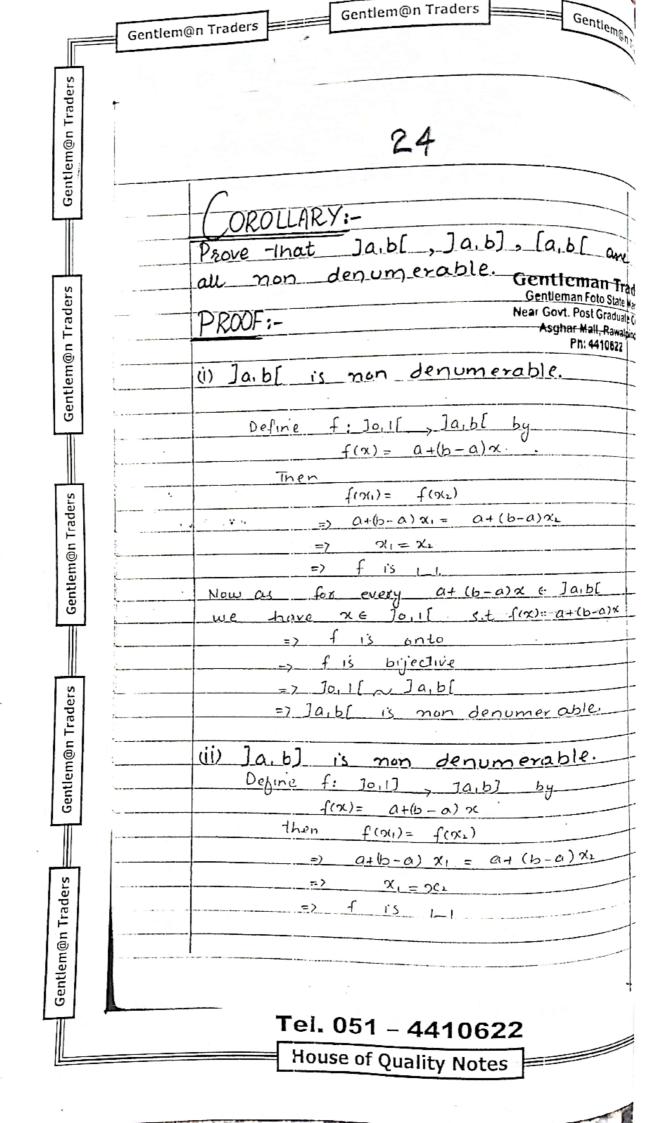


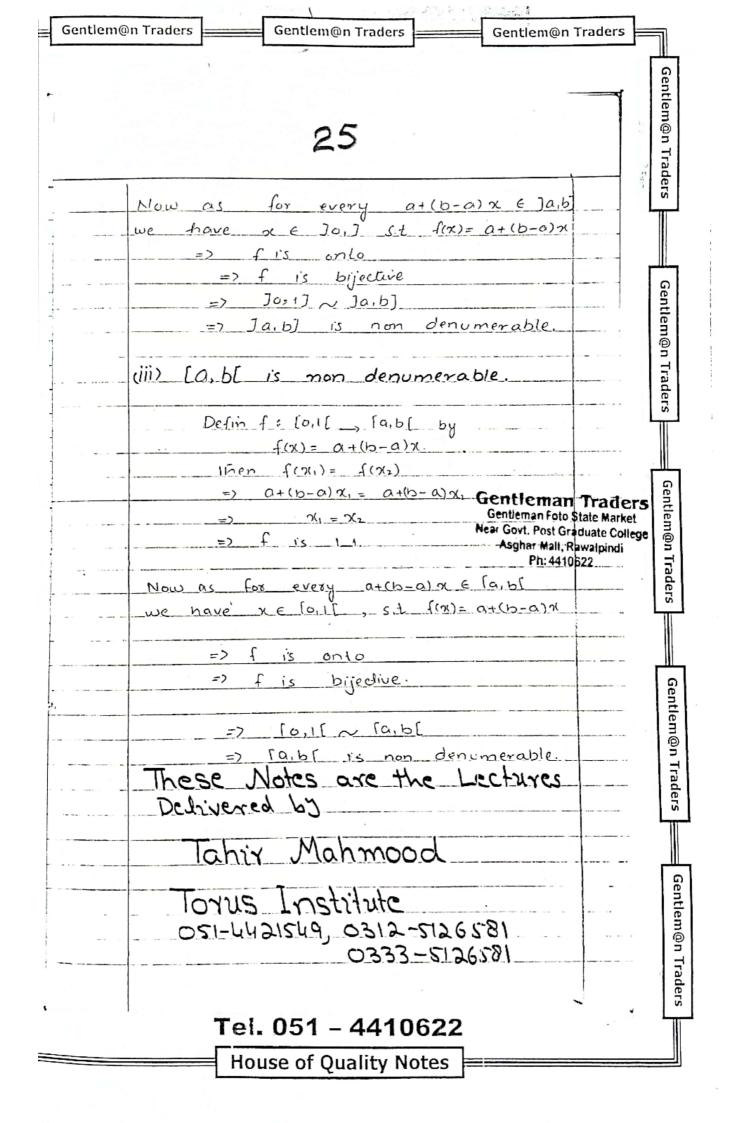


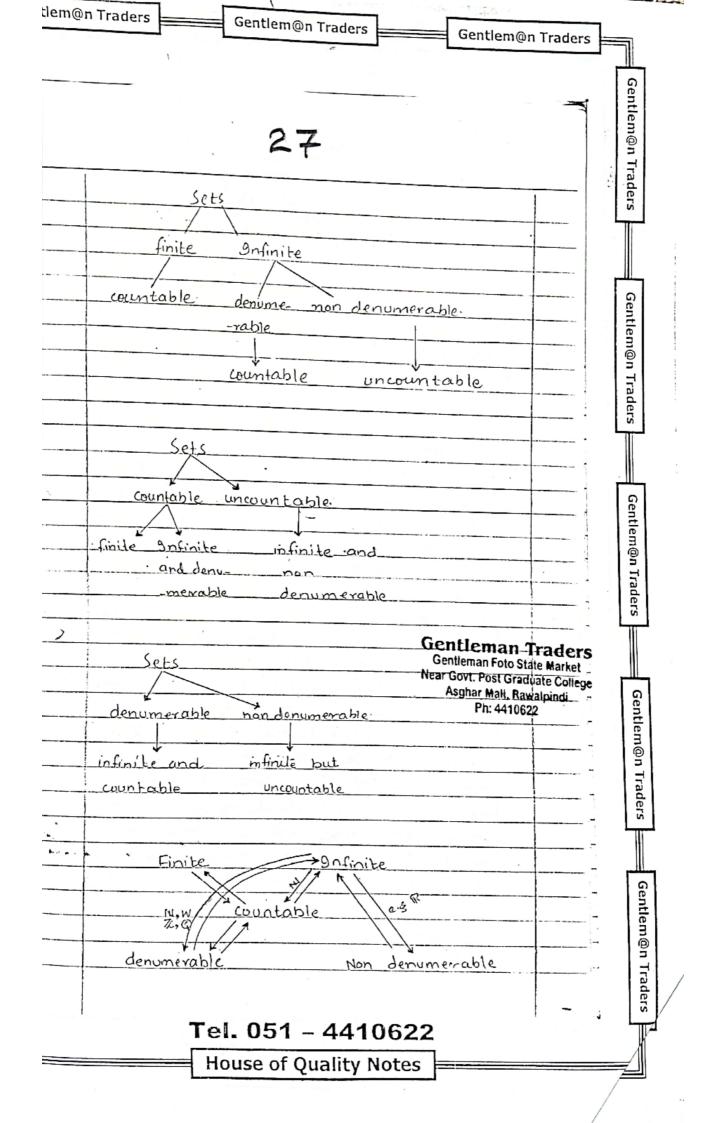


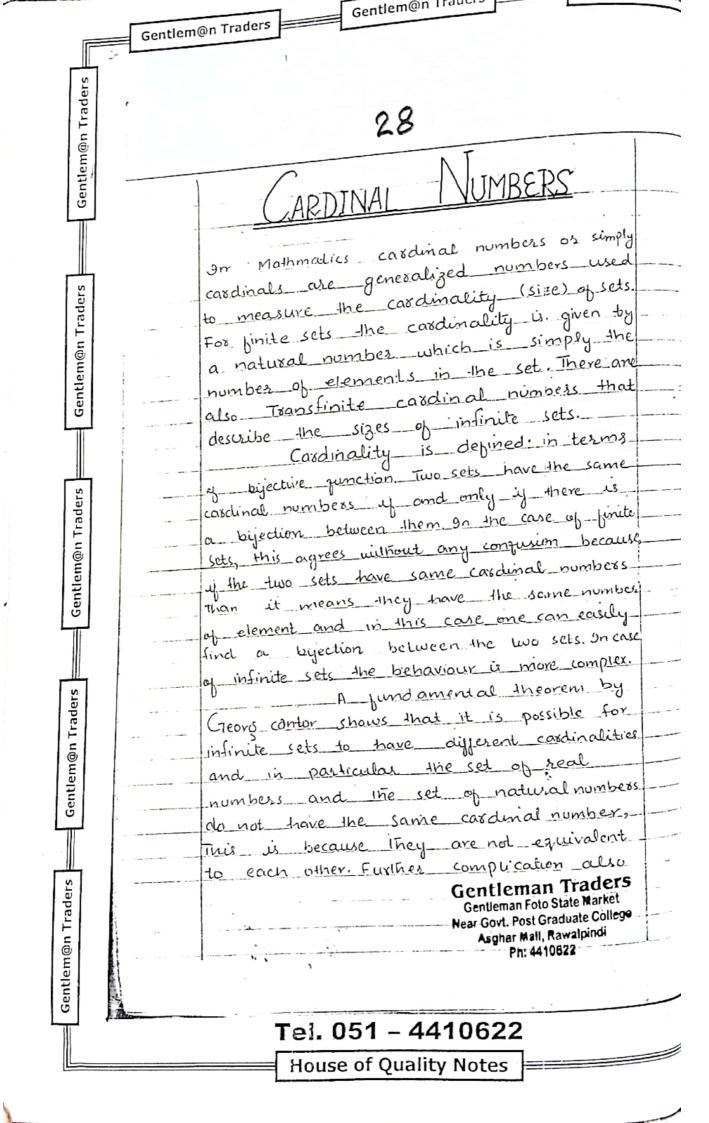






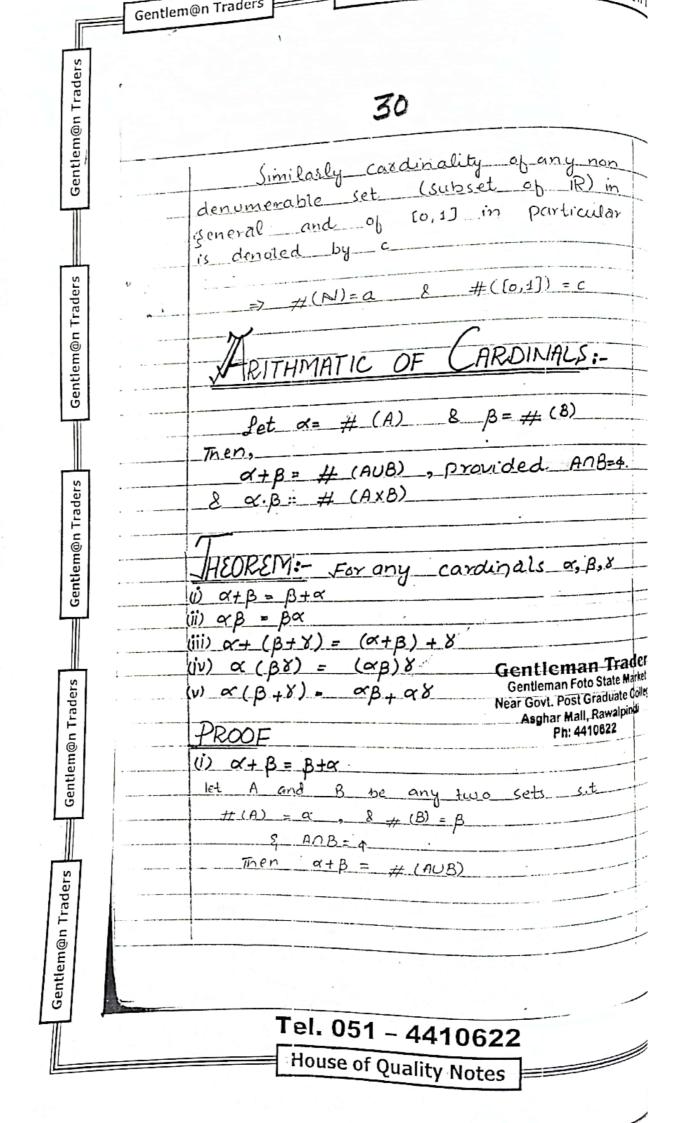


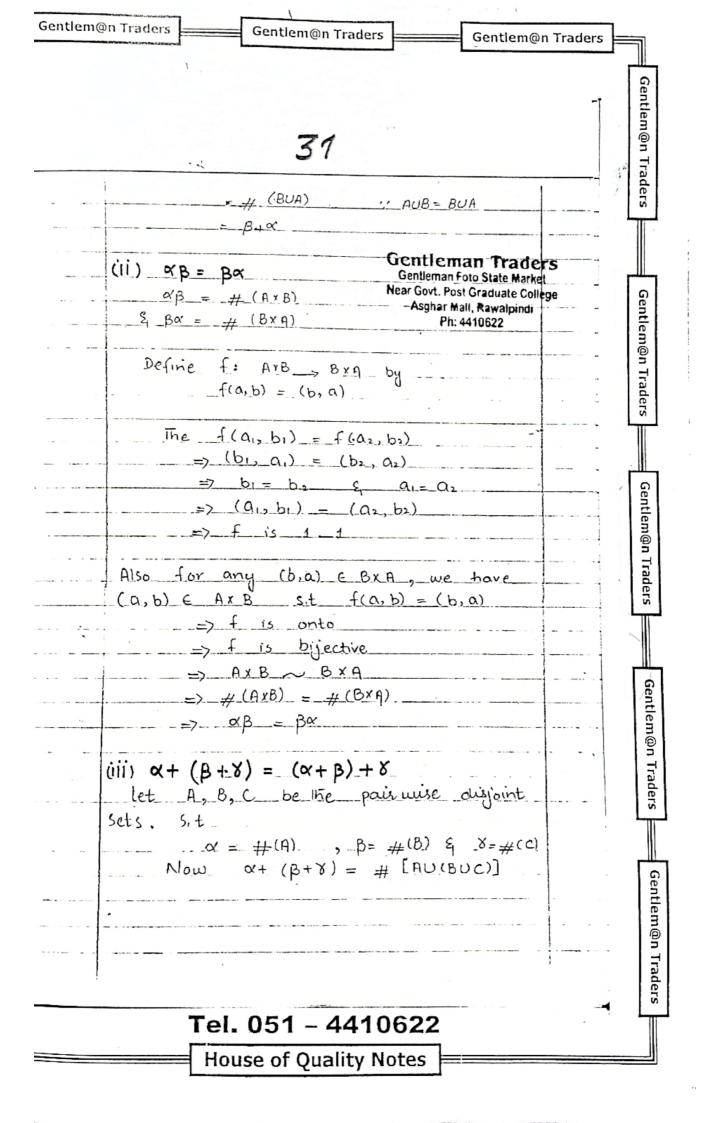


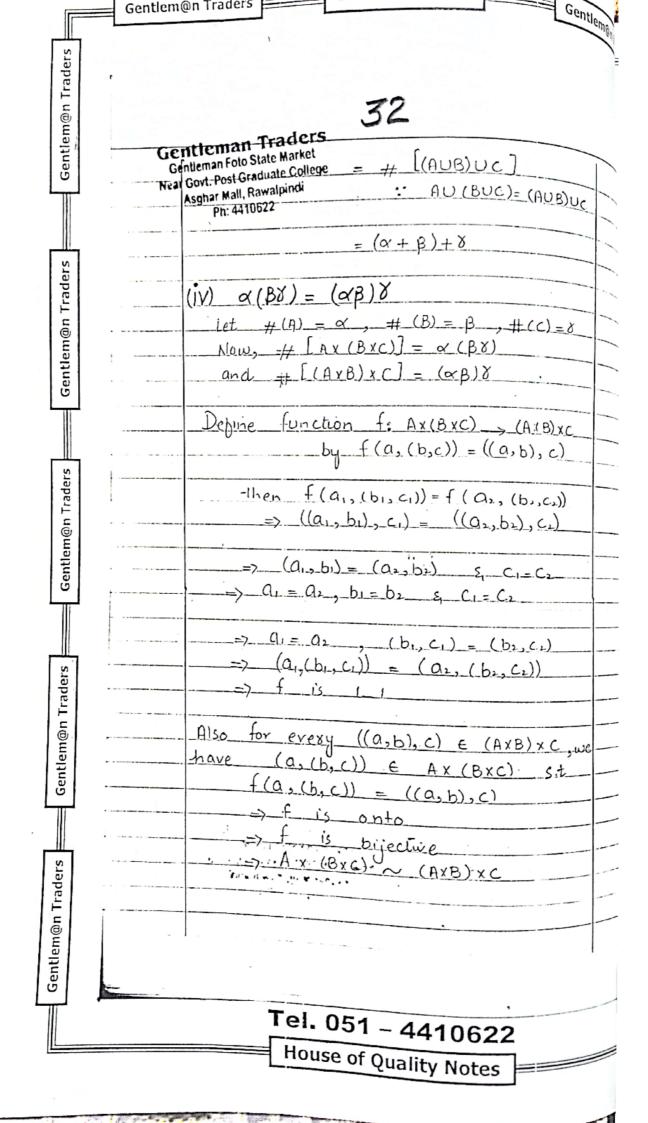


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House of Quality Notes







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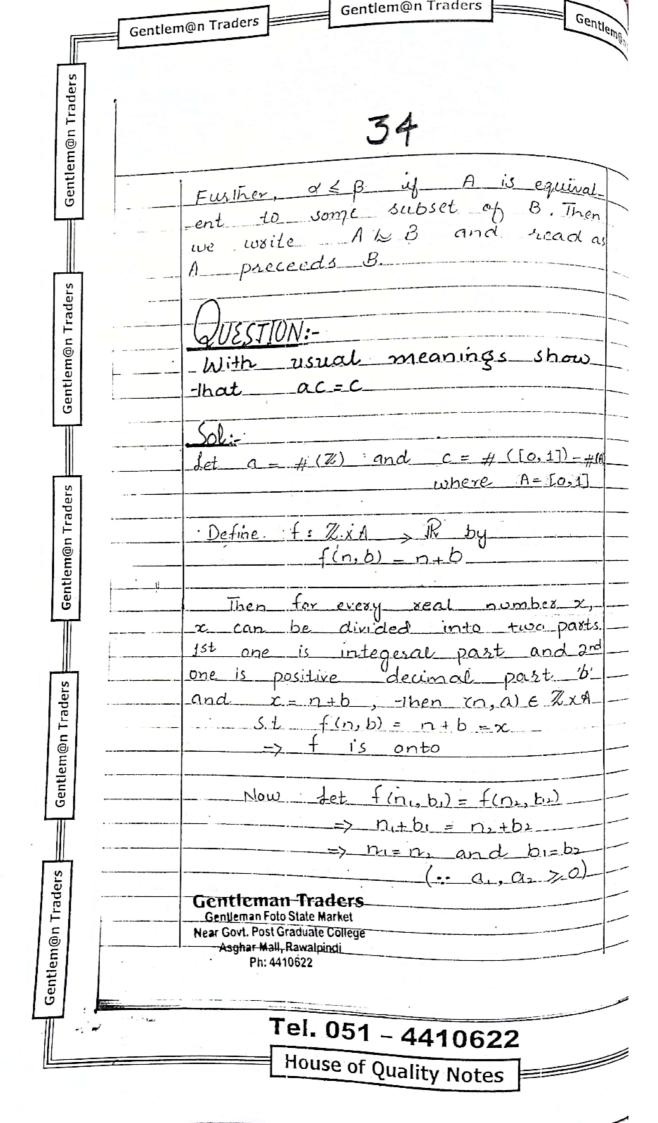
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Gentlem@n Traders

| α ∠β (read as α is less then β), if every I_I function f: A > B is not onto. OR Q A is equivalent to some subset B and A is not equivalent to B. Then we write A & B, and read it as A strictly preceeds B. Gentleman Traders |
|---|
| if every 1_1 function f: A > B is not onto. OR Q A is equivalent to some subset OR B and A is not equivalent to |
| if every LI function f: A > B is not onto. OR |
| if every 1_1 function f: A > B |
| a LB (read us a 15 less then b) |
| Then then By |
| Let A and B be two sets with $=$ $\#(A) = \alpha$ and $\#(B) = \beta$ |
| |
| NUMBERS:- |
| INEQUALITIES IN CARDINAL |
| $= \# \left[:(A \times B) \cup (A \times C) \right]$ $= \alpha \beta' + \alpha \delta$ |
| $\alpha (\beta + \delta) = \# [A \times (B \cup C)]$ |
| (A x B) \(\text{(A x C)} = \(\phi \) |
| and $\alpha = \#(A)$, $\beta = \#(B)$, $\delta = \#(C)$ ote that as $B \cap C = \phi$, so |
| onc = p |
| $(\beta + \delta) = \alpha \beta + \alpha \delta$ |
| $\Rightarrow + (A \times (B \times C)) = + ((A \times B) \times C)$ $= \Rightarrow \alpha (B \times C) = (\alpha B) \times C$ |
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 $(n_1, b_1) = (n_2, b_2)$

 $\#(\mathbb{Z} \times A) = \#(\mathbb{R})$

KEMARK:-Show by an example inat. i) Cancellation laws do not hold for casdinal addition.

iii) Cancellation laws do not hold for cardinal multiplication.

SOLUTION:-

Then

NUA = N and NUB= {x,1,2,3,

Then # (NUA) = # (N)

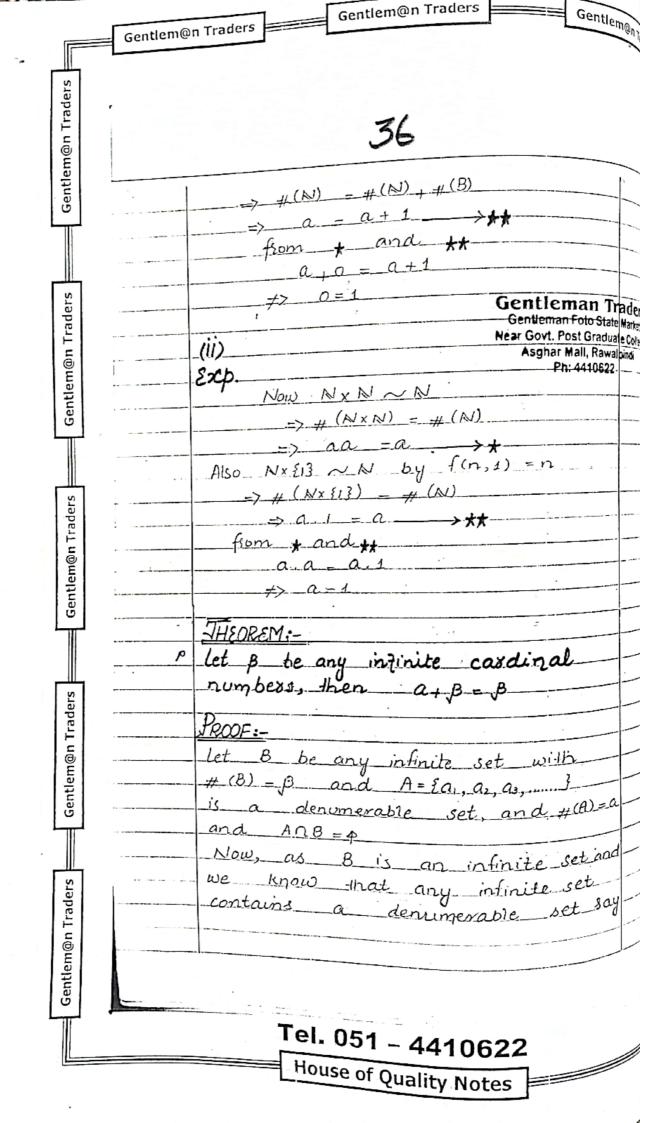
(N) + # (A) = # (N)

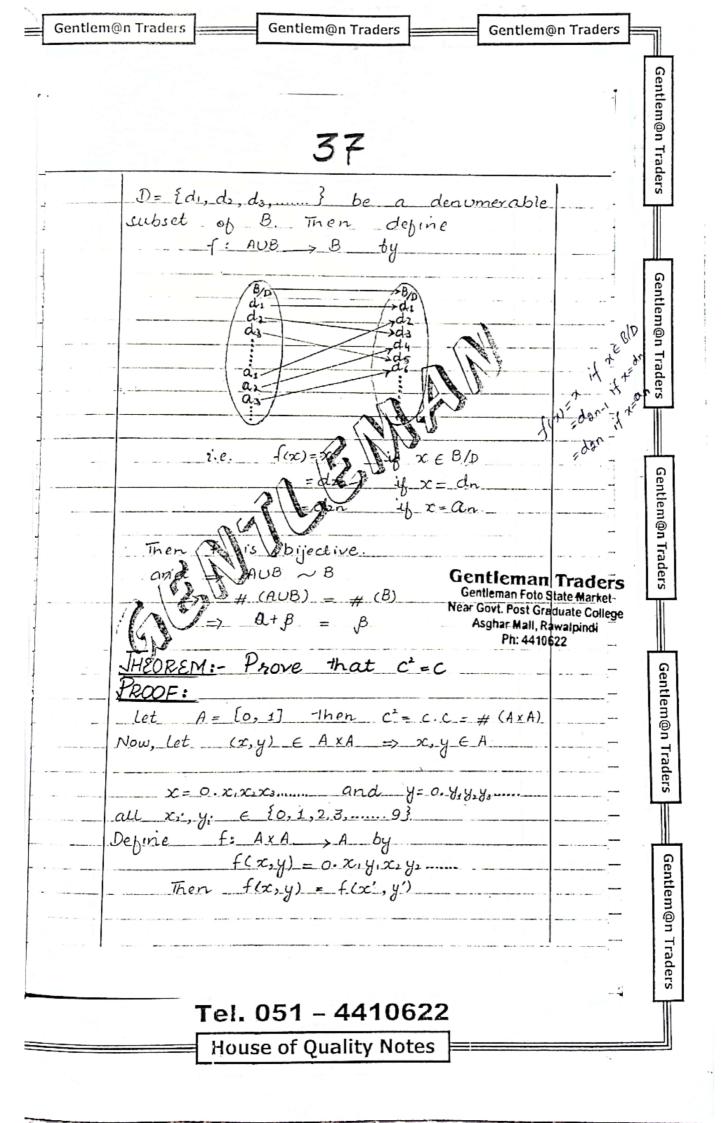
Now_define____

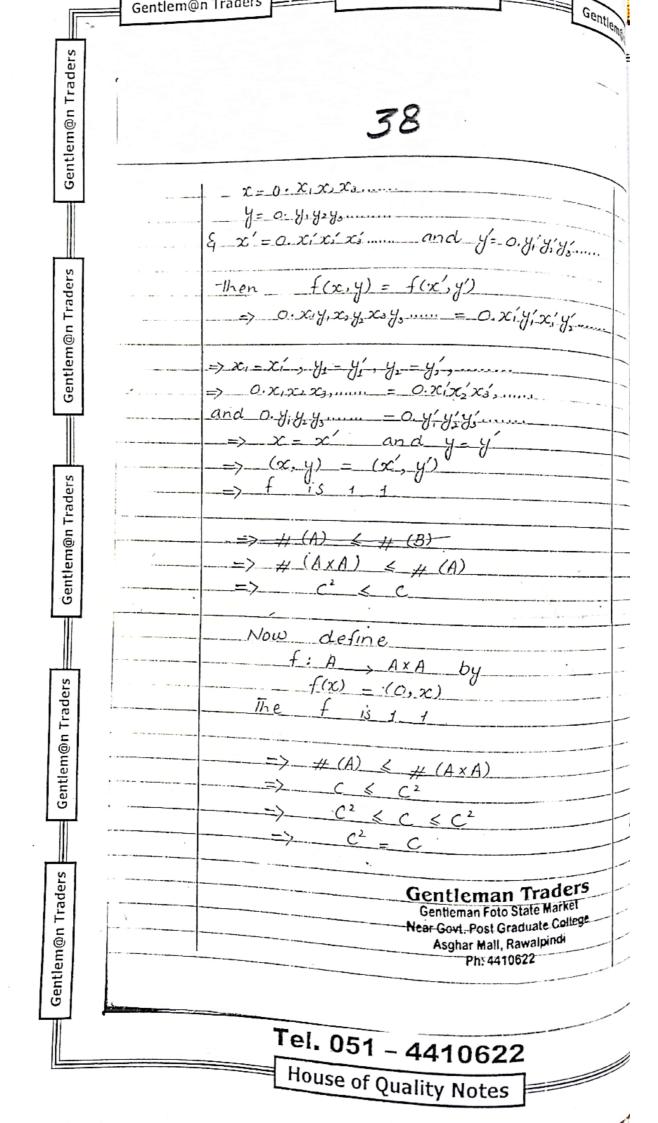
Then_f_is_bijective.

=> N~ NUB => #(N) = # (NUB)

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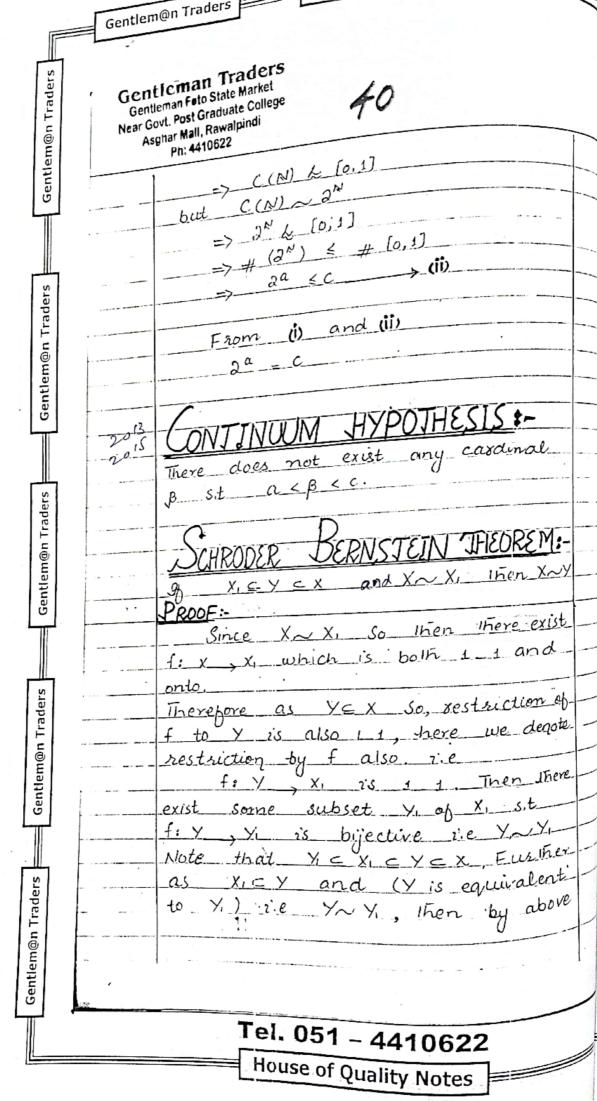


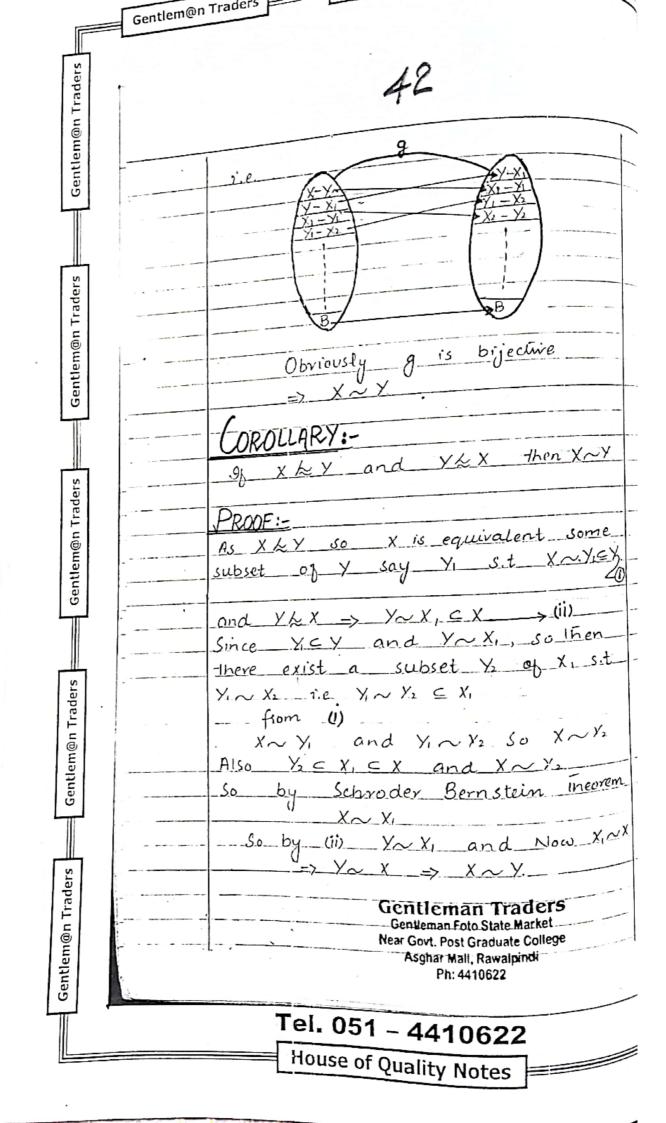


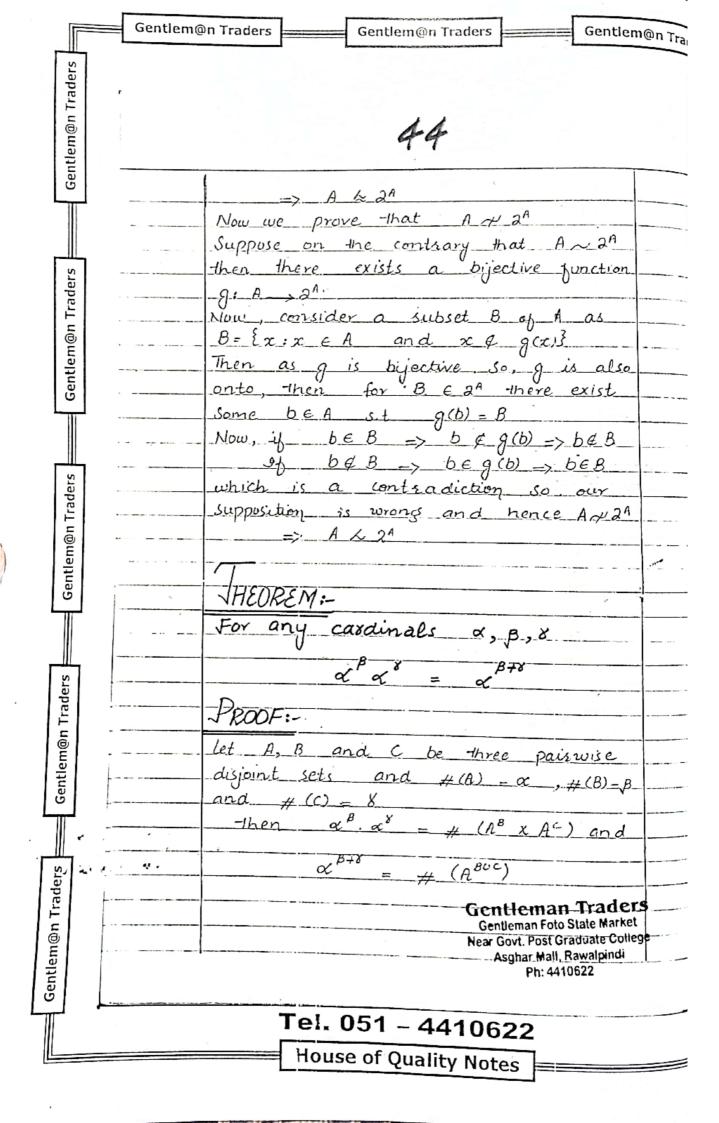


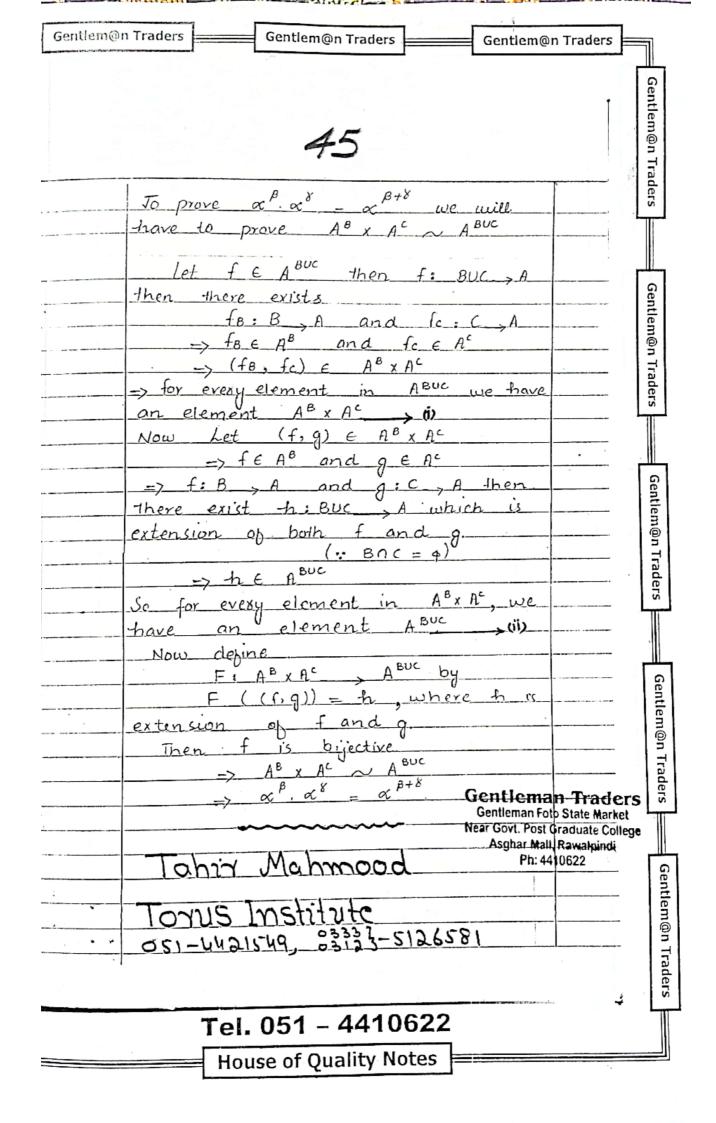
| QUESTION: - Show - Inat 2a = c. | |
|---|----------|
| Col. | |
| Define f: R 20 by | |
| Define $f: \mathbb{R} \to 2^{\mathbb{Q}}$ by $f(x) = \{q: q \in \mathbb{Q} \text{ and } q \in \mathbb{Z}\}$ | |
| Then if x, y & R S.t N# | |
| then say x <y< td=""><td></td></y<> | |
| Then by rational density theorem. | |
| there exist some rational number &, | |
| st x l x l y | |
| | |
| As $8 < y$ so $8 \in f(y)$ and $8 > x$ i.e. $8 \not< y \Rightarrow x \notin f(x)$ | |
| and 87x i.e 8 4 7 => 8 4 + (2) | |
| $\Rightarrow f(x) \neq f(y)$ | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| => #(R) ≤ # (2°) | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| | |
| Now, Consider C(N), Set of characteris | |
| eta runction defined on N and | |
| dolina t: C(N) - 10,33 Dg | |
| $F(f) = 0 \cdot f(1) f(2) f(3) \dots$ | |
| let f. S E C(N) sit f + 8 | |
| Then There exist at least one | |
| $n \in \mathbb{N}$ s.t. $f(n) + g(n)$ | |
| => 0. f(1)f(2)f(3) + 0.919593} | |
| $=\rangle$ $F(f) \neq F(g)$ | |
| F is 1 1 Gentleman | |
| Gentleman Foto St Near Govt. Post Grad | |
| Asghar Mall, Ra | walpindi |
| Ph: 44106 | 22 |

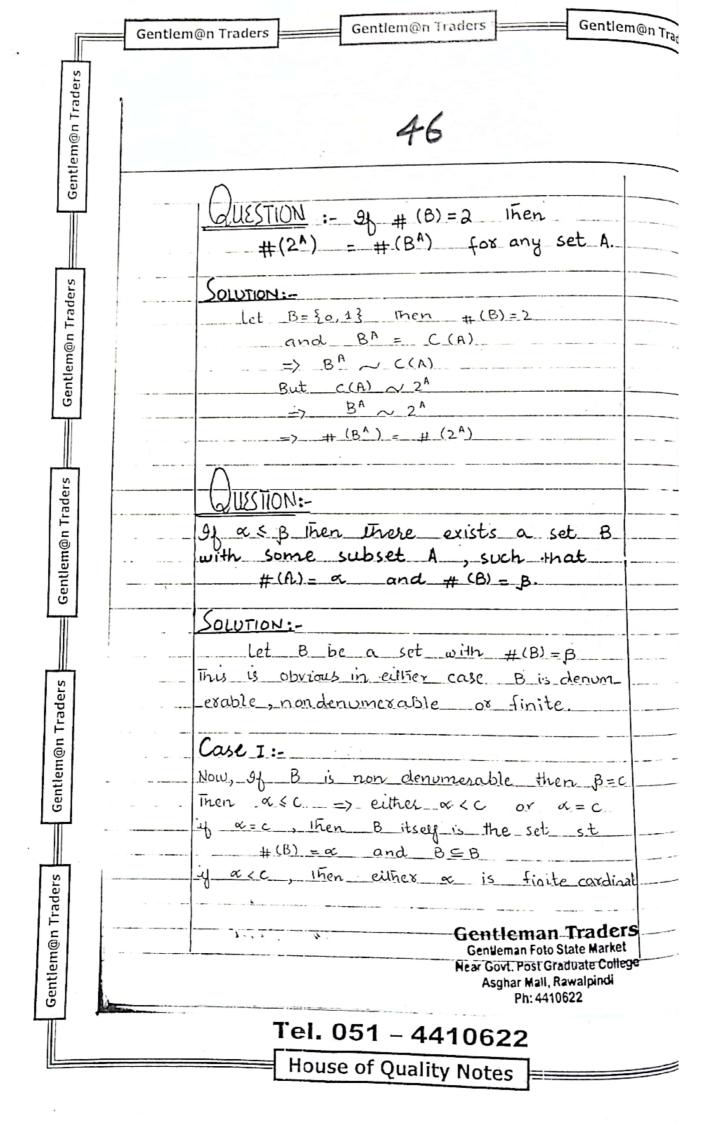
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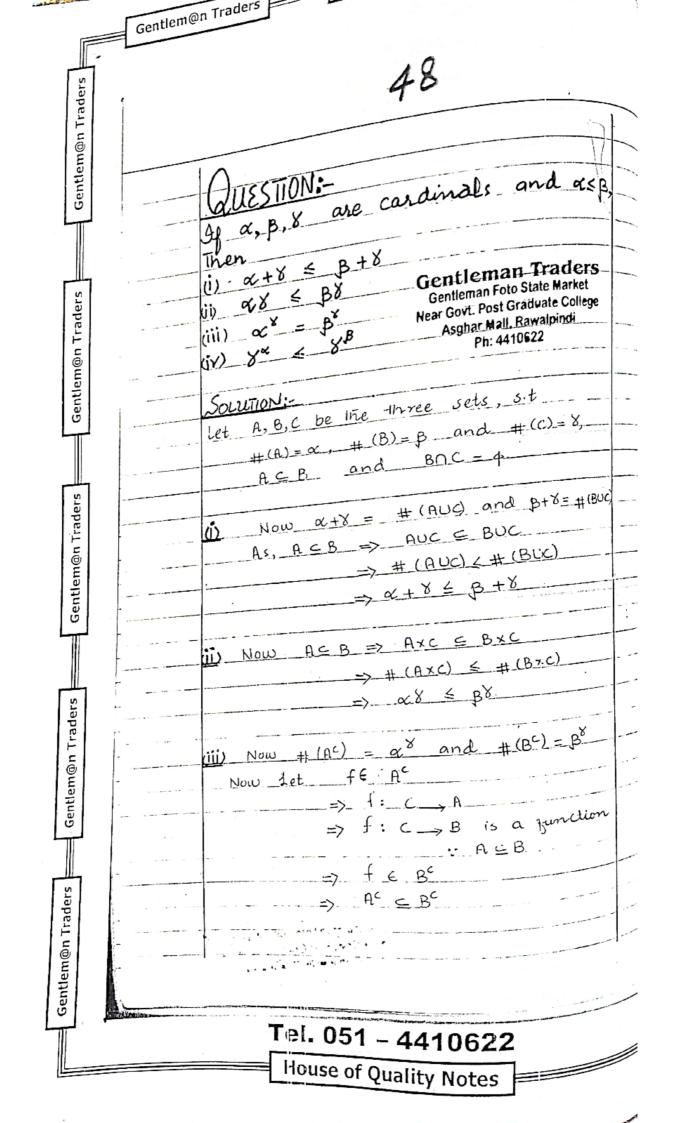


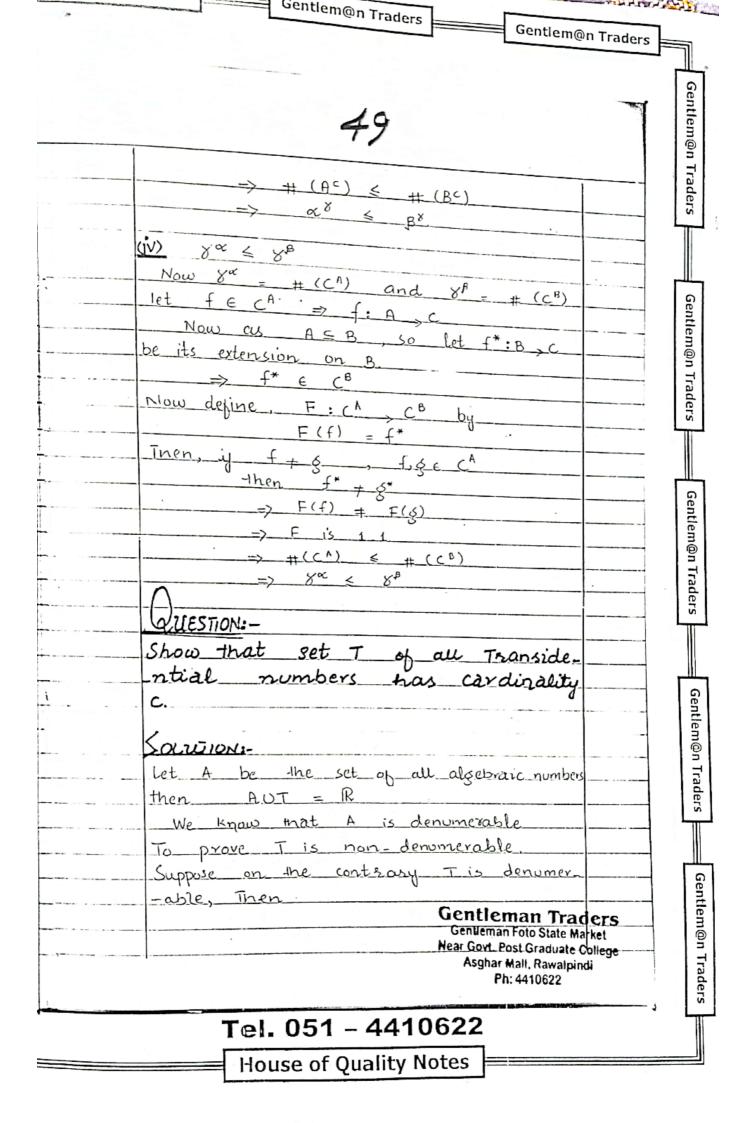




| or a | is cardinality of some denumerable |
|-------------|--|
| | is figite conding to the state of |
| 0 | is finite coordinal, then there exists |
| some | finite subset A of B st #(A)=a |
| -96-x | is cardinality of some denumerable |
| set, | Then as for every non denumerable |
| | as a denumerable subset then, there |
| exist | a denumerable subset A of B st |
| _ | = \infty. |
| Case: | |
| | is some denumerable set, then |
| $\beta = a$ | Then $\alpha \leq \beta$ means $\alpha \leq \alpha$ |
| | $-\gamma \alpha = \alpha \circ \alpha \times \alpha \times \alpha$. |
| | a , Then B itself is the set with |
| #(8) | $= \alpha$ and $B \subseteq B$. |
| - | 9/ a < a, then a is some finite cardin- |
| -al, | then there exists some finite subset |
| A of | B 5.t # (A) = ~ |
| Case | Ш :- |
| 9+ | B is some finite set and #(B)=B |
| Then | B is some natural number. |
| | $\alpha \leq \beta \Rightarrow \alpha = \beta \text{ by } \alpha \leq \beta$ |
| | (= B => B itself is the set s.t |
| # | $(B) = \infty$ and $B \subseteq B$ |
| 91 0 | LB then or is some finite cood! |
| 70-0 | Then there exist some finite |
| -nal | 0 1 11 (0) |
| Subse | $2t$ A of B, s.t. $\#(H) = \infty$ |
| | Gentleman Traders |
| - | Gentleman Foto State Market |
| | Near Govt. Post Graduate College Asghar Mall, Rawalpindi |
| | Ph: 4410622 |
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Tel. 051 - 4410622



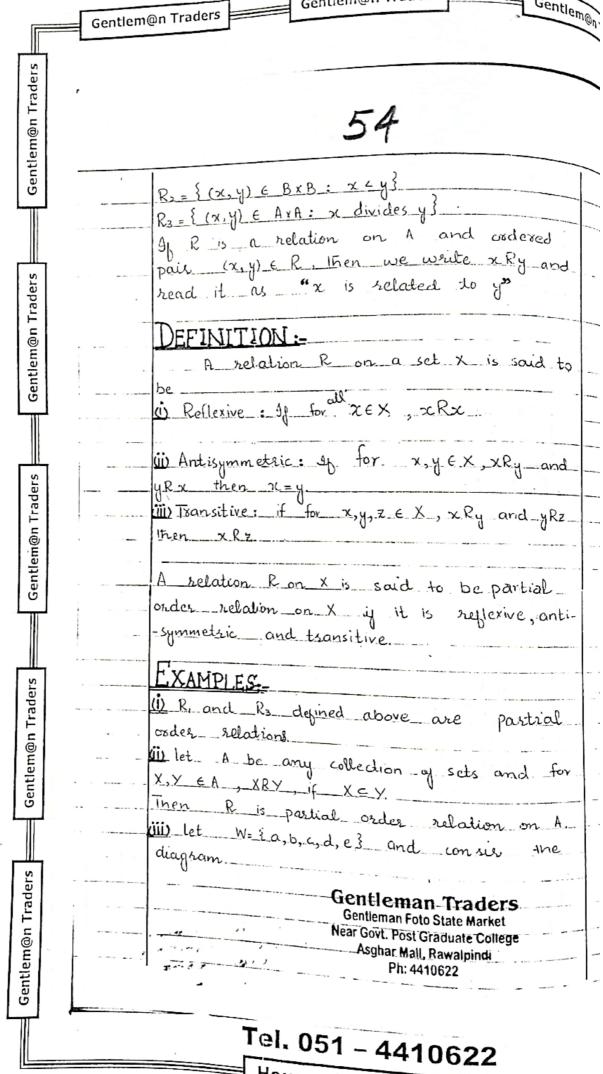


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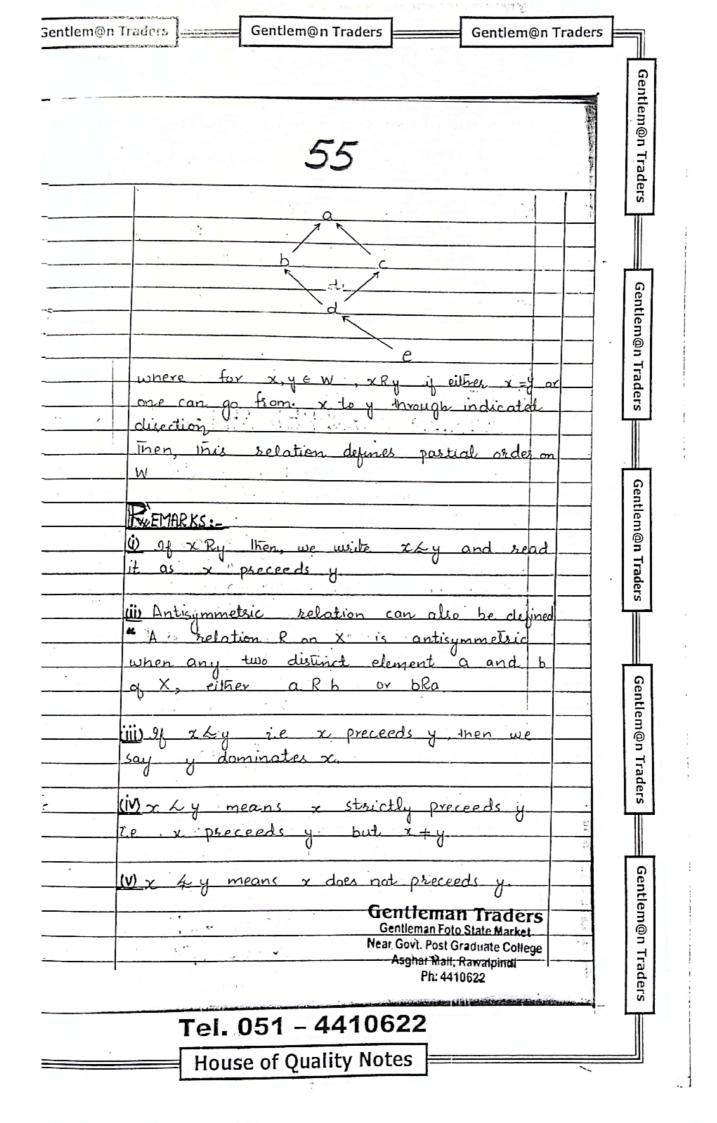
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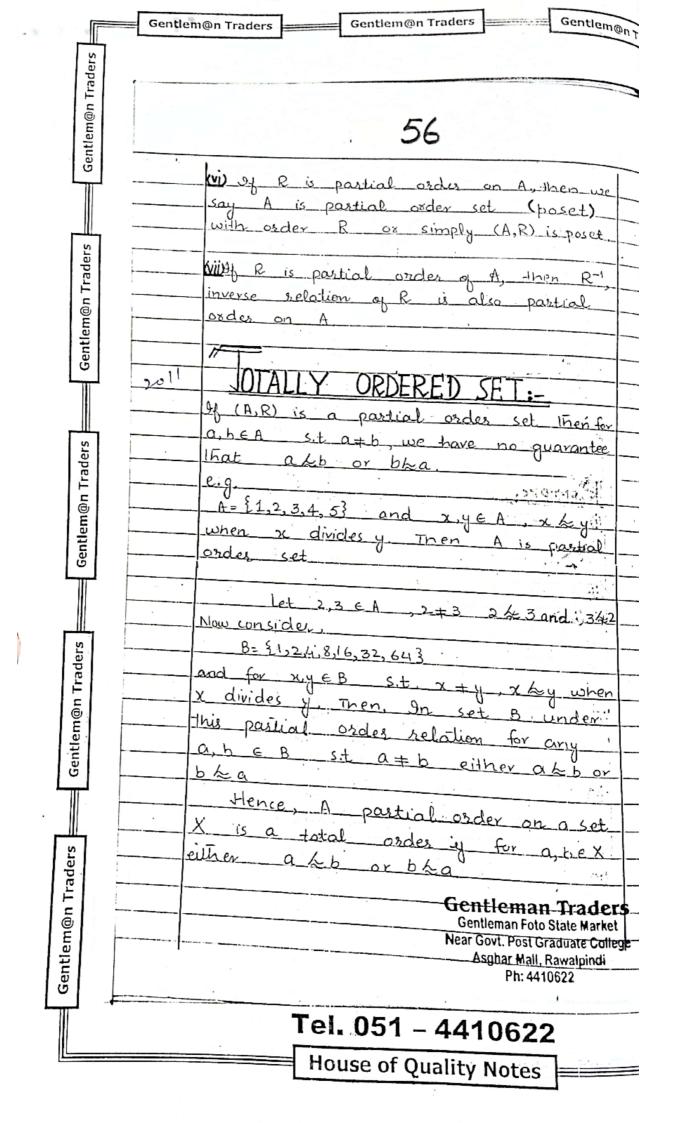
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Gentlem@n Traders Gentleman Traders Gentleman Foto State Market Gentlem@n Traders Near Govt. Post Graduate College Asghar Mall, Rawalpindi Ph: 4410622 Question: If I is any infinite cardinal then lth = l Solution2 - By continuum ty pothesis either & is a or "c" Further 1+1=1 follows by the fact that Gentlem@n Traders nion of two denumerable sets is denumerable and union of two non-denumerable is non-denumerable nestion: - Prove that RM + honce RER Solution: Consider 5= Jos [= {xelfroxxxi} 4 52-5XS= { (XX): 0< X< 14 0< Y< 1} Gentlem@n Traders Now for (25) = S2=) x,yeS= Joll can x=0.didada---- y=0.818283---. where all discrefold - 193 4 each decimal exbision contains infinite number of nonzero divits es-1 is written anyagg -- instead orsoon ... Now define f: 5°->5 by f(7,3) = f(0.d,d2 d3-... 0.6,626,-...) = 0.d,6,026. Gentlem@n Traders Then due to uniqueness of decimal expansion f 15 1-1=> 52 F(x) = (x,0.5) then Theorem Now IR~S=) IR=RXIR~SXS Gentlem@n Traders CX IR IR3 RXR ~ RXR~R Similarly by induction Tel. 051 - 4410622 House of Quality Notes

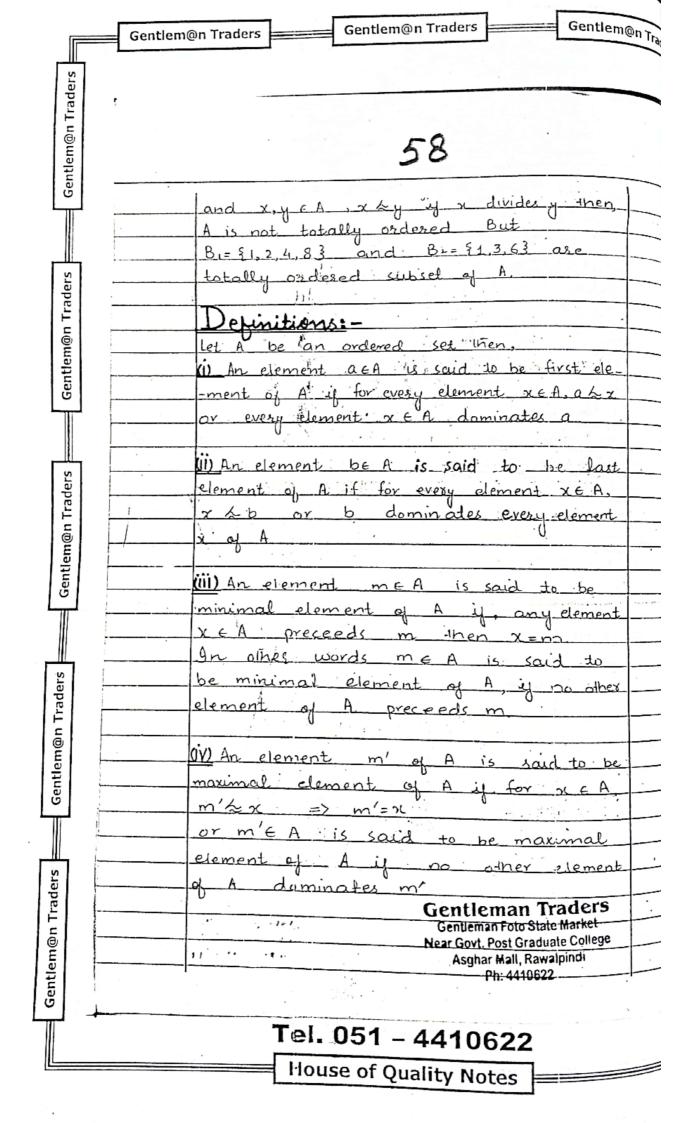


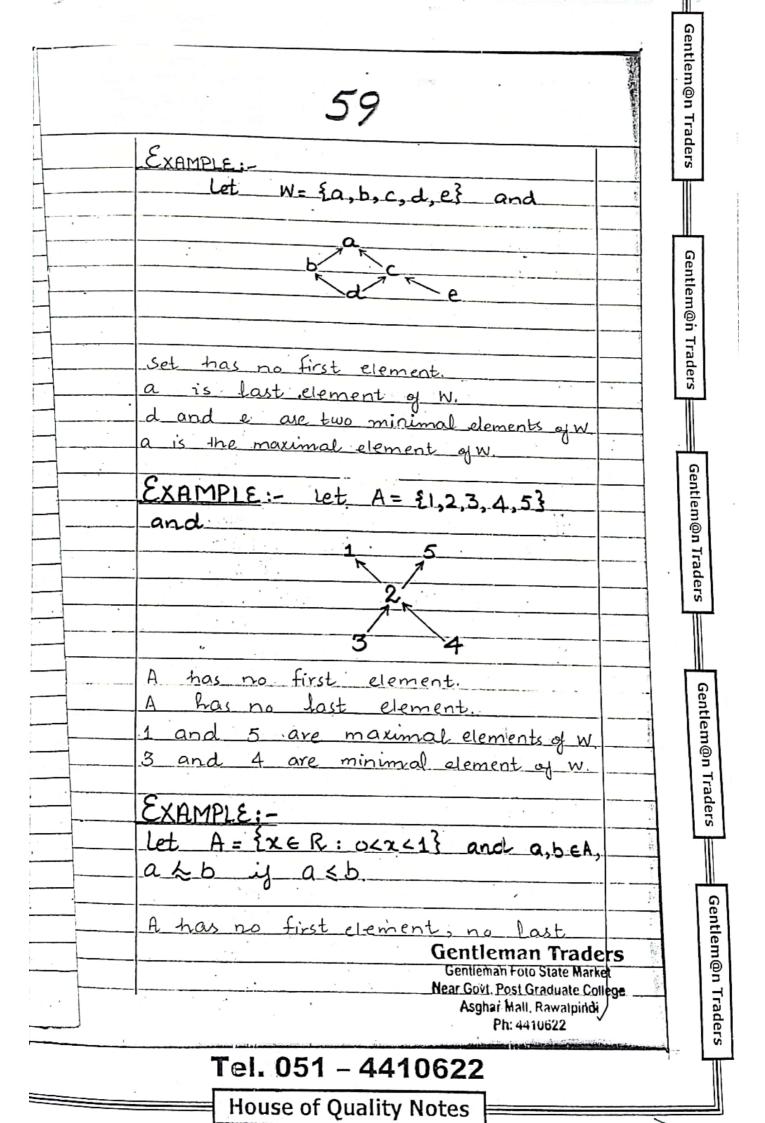
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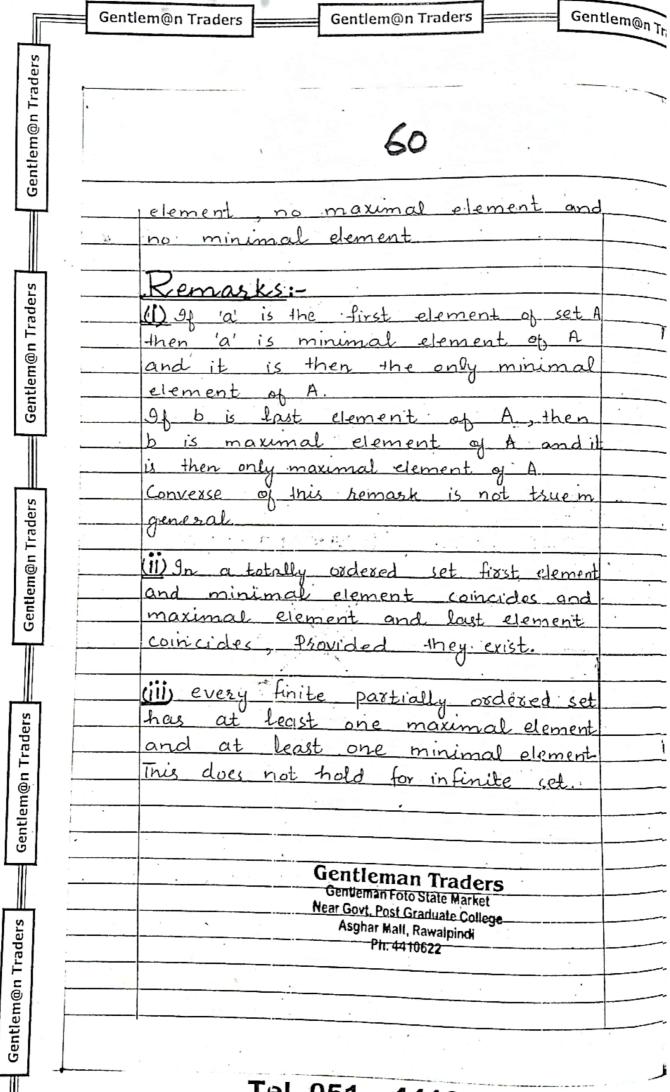




| lem@n Trac | lers Gentlem@n Traders Gentlem@n Traders | ı |
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| | Gentleman Traders | 1 |
| | 5 7 Gentleman Foto State Market Near Govt. Post Graduate College | |
| | Asghar Mall, Rawalpindi | 1 |
| | Ph: 4410622 | |
| N | -: 3TC | _ |
| <u> </u> | euther a b or b a then, we say | |
| a_ | and b are compareable. So in a poset | Г |
| <u>lit_</u> | is not necessary that every two ele- | |
| | ents are compareable, but in a total | |
| | lered set every two elements are | 1 |
| | paseable. | |
| KE | MARK-1- | |
| | A set X is said to be ordered | |
| set | if it is either partial ordered set | ٦ |
| 02 | totally ordered set. | |
| - 0 | | H |
| <u> </u> | BSET OF AN ORDERED SET :- | |
| Let | (A,R) be an ordered set and BCA, | |
| lhe | | |
| in_ | the way for x, y & B, x R'y ij x Ry. | |
| <u> +%o</u> | n this we can say every subset of an | |
| Oro | lesed set is again an ordered set | 4 |
| e.g | | |
| —————————————————————————————————————— | n, | L |
| - Ihe | n . | |
| | $\{(1,1),(1,2),(1,3),(1,4),(2,2),(2,3),(2,4),(3,3),$ | |
| | (3,4), (4,4) | |
| | id B= \$1,33 cA | |
| Po | $= \{(1.1), (1.3), (3.3)\}$ | |
| C | MARK:- | |
| Eve | ex subset of a totally ordered set is totally | ٦ |
| _ | Converse & not telle | ار |
| gen | eral eg; A = {1,2,3,,8} | ۲ |
| | | |
| | | |
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Gentleman Traders

Gentleman Foto State Market Near Govt. Post Graduate College

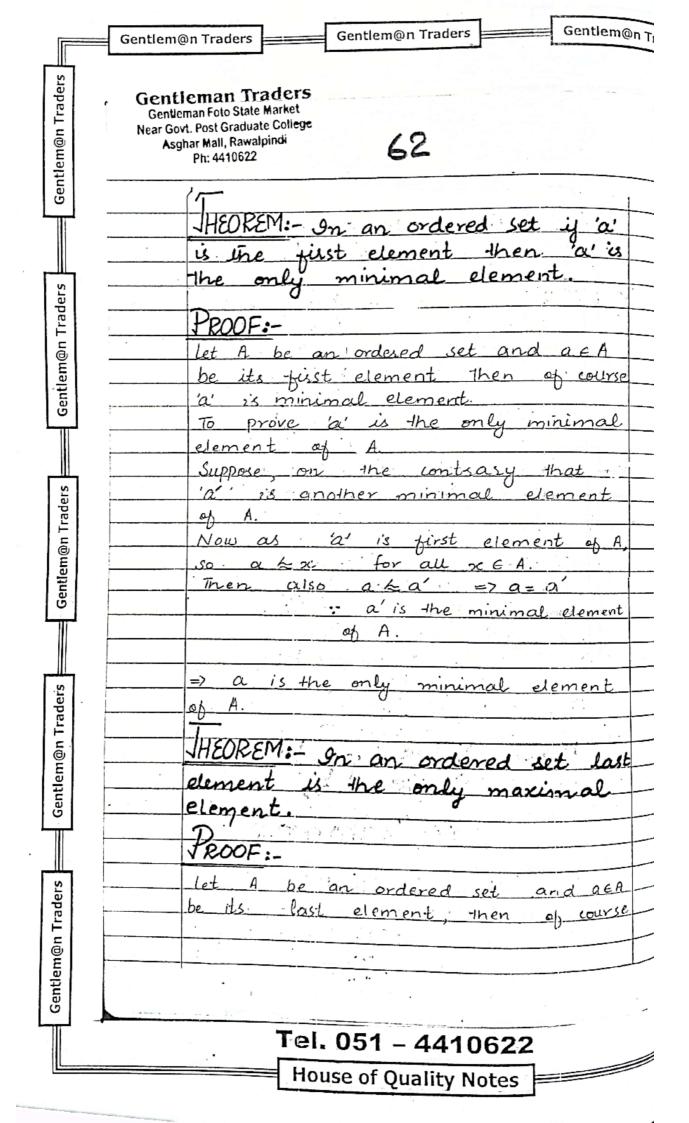
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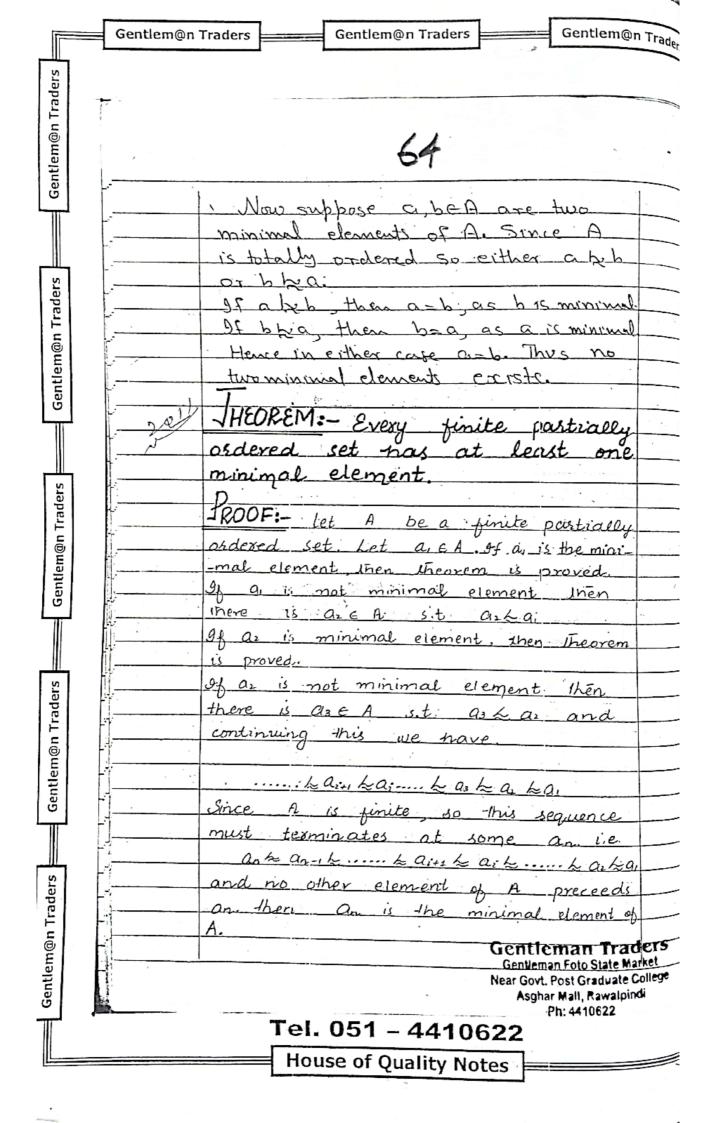
an ordered last elements are unique.

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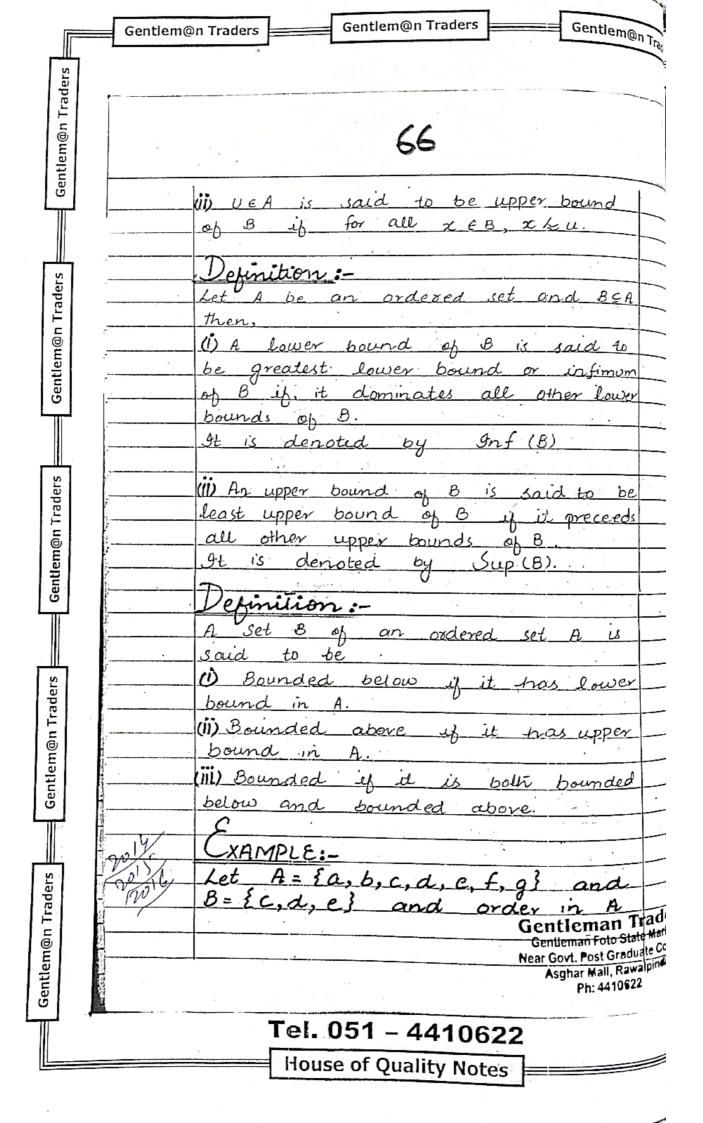
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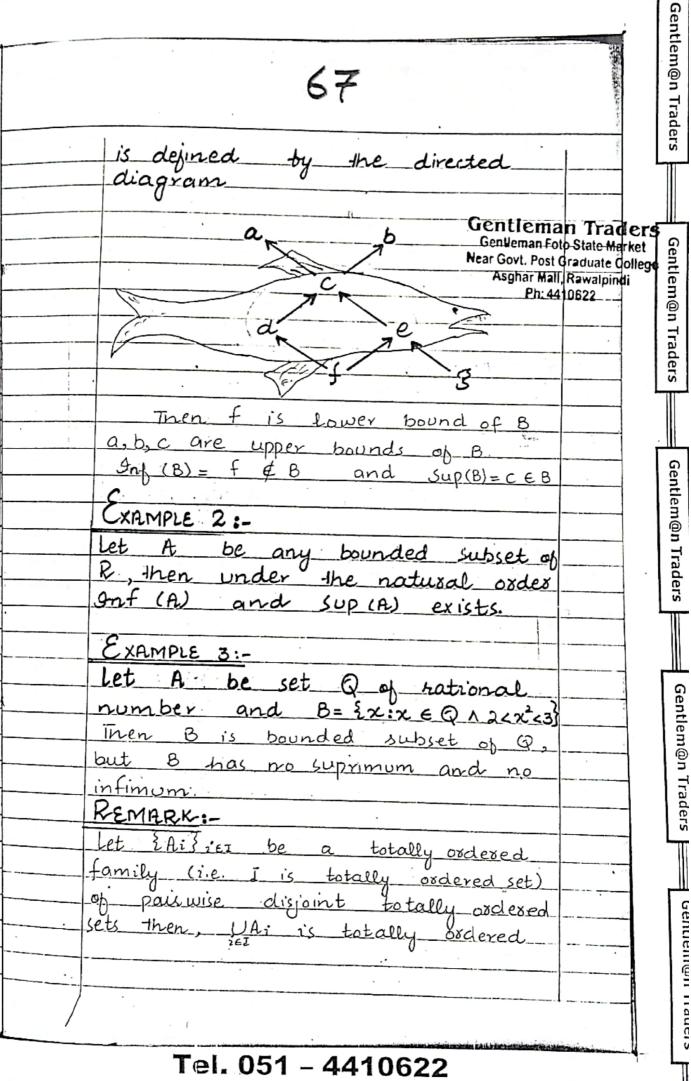
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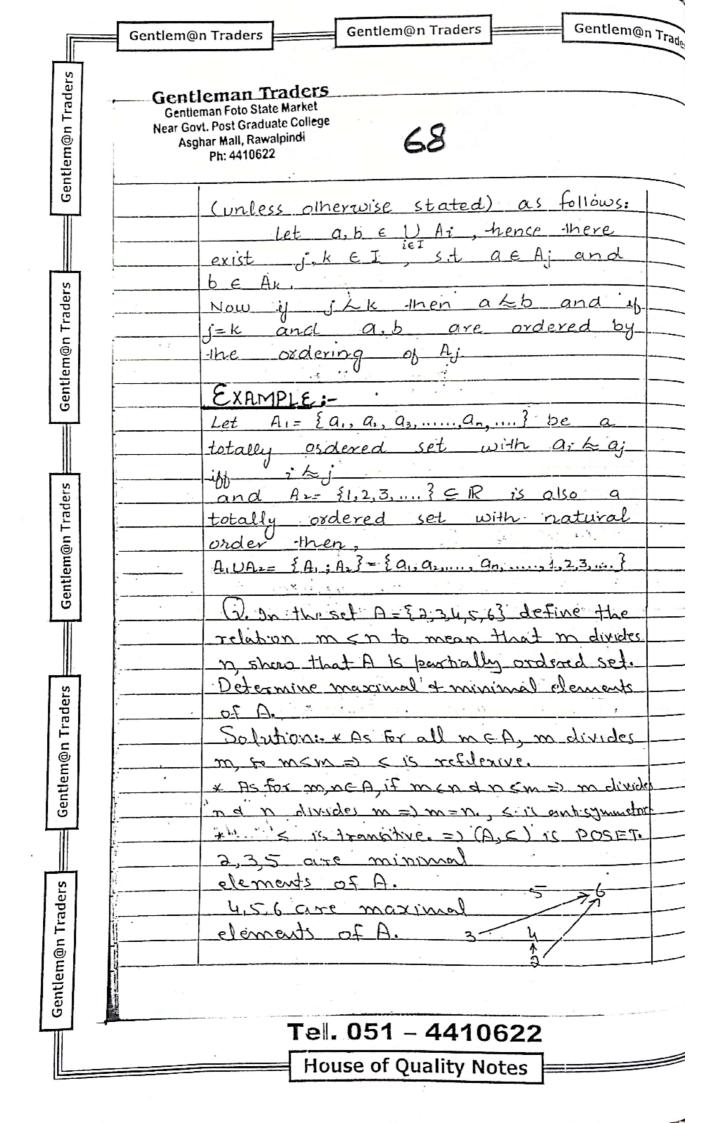


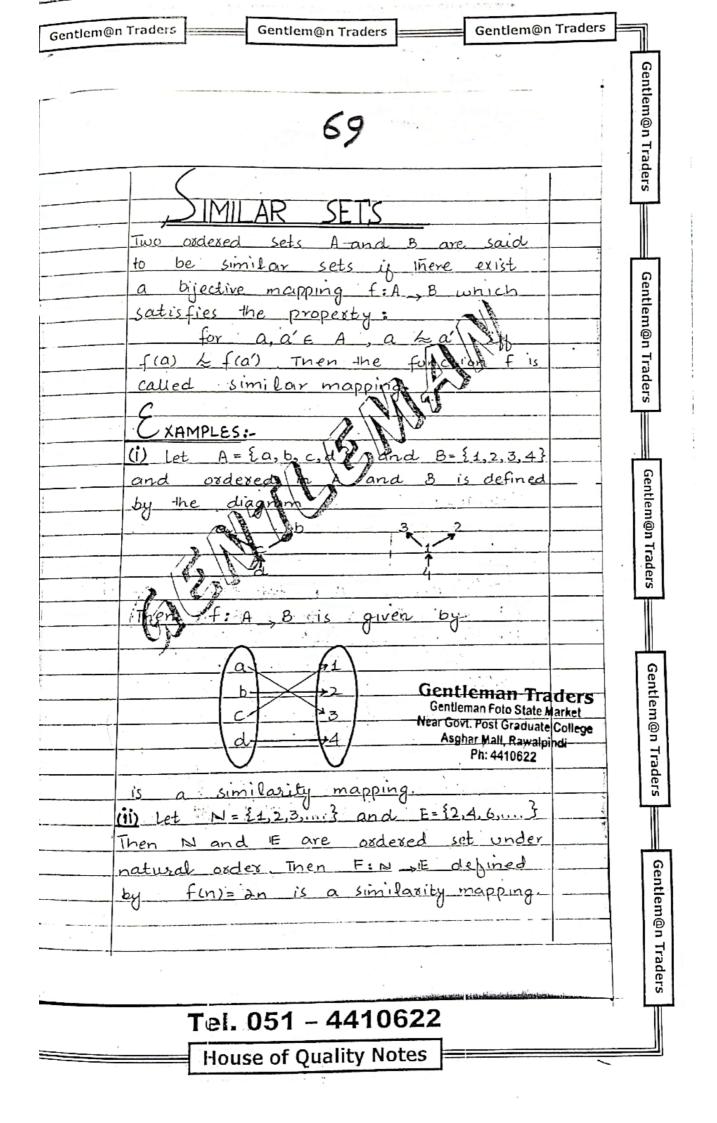


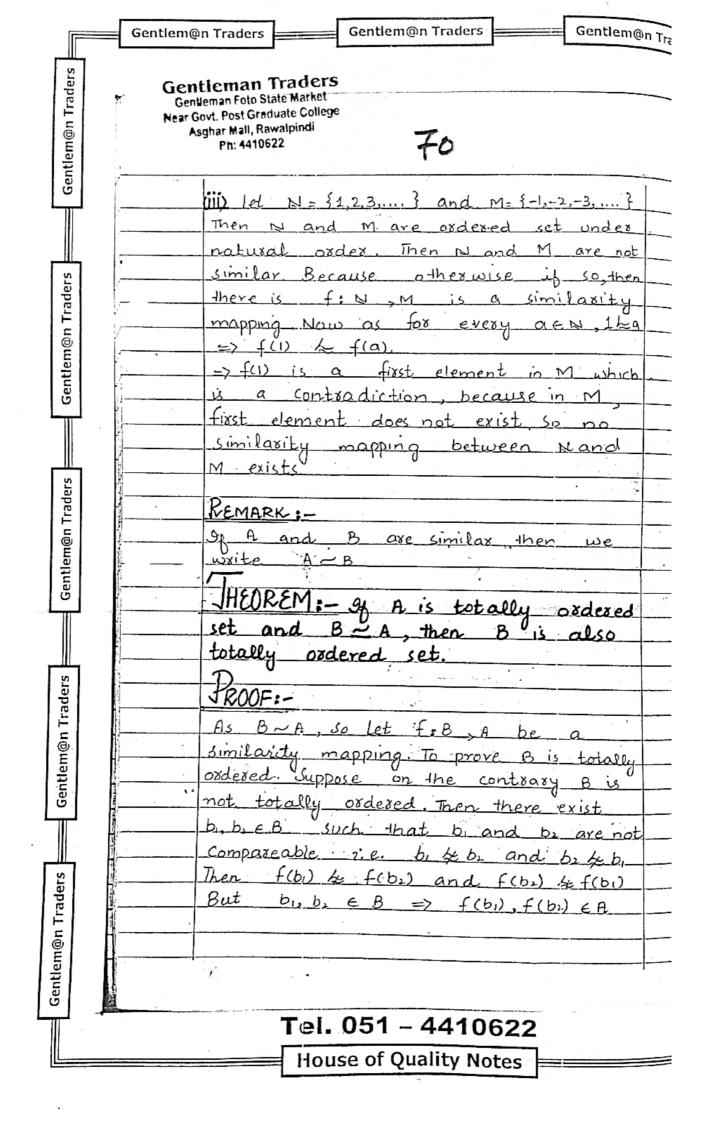
| | 65 Gentleman Tra Gentleman Foto State N Near Govt. Post Graduate |
|---|---|
| X | Asghar Mall, Rawalpi Ph: 4410622 |
| | HEOREM: - Every finite partially ordered set have at least one maximal element. |
| | set have at least one maximal |
| | element. |
| | Penns |
| | TROOF: - Let A be any finite partially ord- |
| | -coed set het die H, of ai is maximal |
| | element then theorem is proved. |
| | 96 a, is not maximal element then |
| | there is $a_1 \in A$ s.t $a_1 \not = a_2$ |
| | 9/ 92 is maximal element then theorem |
| | is proved 91 as is not maximal element |
| 1 | then there is a3 EA s.t a2 La3 |
| | By continuoing this we have |
| | Since A is finite, so then this sequence |
| | must terminates at some an. |
| | i.e. |
| , | a, & a, & a, & & a, & air, & an |
| | |
| | and no other element of A domina- |
| | -tes an |
| | -> an is the maximal element of A. |
| | |
| | |
| | Definition: |
| | Let A be an ordered set and BCA |
| | then an element |
| | to be lower bound |
| , | of B, if for all $x \in B$, $l \leftarrow x$ |

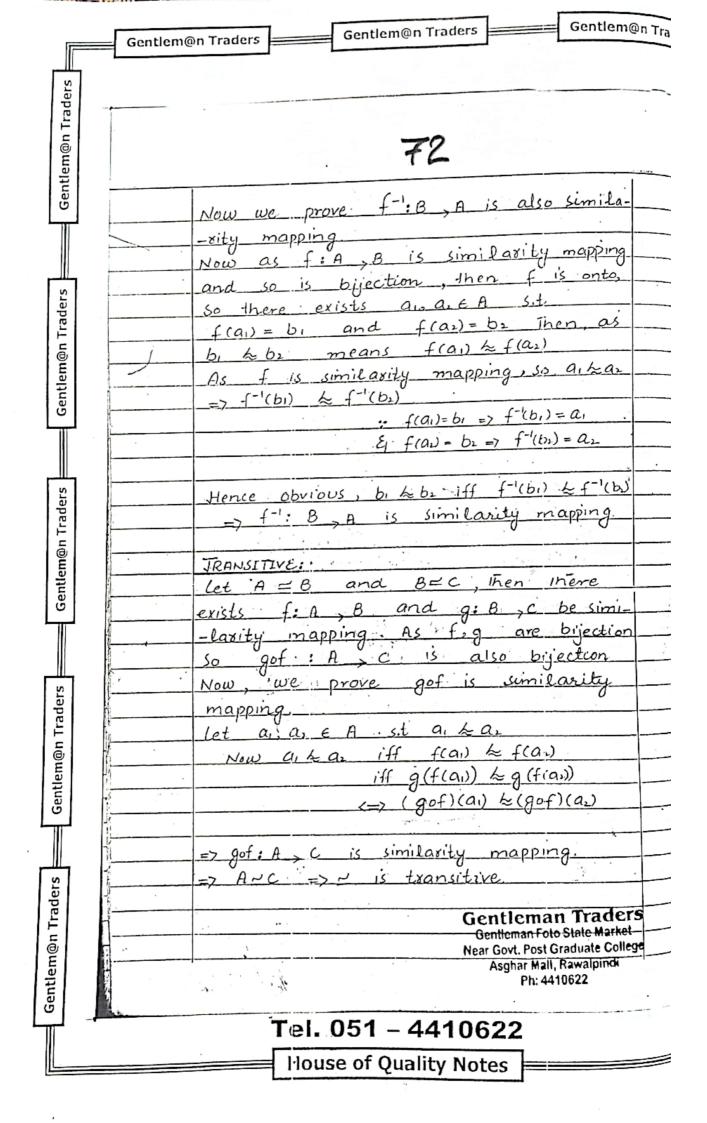










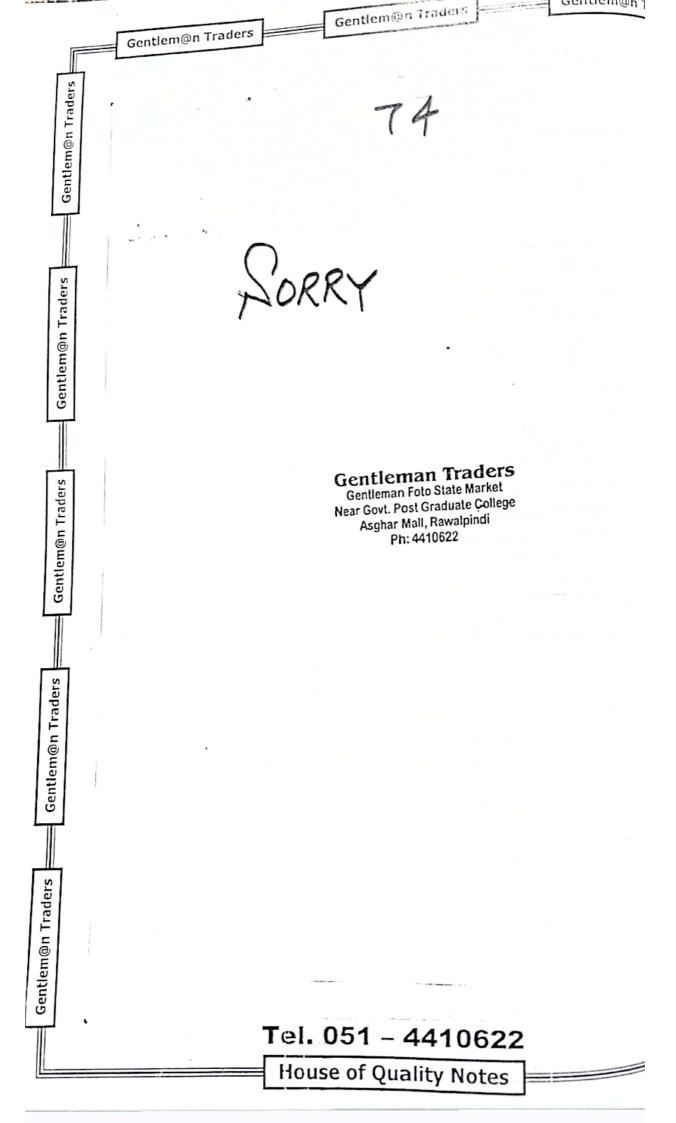


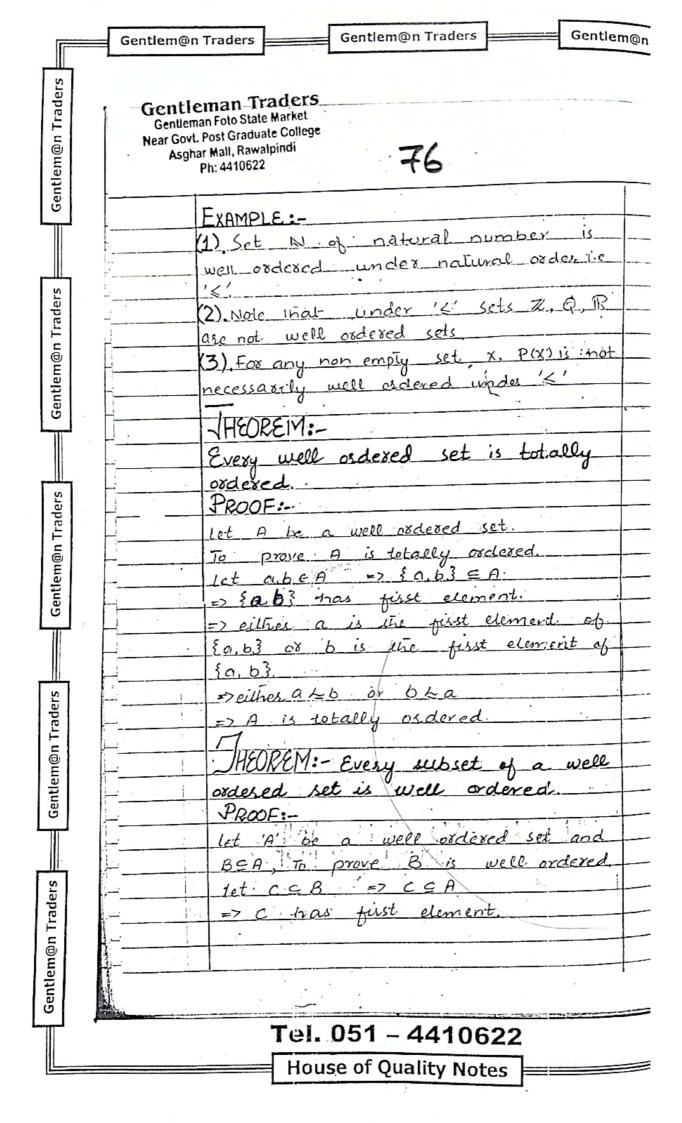
equivalance Similarity sets is an relation. PROOF:f(a) Conversely f(X) EB 442154 Gentleman Traders Gentleman Foto State Market Near Goyt. Post Graduate College Asghar Mall, Rawalpindi

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House of Quality Notes





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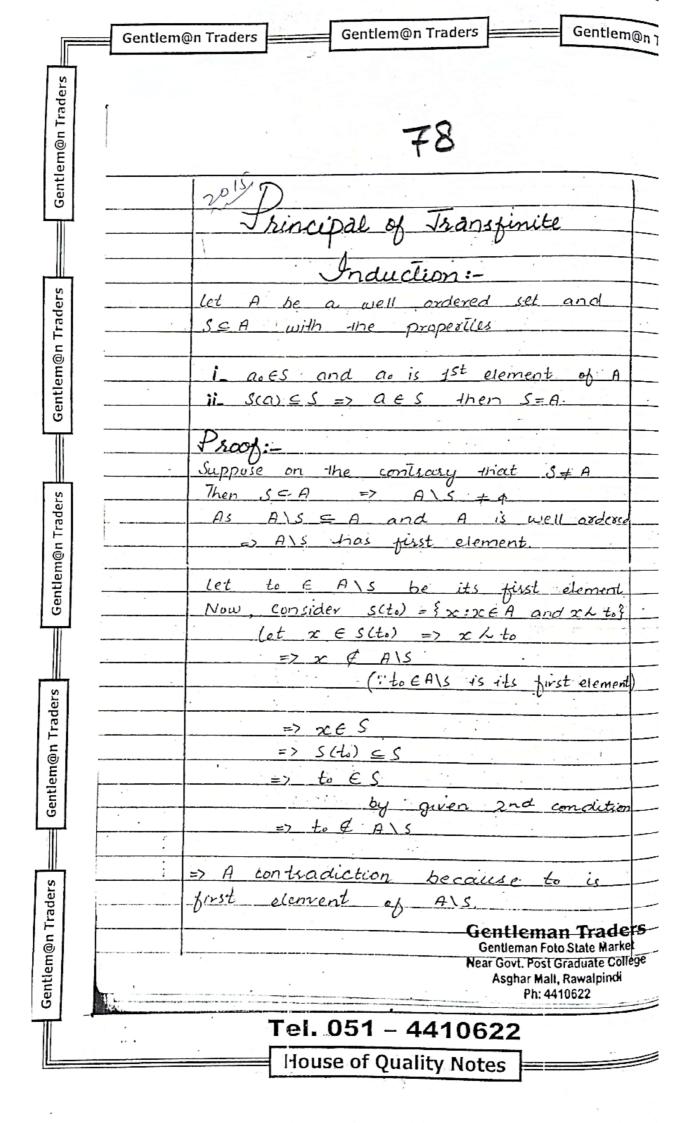
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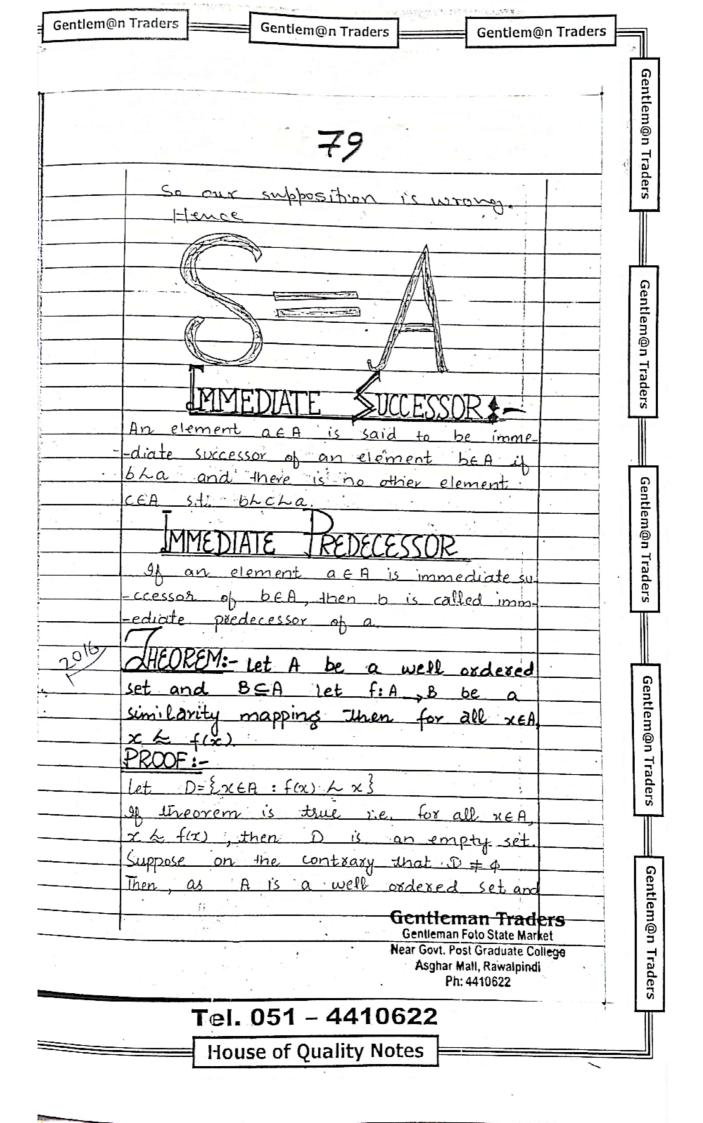
| (because A is well ordered) | |
|---|------|
| => B is well ordered | |
| | |
| TRINCIPAL OF | |
| | |
| MATHEMATICAL INDUCTION | |
| Let SEN with the properties. | |
| $0)$ 1 ϵ 3 | |
| (ii) for nes => n+1 es Thenis=N. | |
| THE CONTRACTOR | |
| INITIAL SEGMENTS: Let A be a well | |
| ordered set and a ca, Then initial segment | 7 |
| of a is denoted and defined as: S(a) = {x: x ∈ A and x La} | |
| | |
| Note that a A s(a) | |
| EXAMPLE:- | 1100 |
| (1). Let nEN and under natural order | |
| '≤', S(n)= {1,2,3,, n-1} | |
| | |
| (2) let A= {1,3,5,} and B= {2,4,6,} | |
| Even both A and B are well ordered | |
| under natural order Then | · · |
| {A; B} = {1,3,5, | |
| Note that S(5)= {1,3} | - |
| | |
| 5(2) = {1, 3, 5, } and 5(4) = {1,3,5,,2} | |
| | |

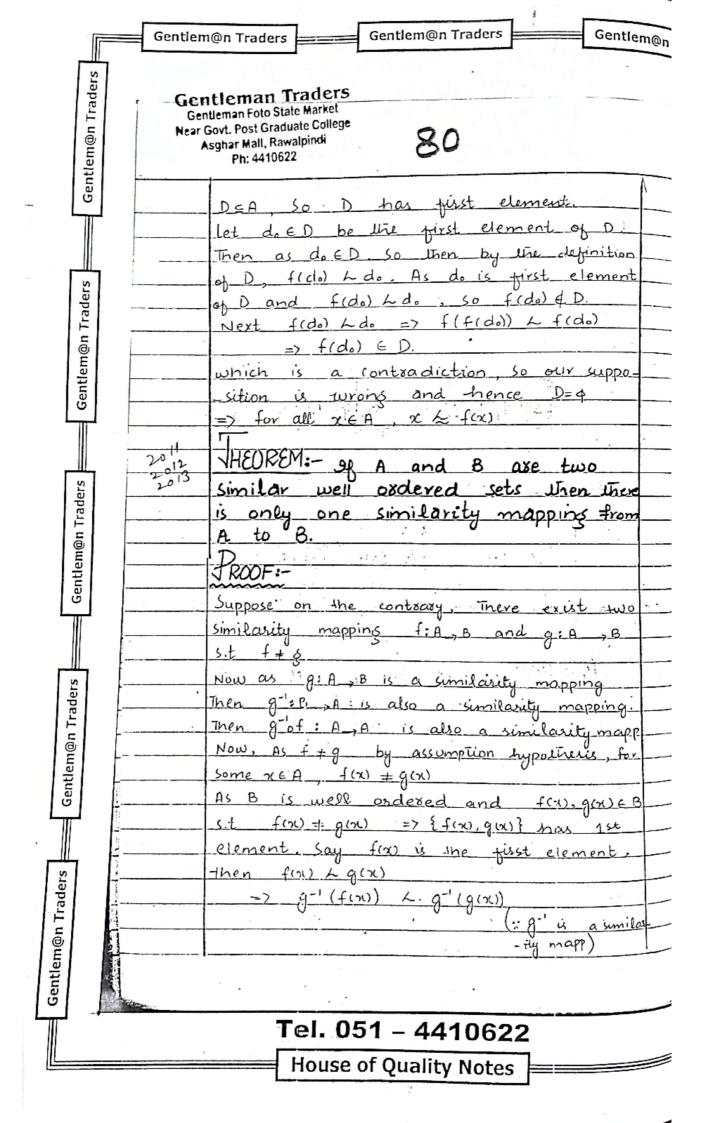
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Gentleman Foto State Market
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Tel. 051 - 4410622

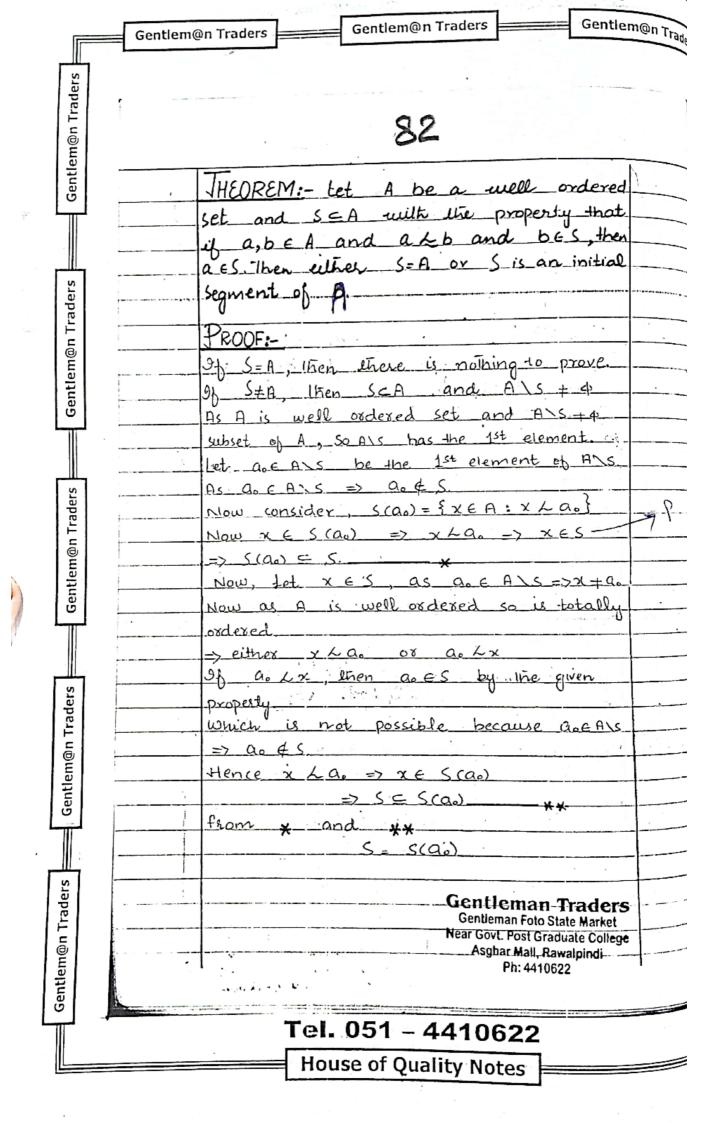
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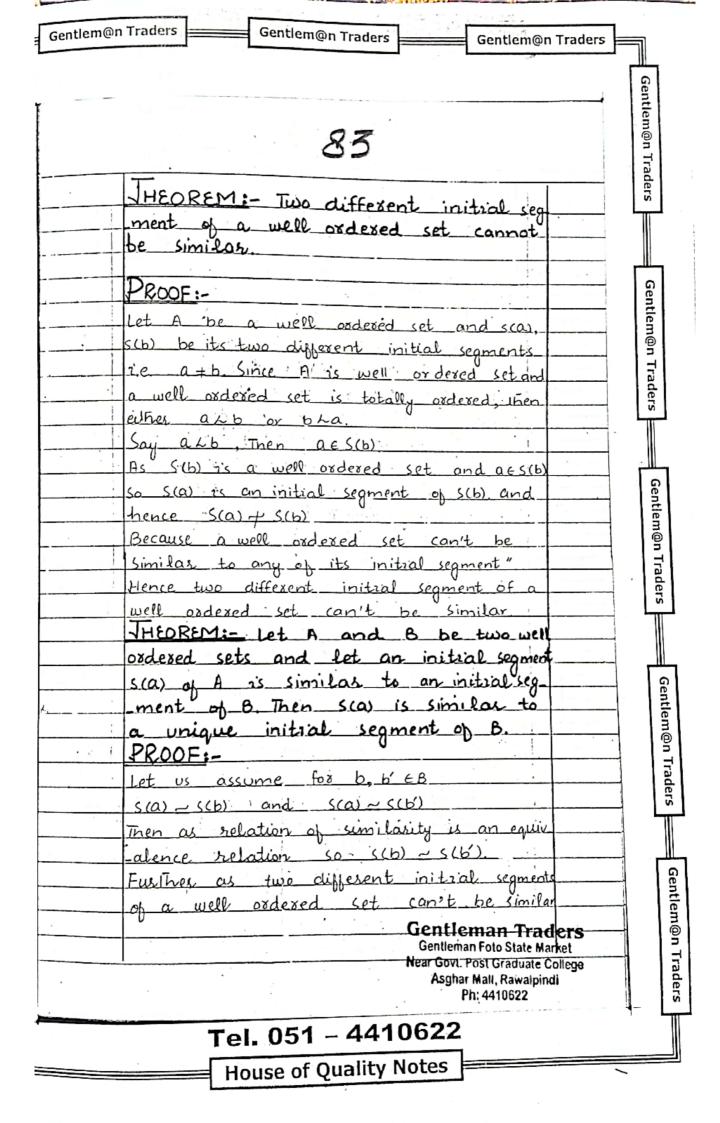


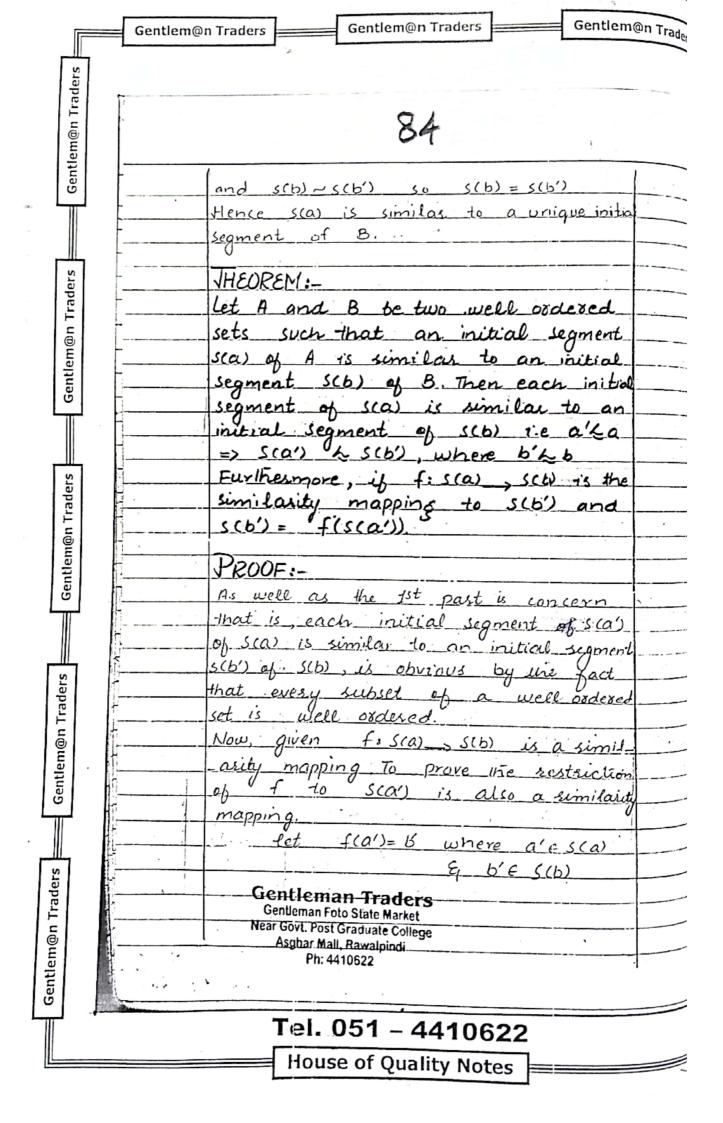




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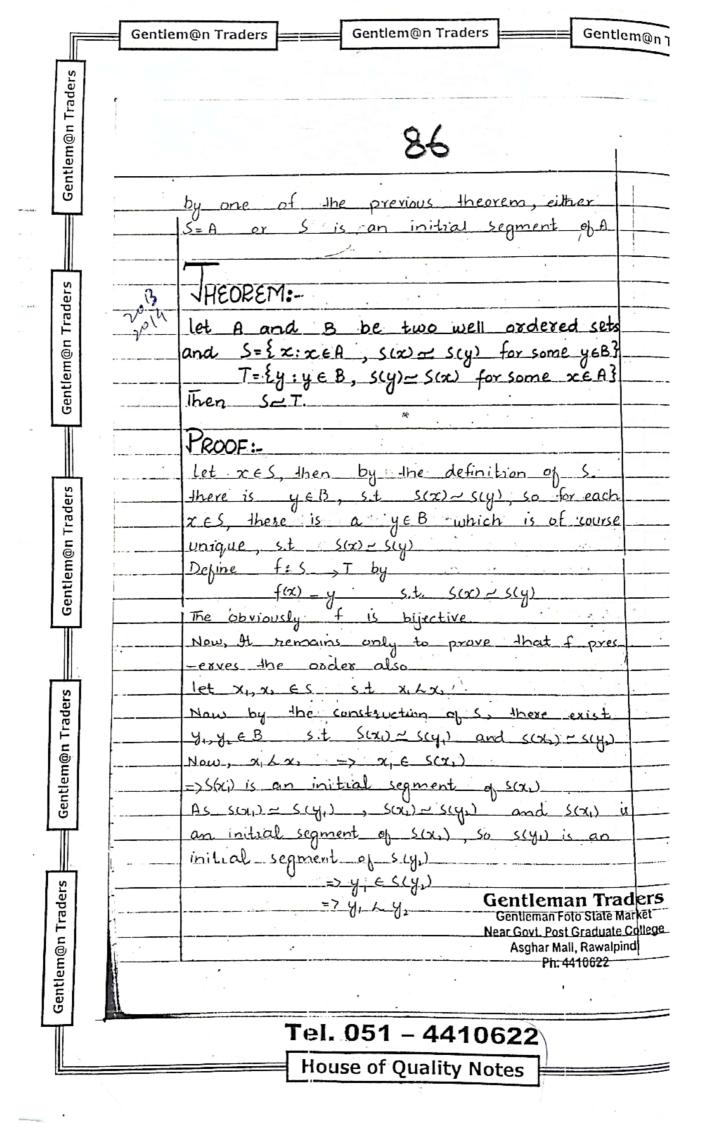






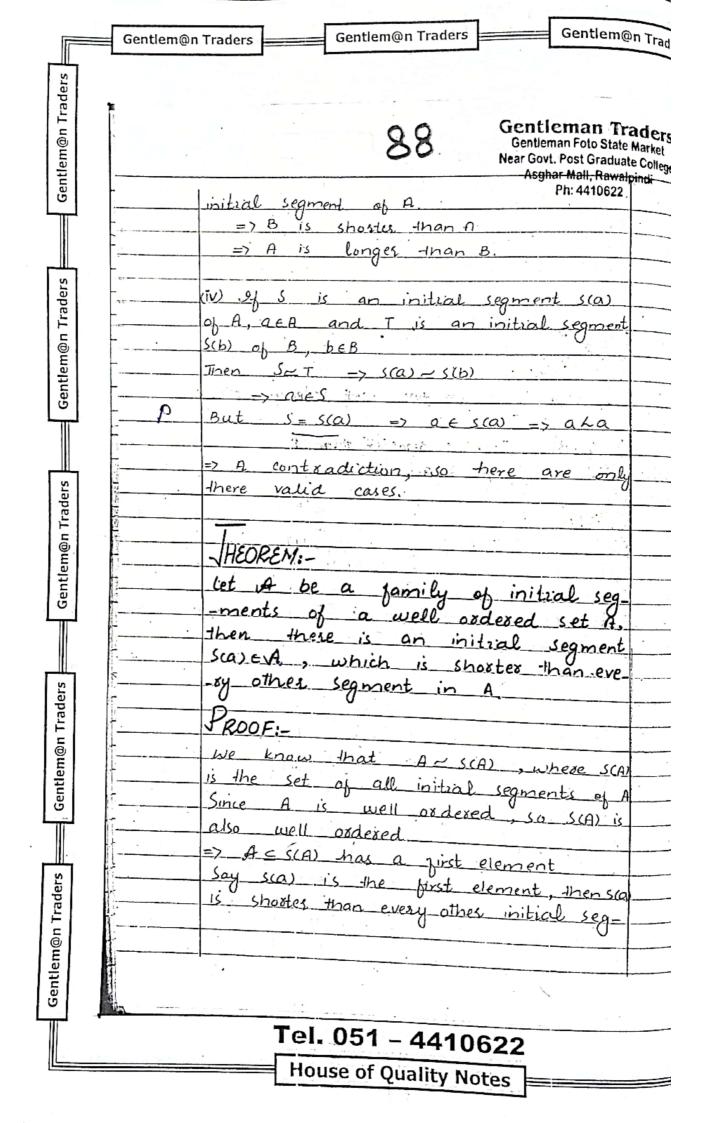
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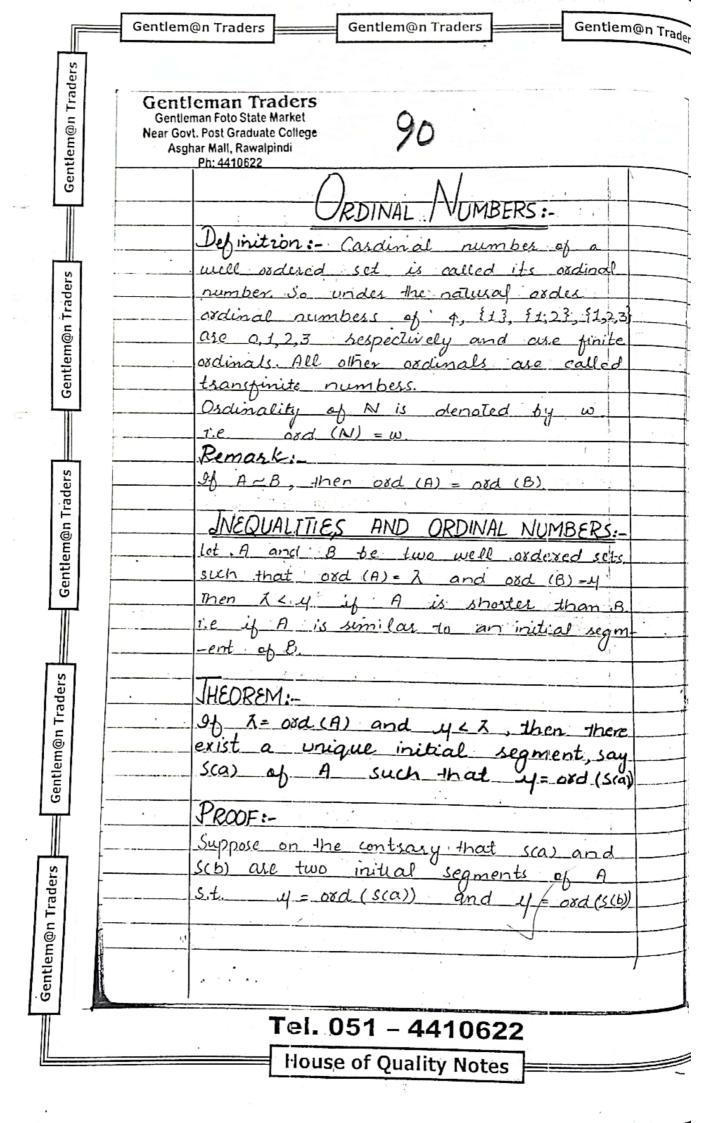
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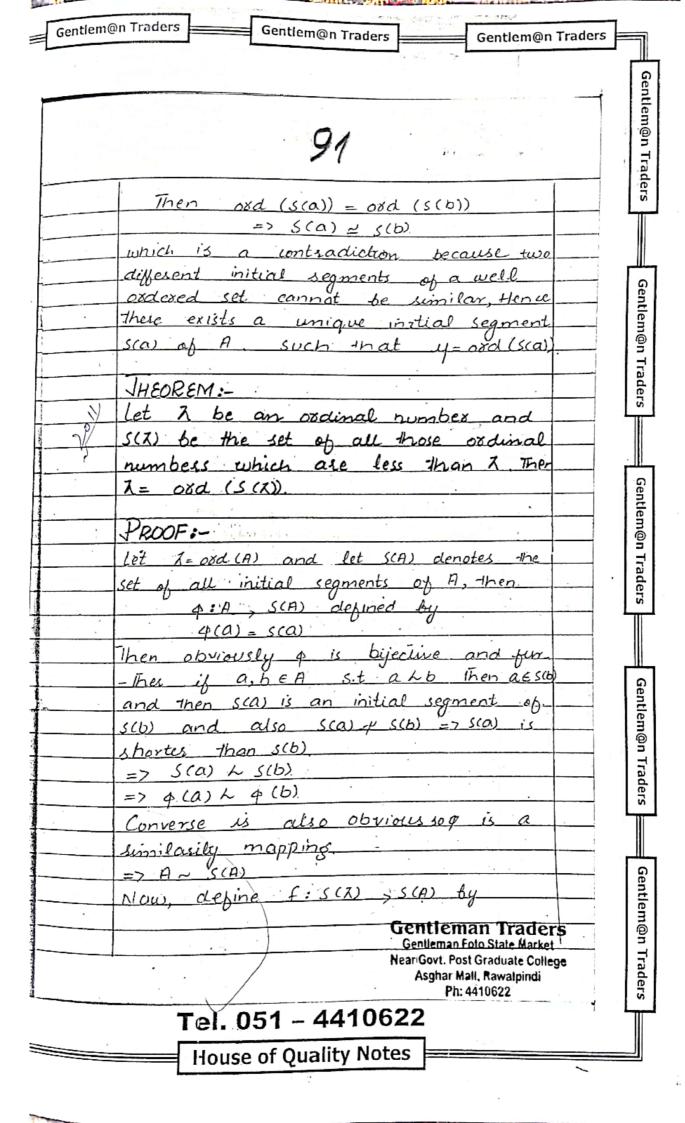


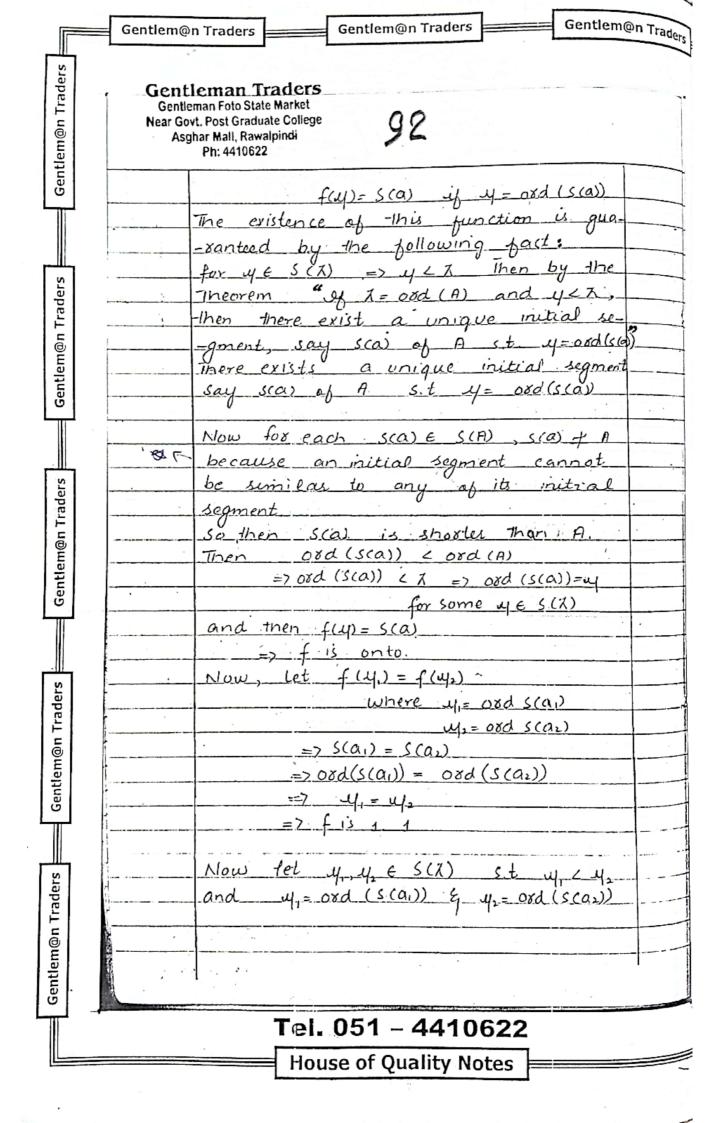
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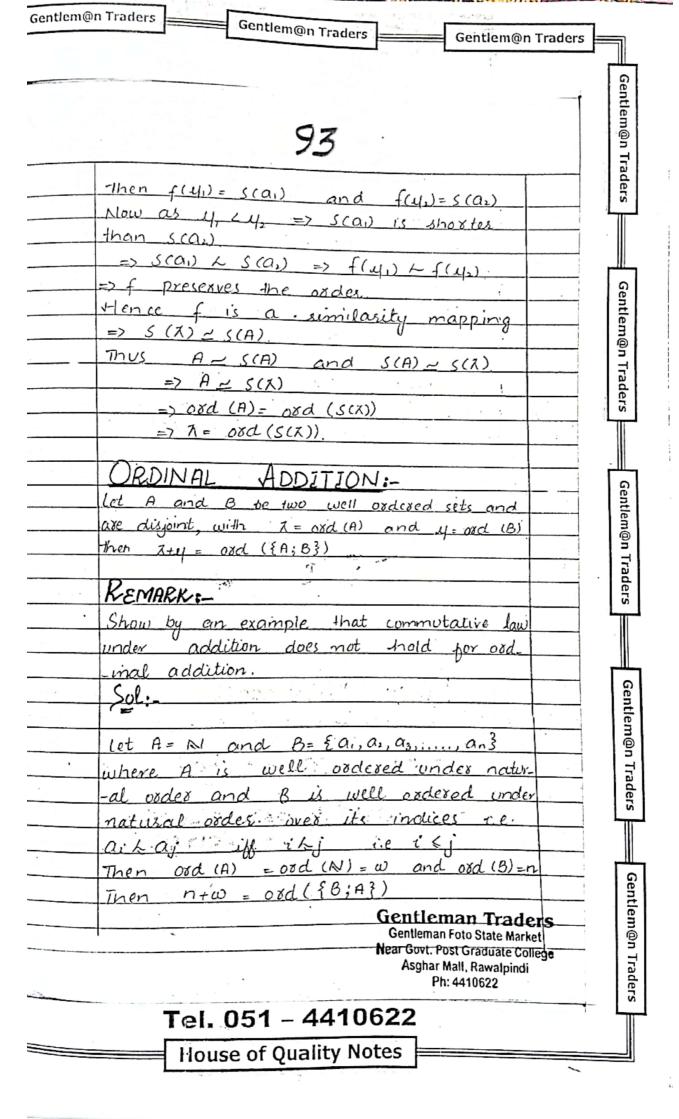
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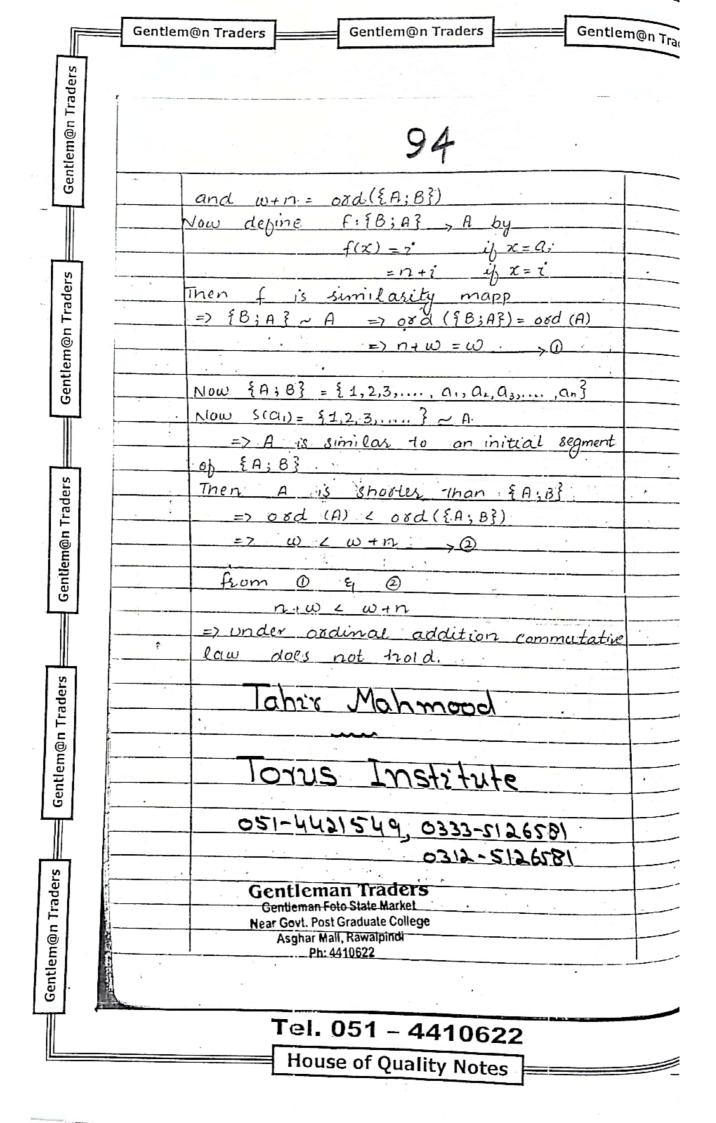


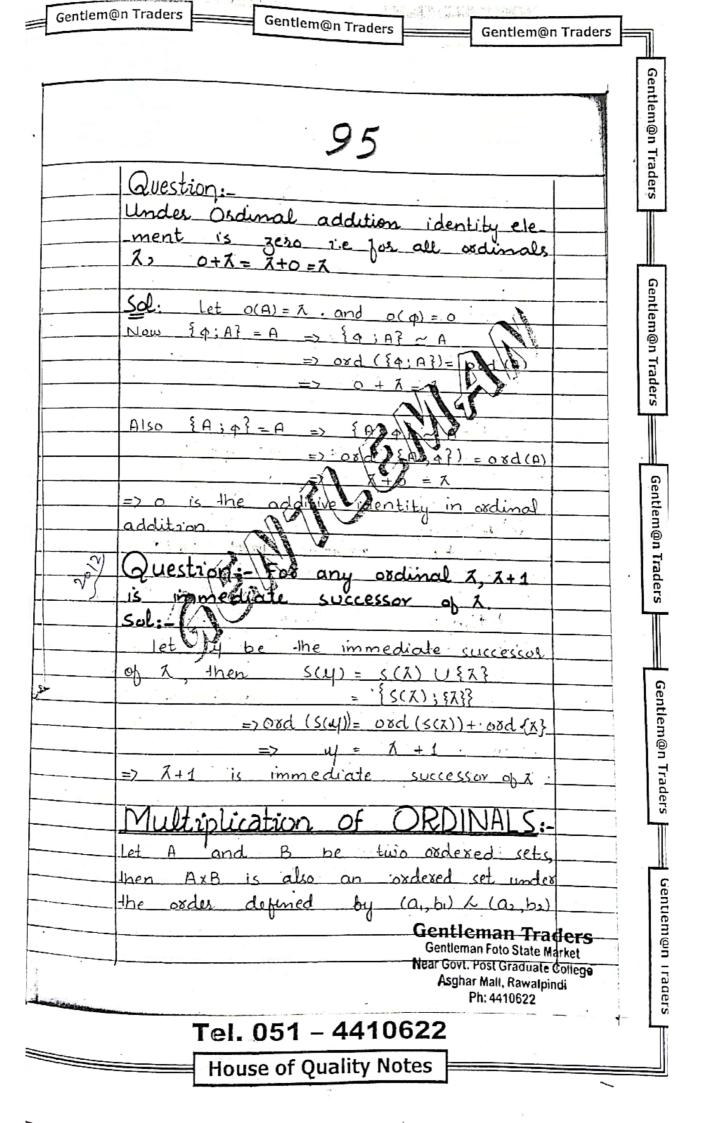


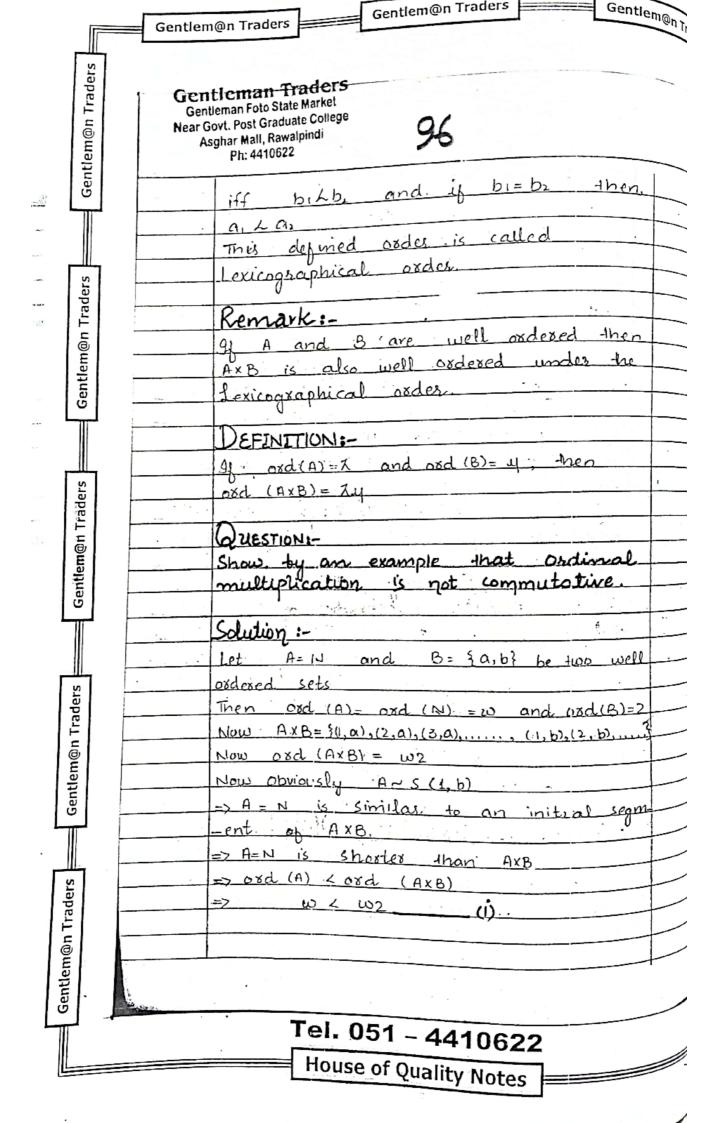


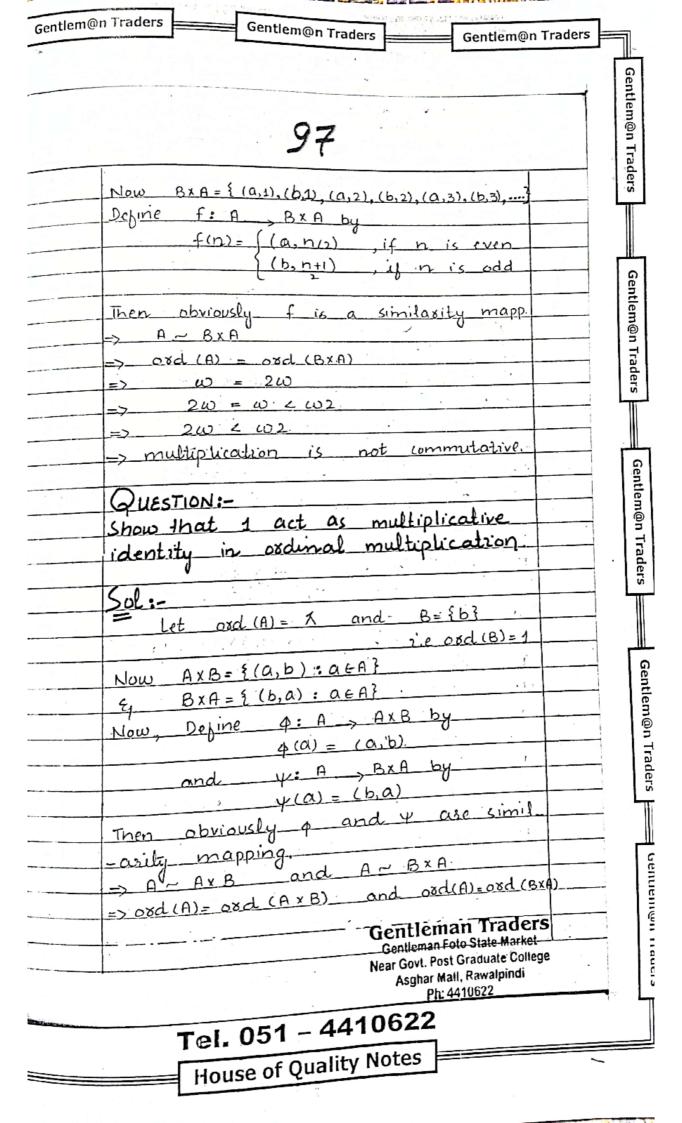


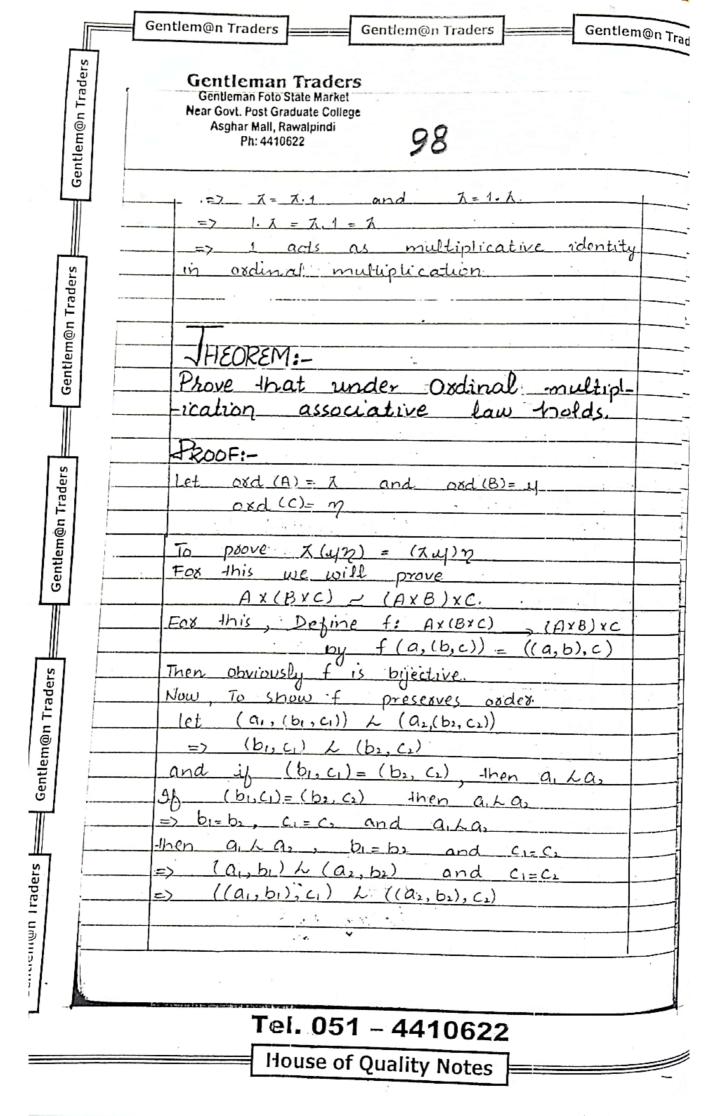


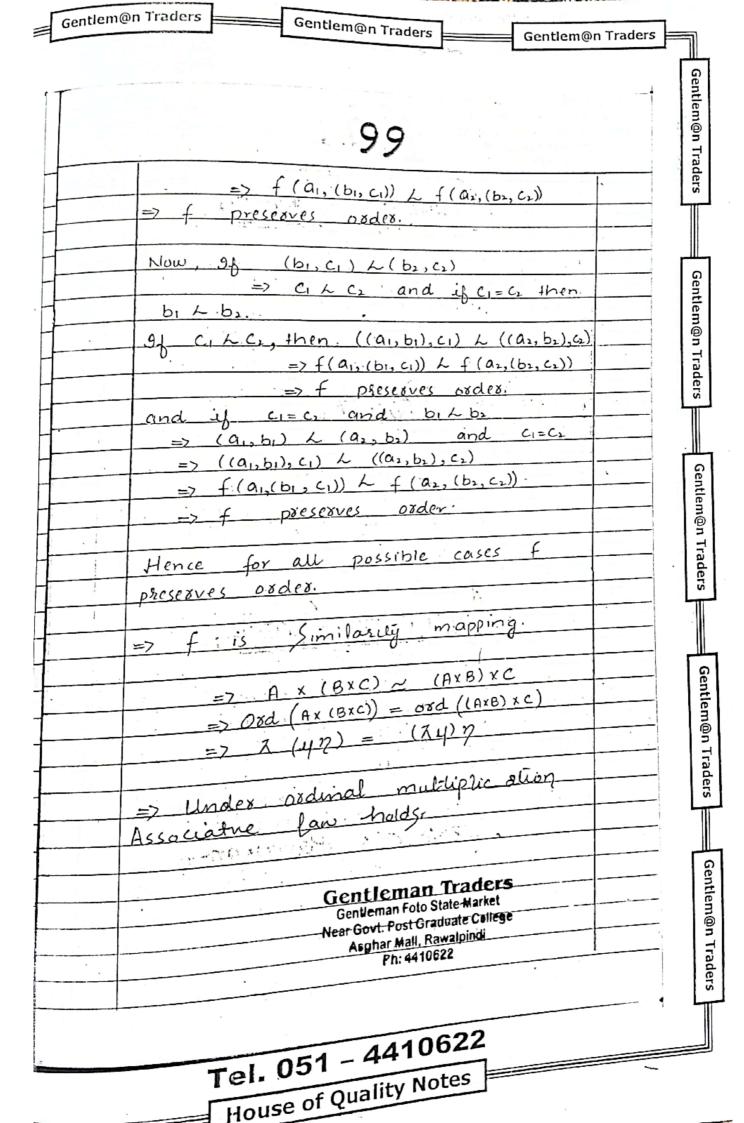


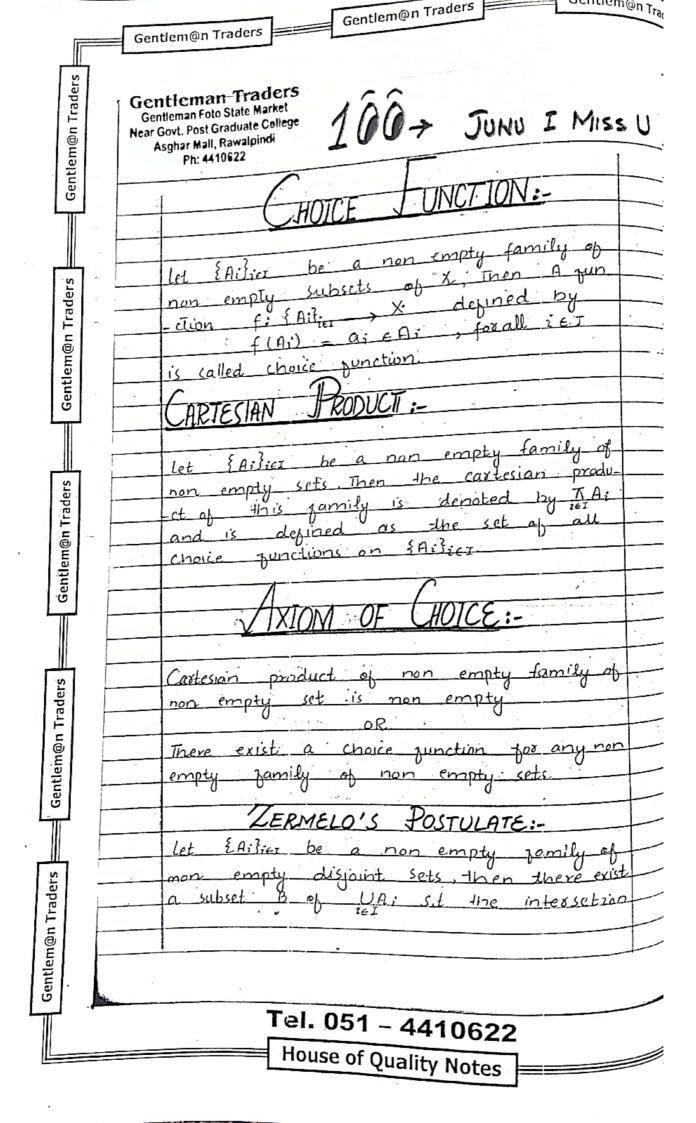


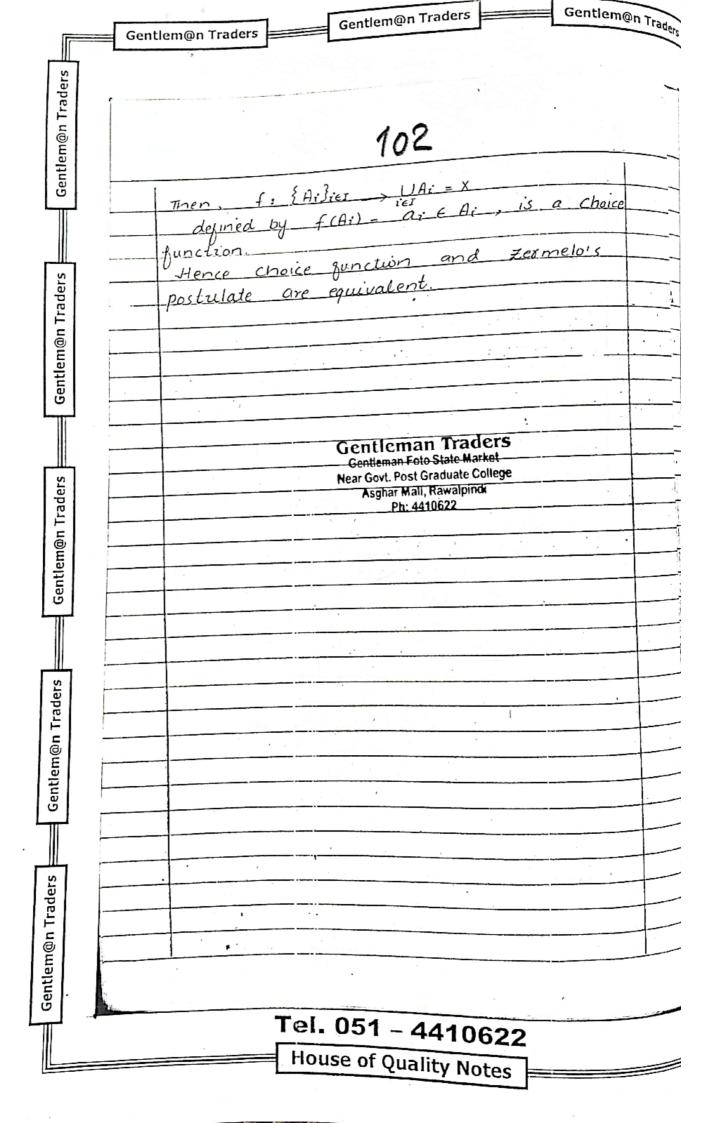


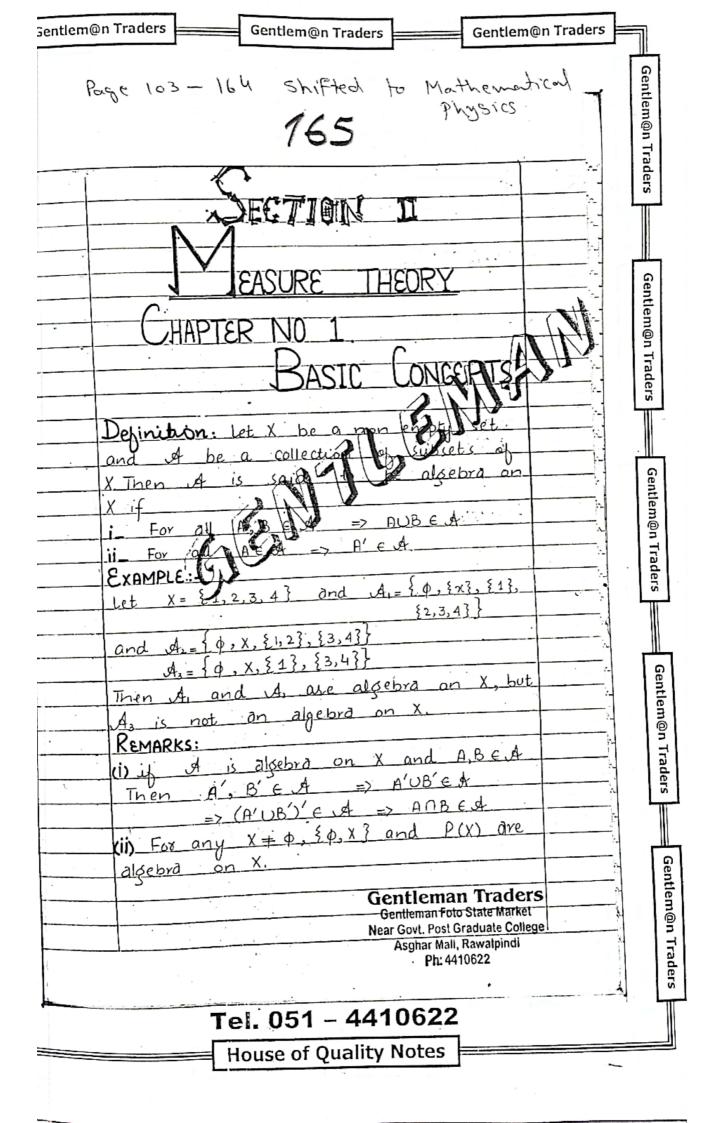


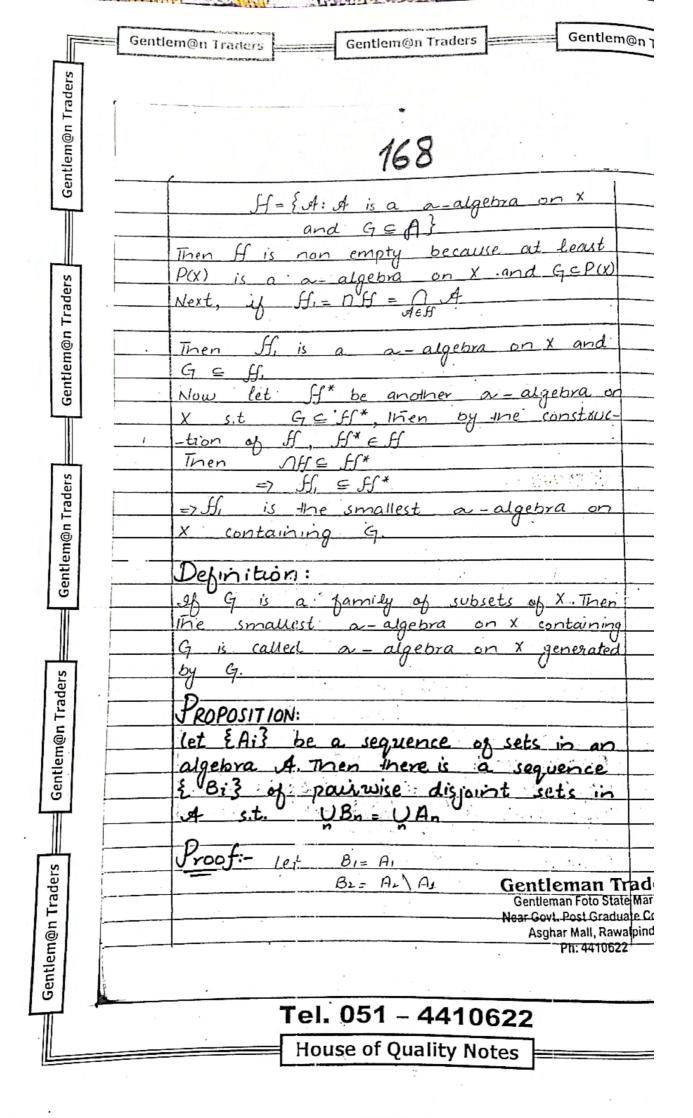


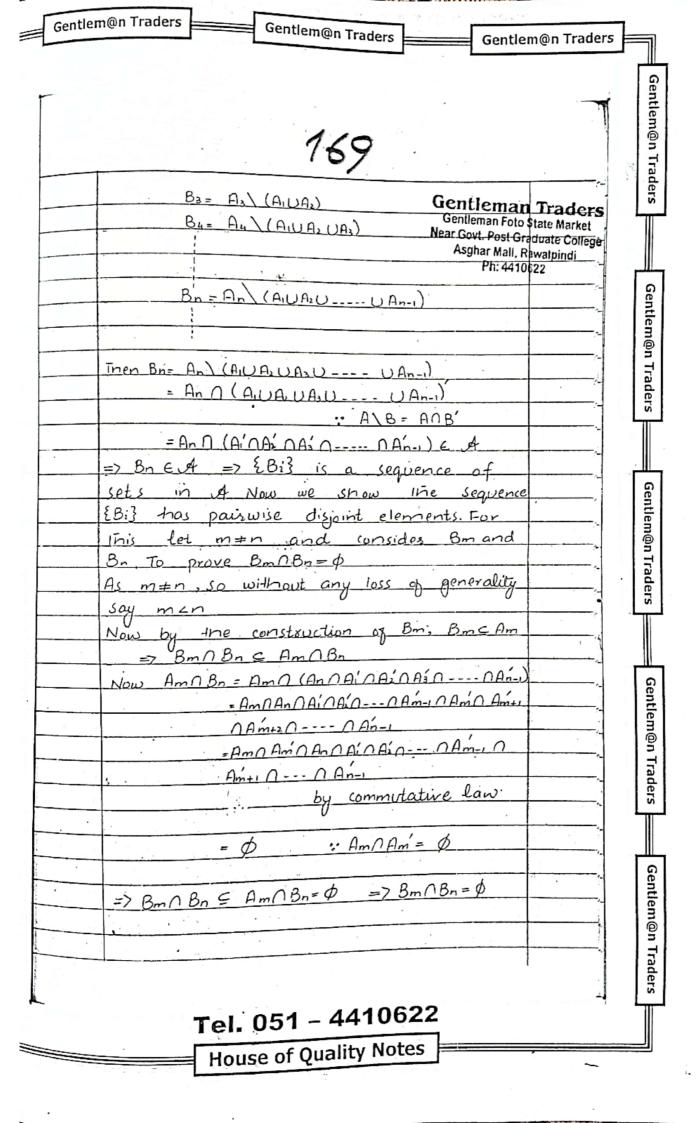


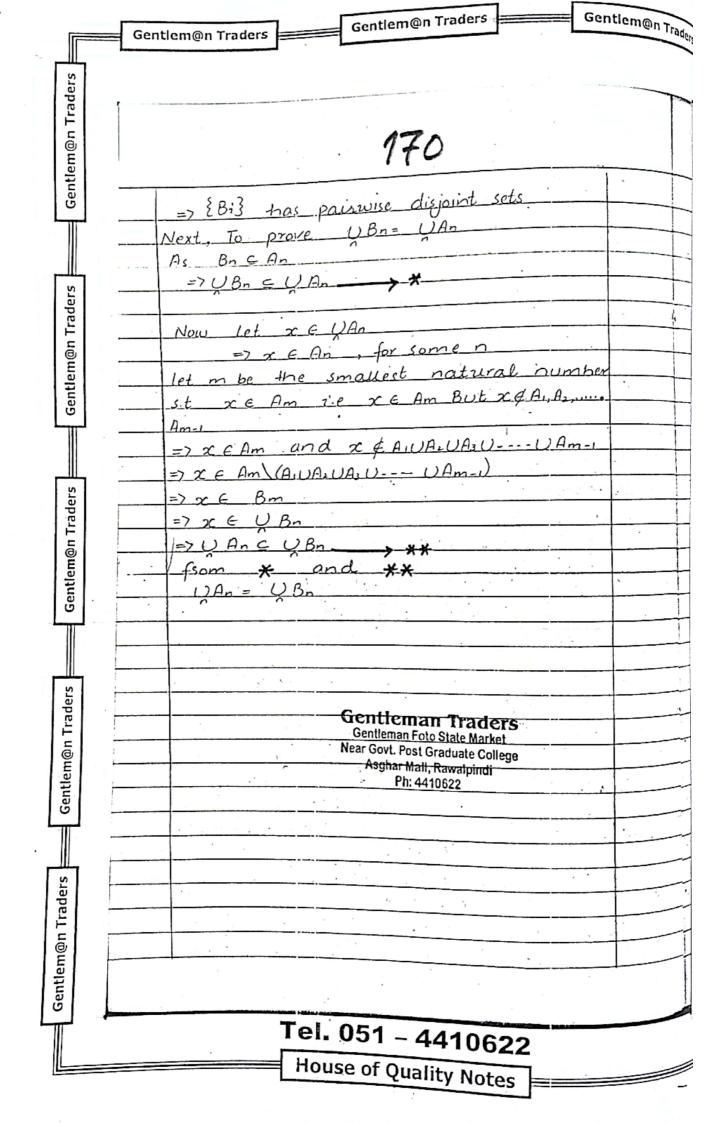


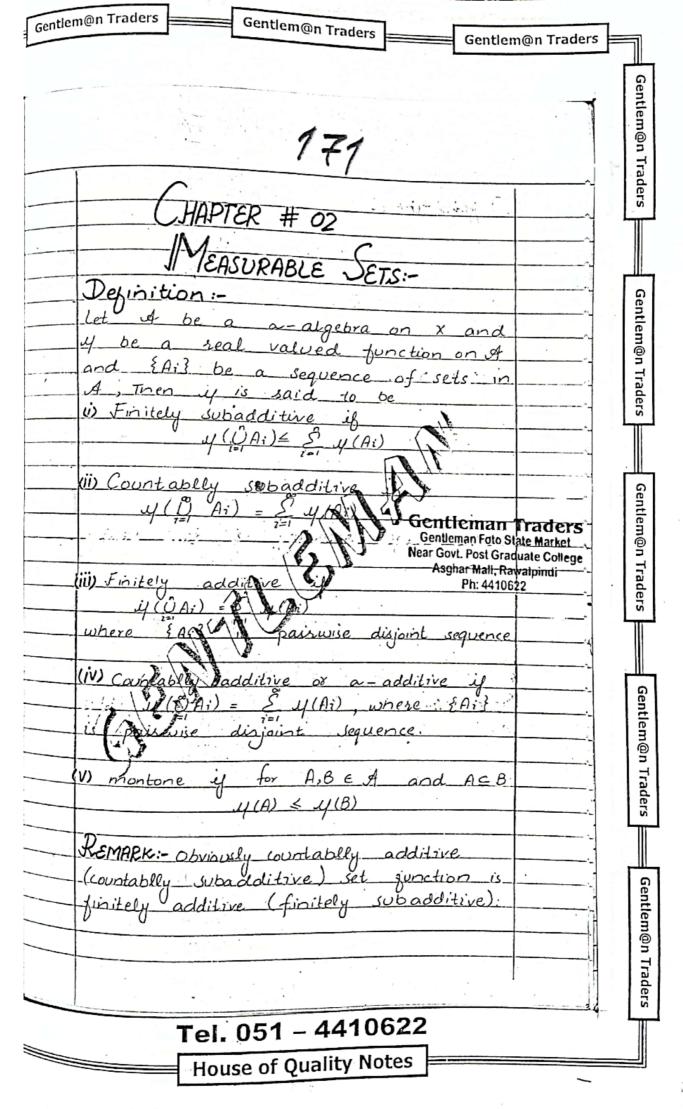




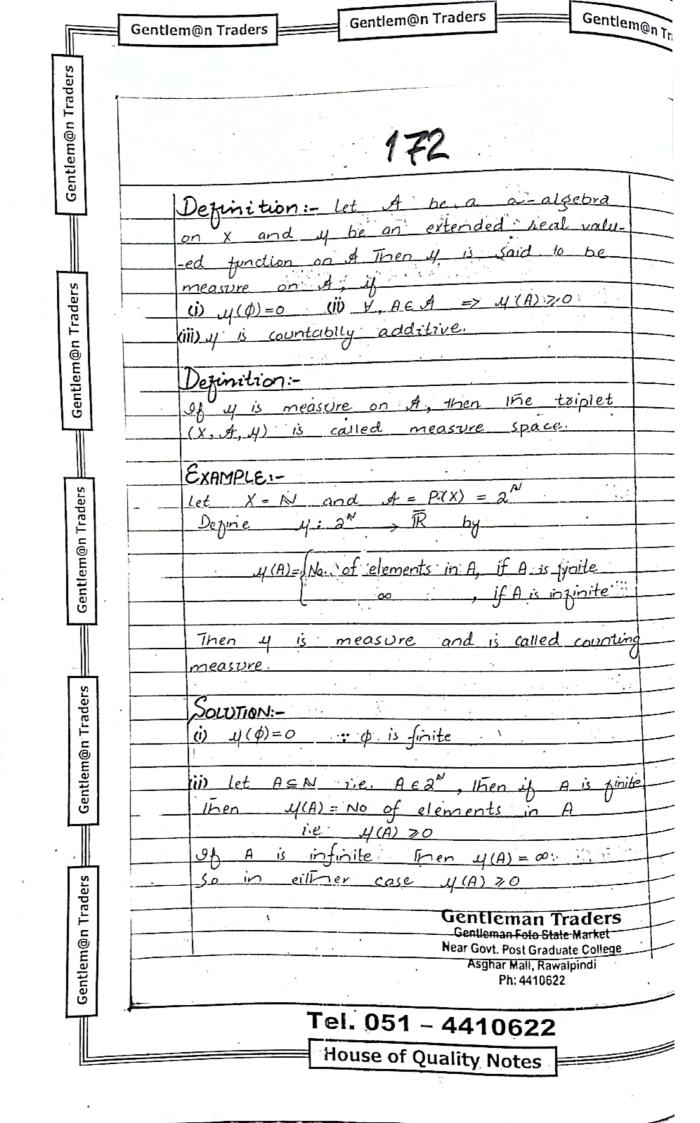


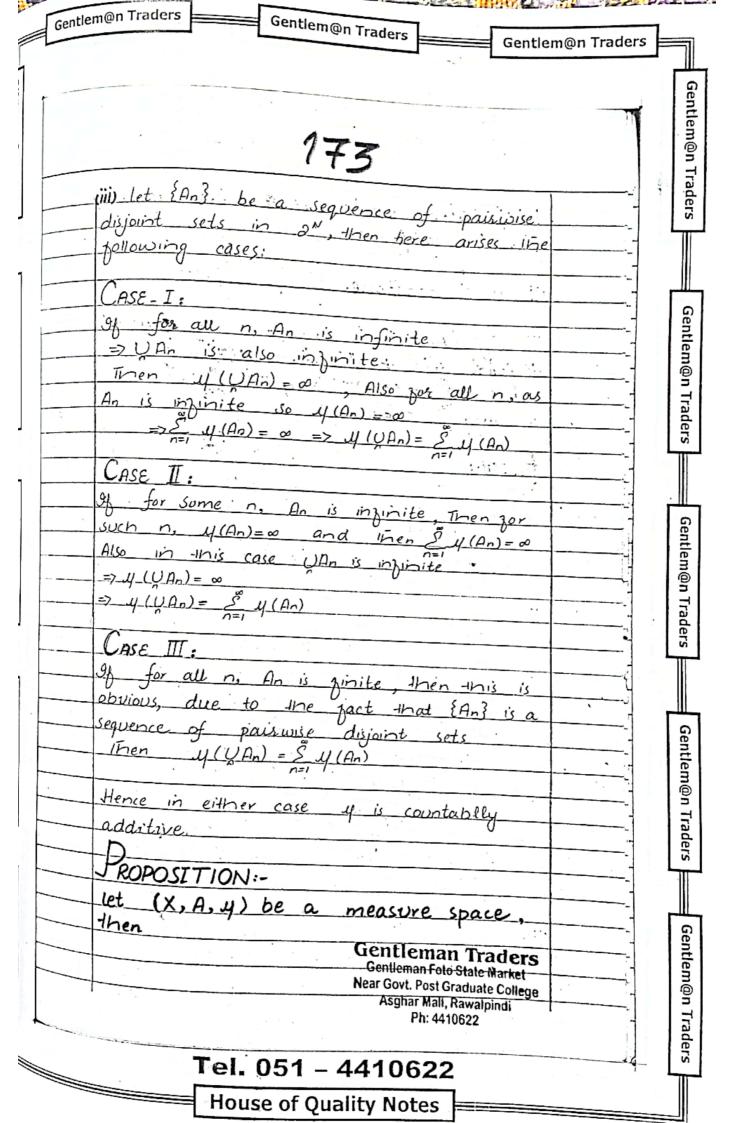


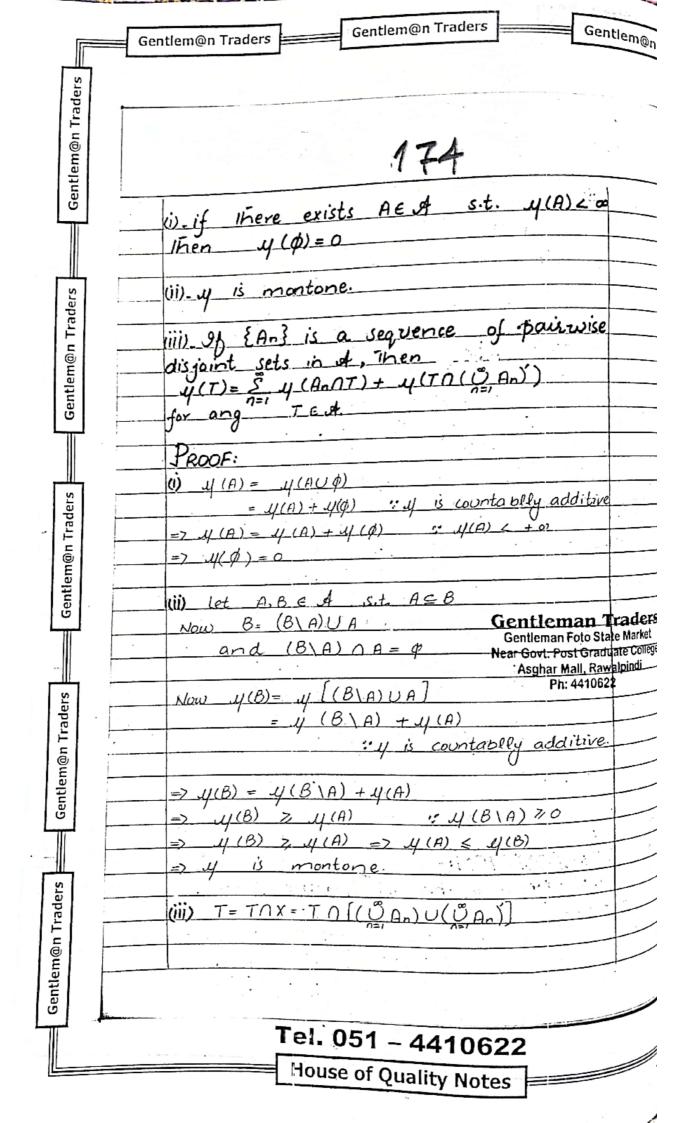


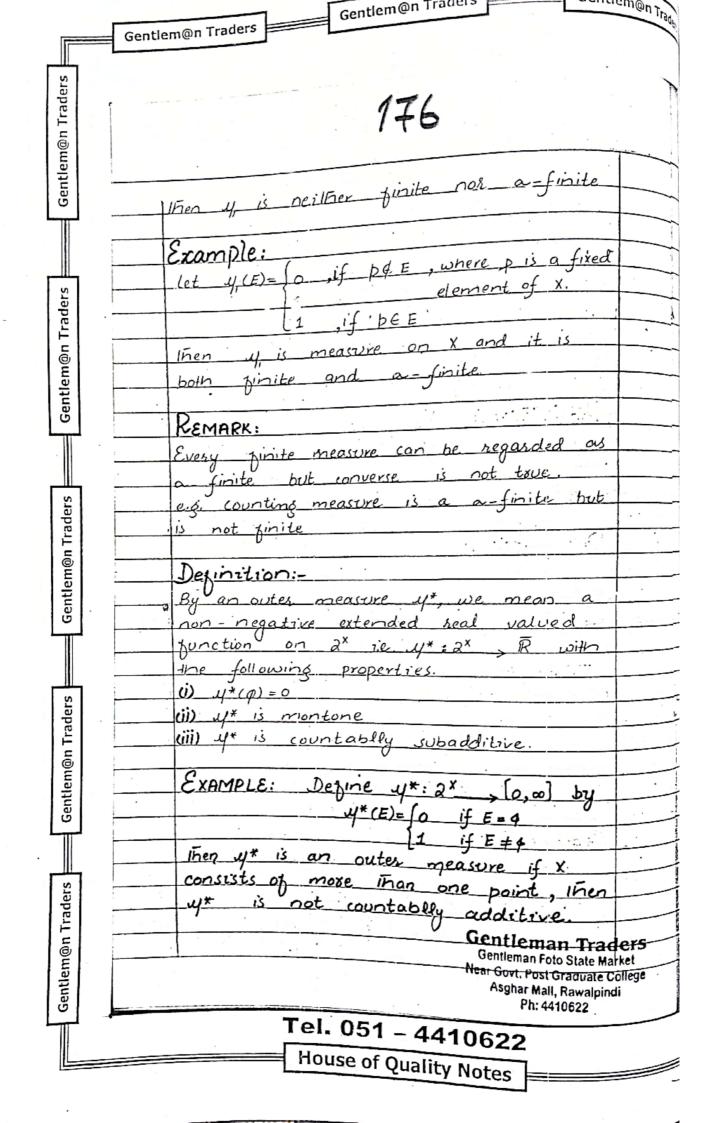


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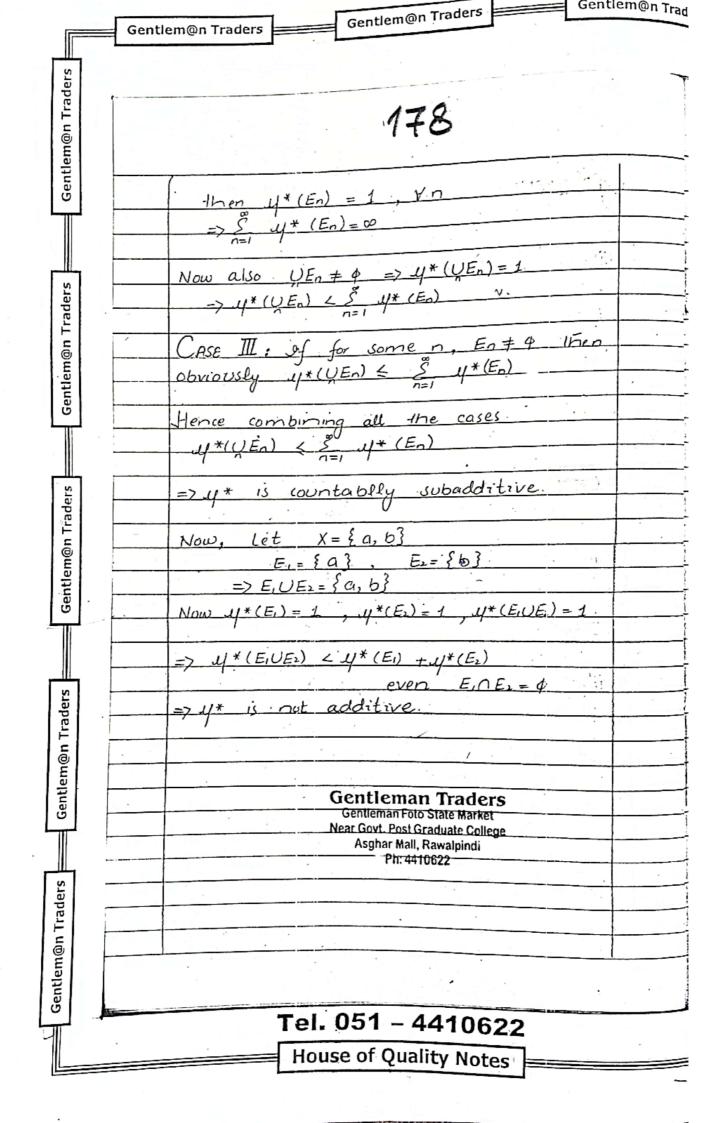


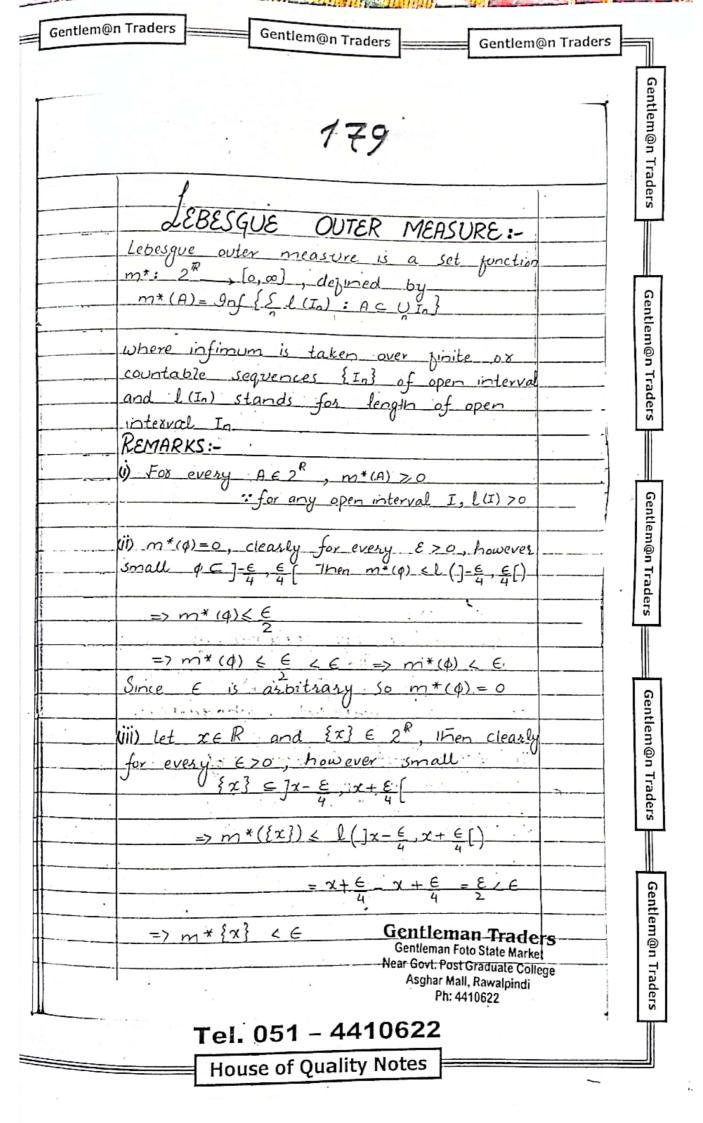


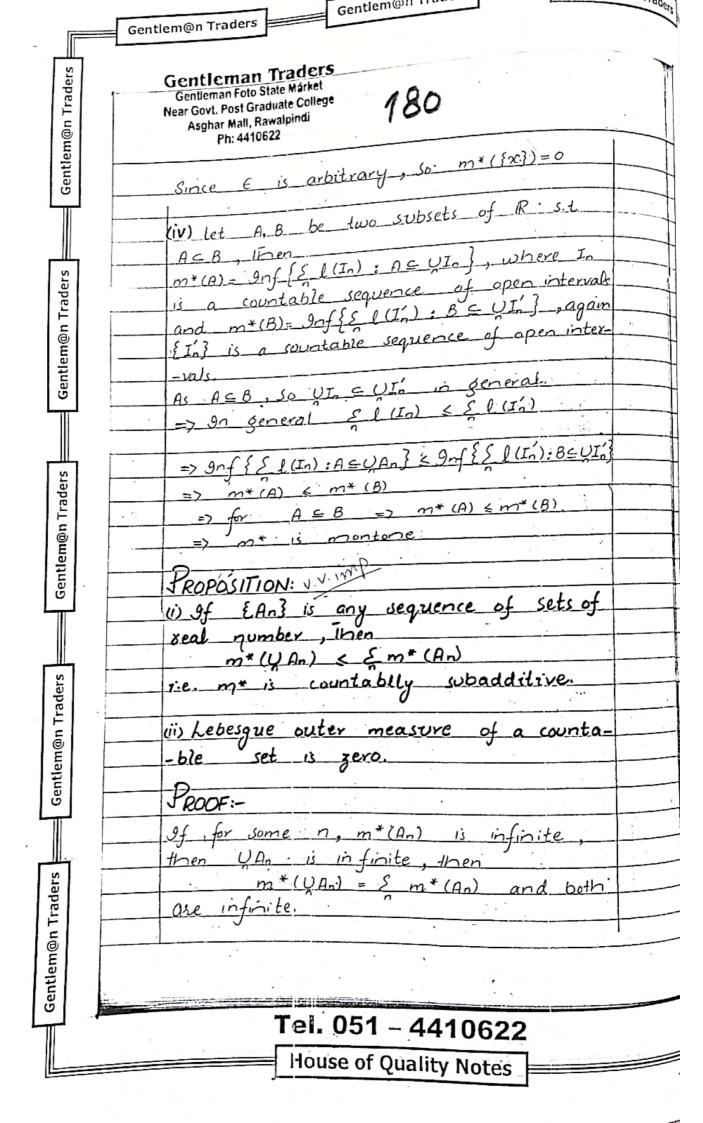


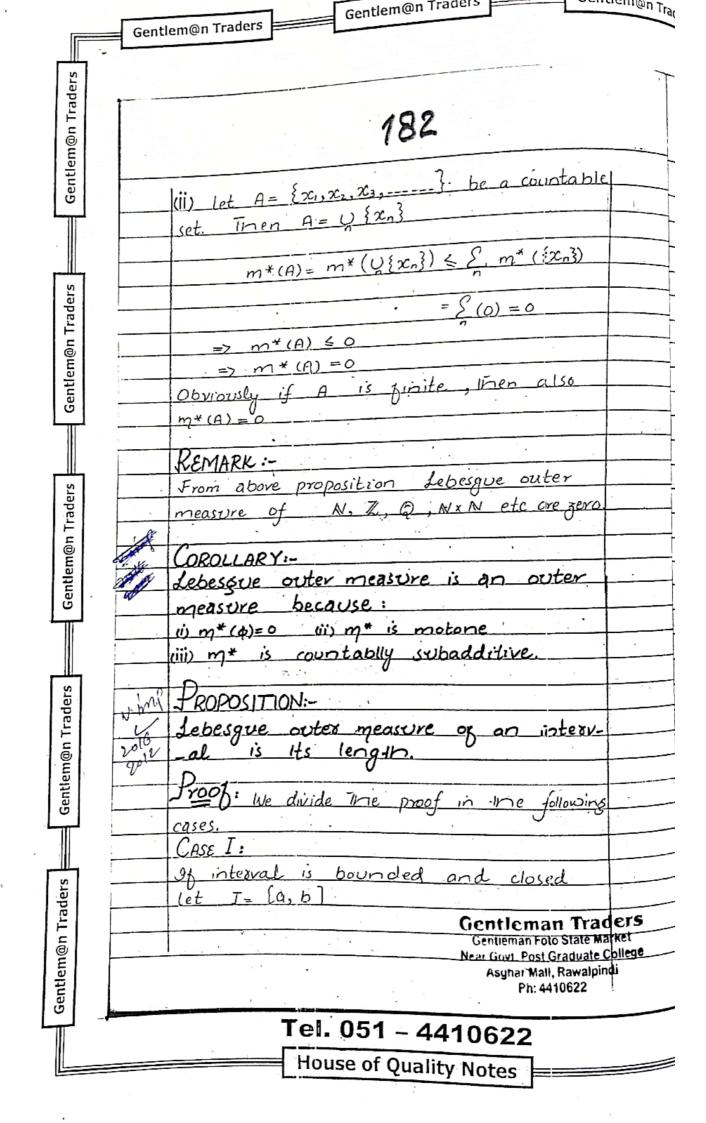


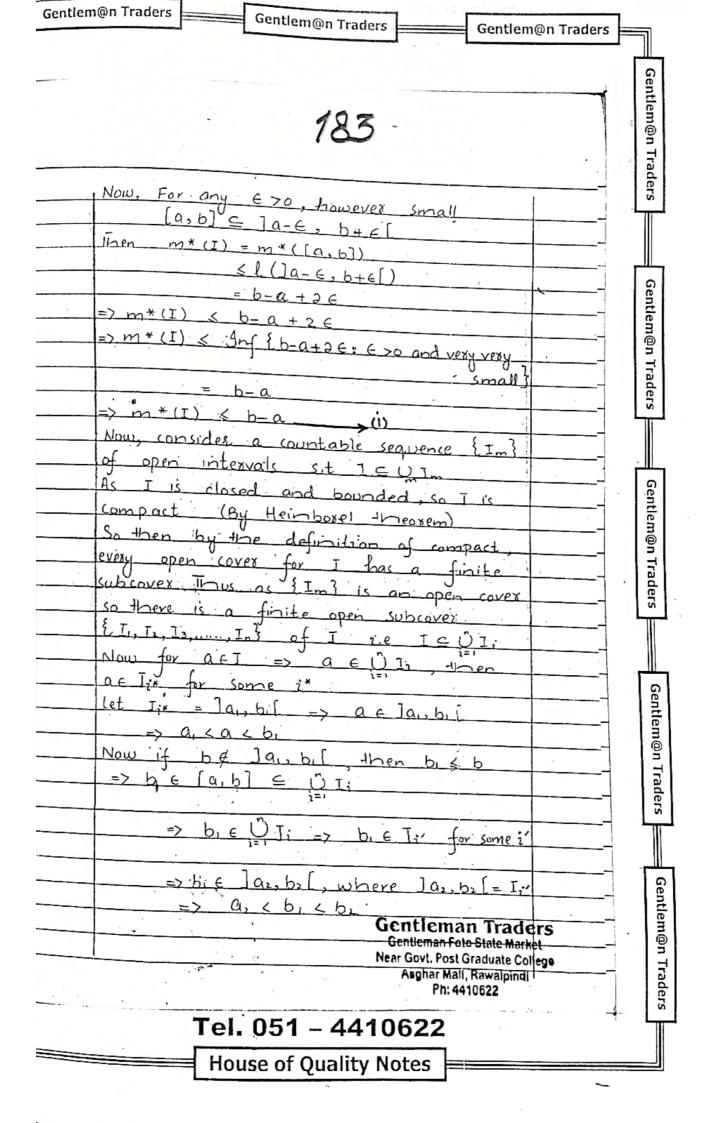
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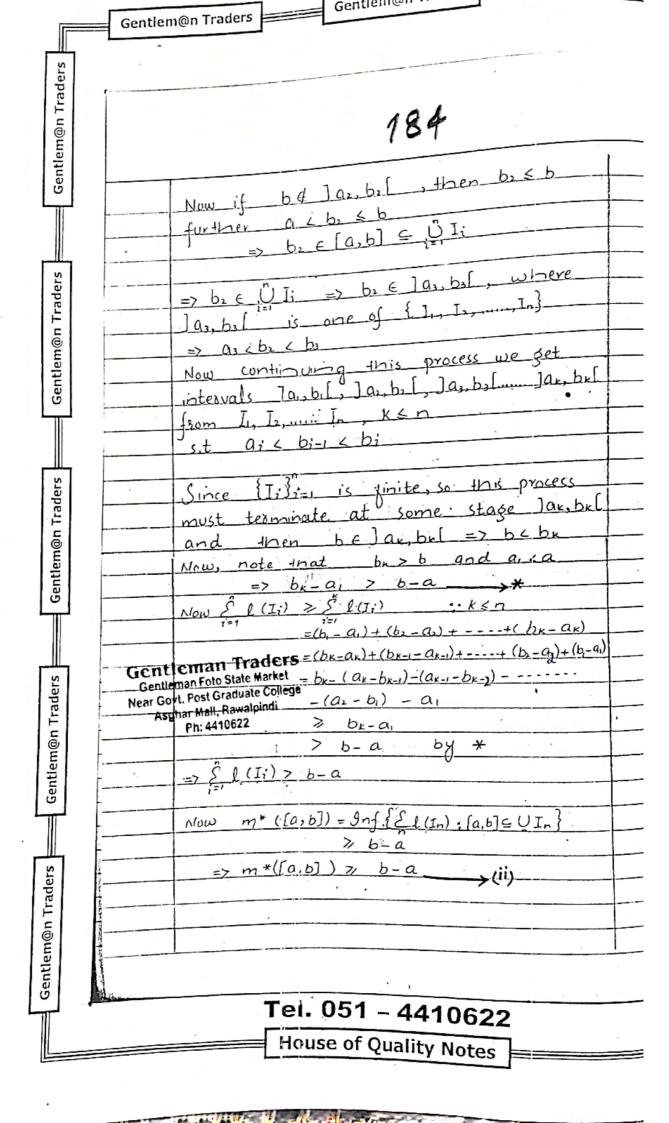








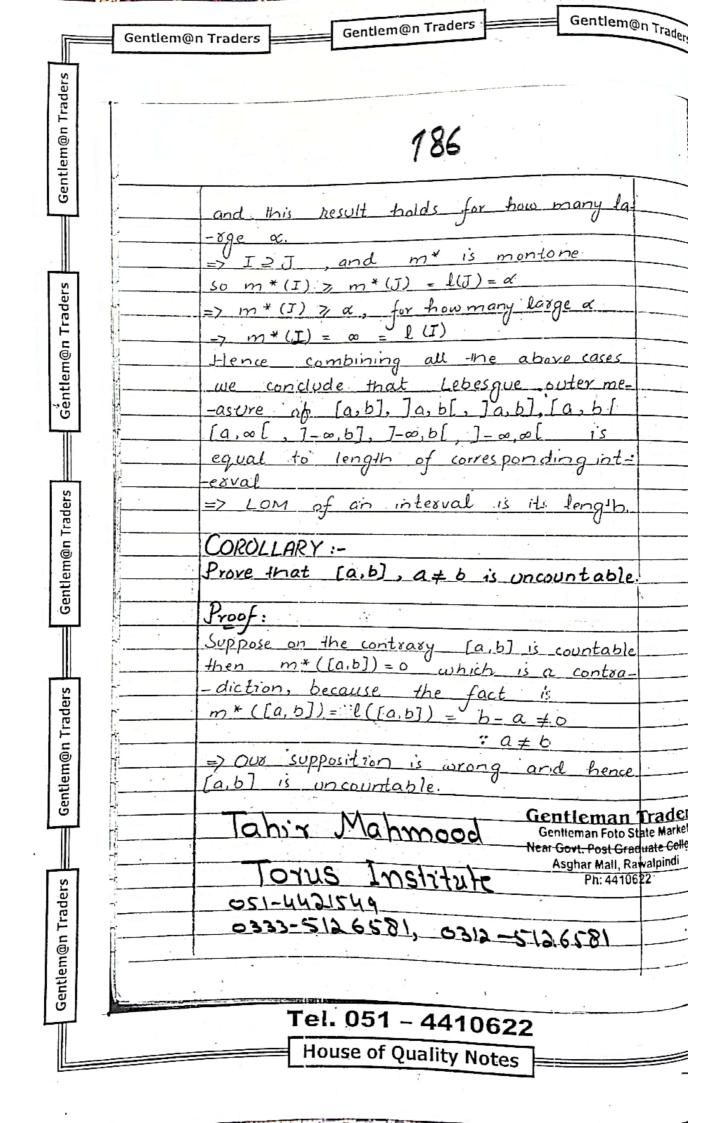


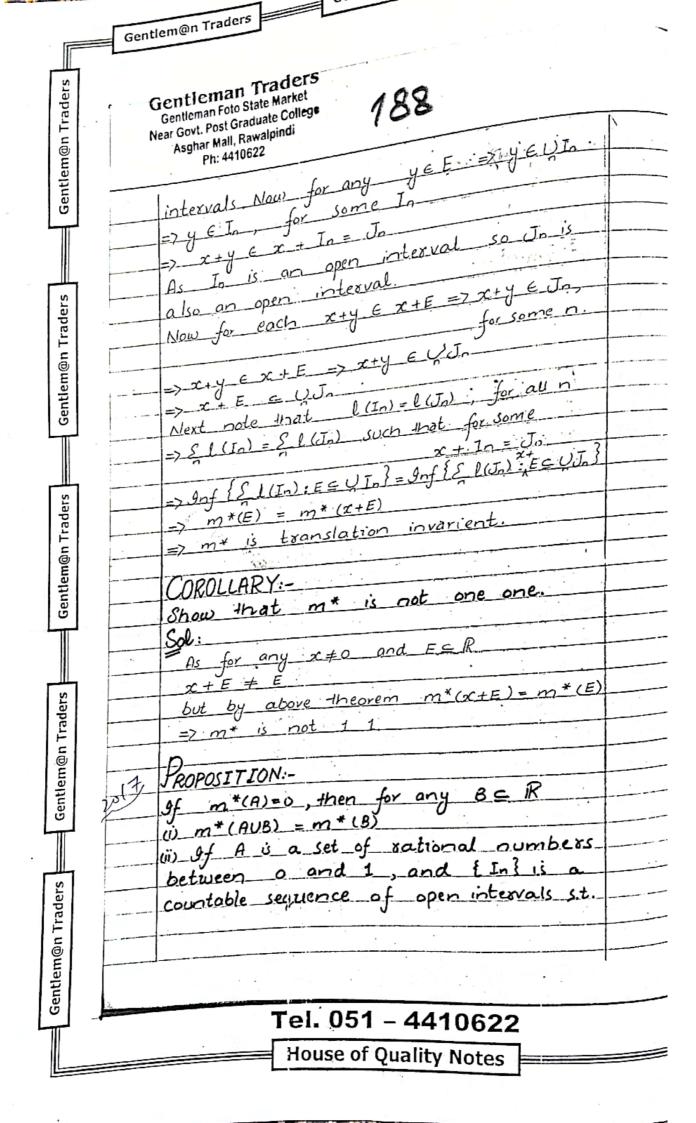


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| real | number | / (| nere i | | closed in | |
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| 000 | 777 | | | A | sghar Mall, Ra Ph: 44106 | walpindi |
| | m*(I) | = $L(1)$ | | Near G | lleman Foto S ovt. Post Gra | duate College |
| from | (ii) and | d (iii) | | Gen | tleman | Traders |
| ->- | m * (I) | < l(I) | > | ii <i>)</i> | | : 1 . |
| - | | | (I) = | | • | |
| 1 | => m* (| T) { m | | | | |
| | also I c | | -> (0) | | | \$ - |
| => l | (I) < m* | (I) | <u>rii\</u> | | by (i) | |
| => | m*(J) \< | * (T) | on # / 7) | - | h | |
| iso | m* is | monton | 2 | ••• | | |
| Now | $\mathcal{J}\subseteq\mathcal{I}$ | 3 / 1 / 1 / 1 / 1 / 1 / 1 / 1 / 1 / 1 / | `& | | | |
| So. | $l(I) \leq n$ | 7 + (5) | () | | | |
| Since | $\begin{array}{c} \in & is \\ l(I) & \leq m \\ , & J \subseteq I \end{array}$ | asbitsa | | | | , |
| • | | | no Pased | intervi | of Chy Ca | (p I) |
| => L(| <u>-€ < l (</u> T) - € < 1 | m * (J) | : m*1 | 1 | A. T | |
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| - | = | l([a,b |)) | | | |
| | ([a,b]) = | 0-a | | | | |
| m* | (a, b1) | la - | | | | |

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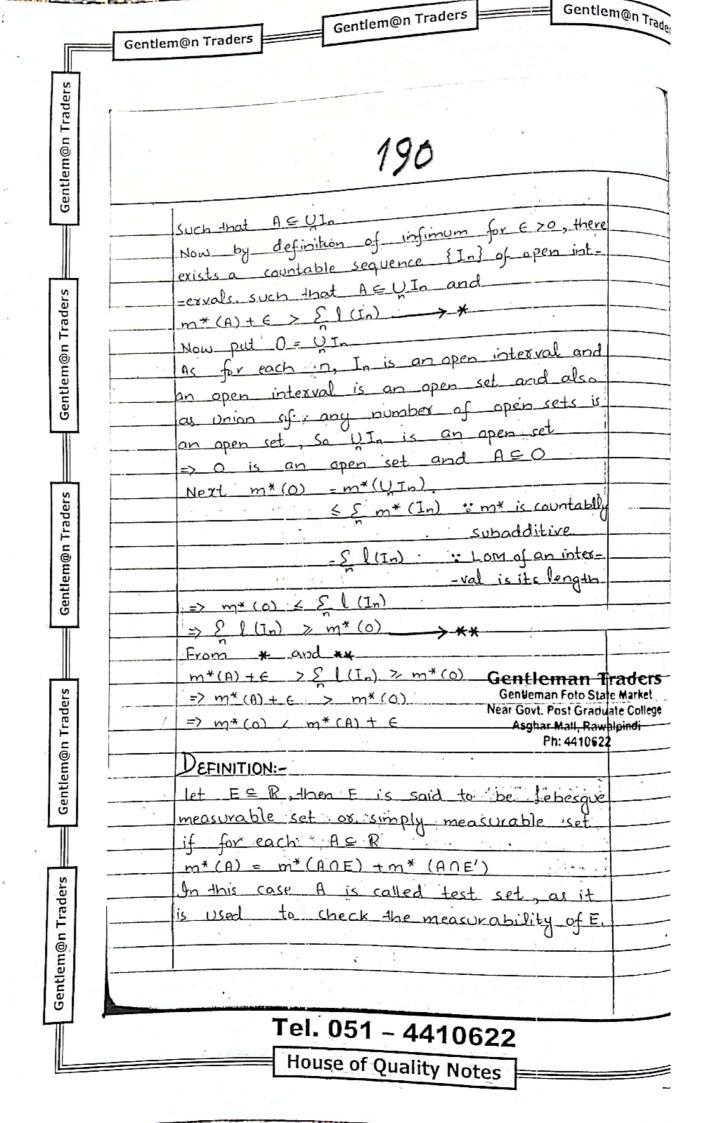


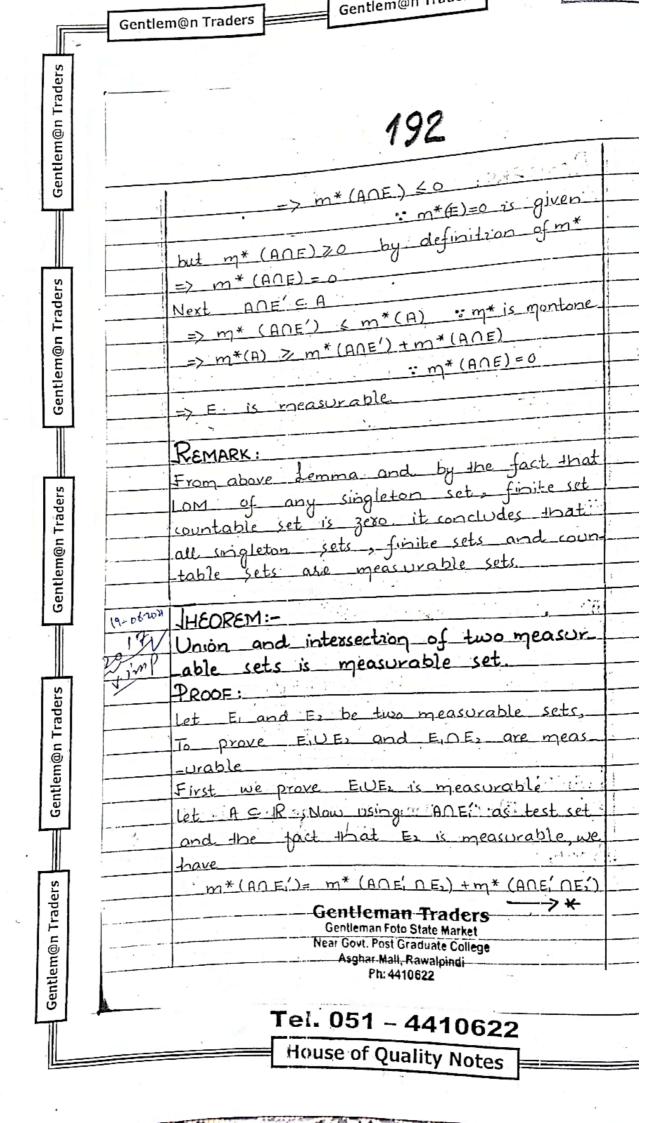


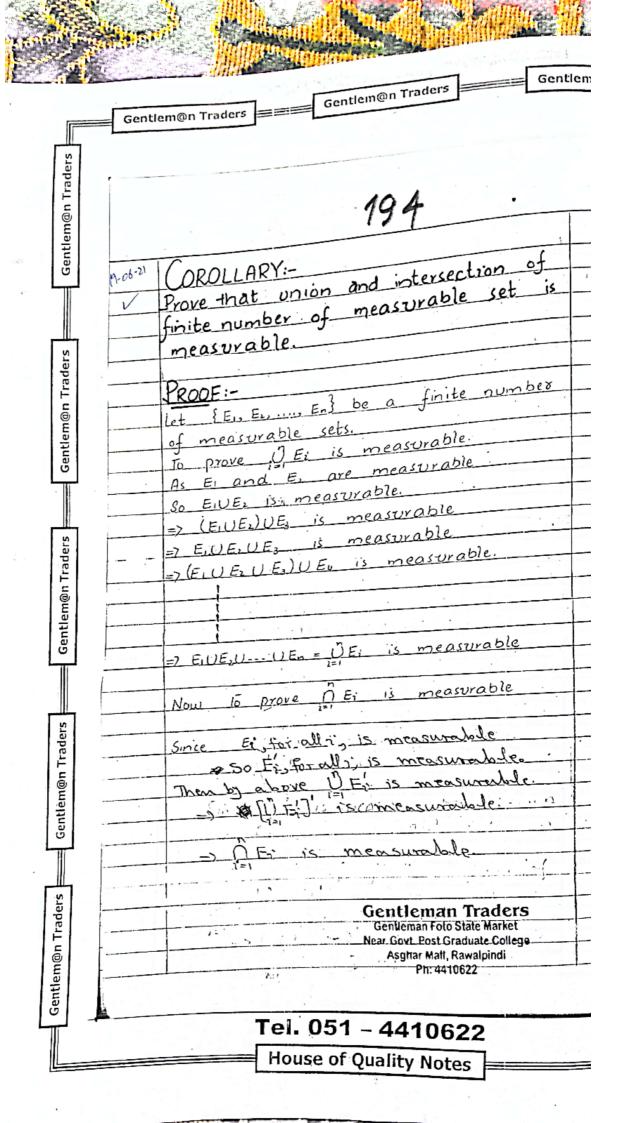
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| TE UIn then Soliti |
|---|
| A = UIn then Sl(In) > 1 |
| PROOF:- |
| DOC - |
| OAS m* is countably subadditive m*(AUB) < m*(O) + m*(O) |
| $m*(AUB) \leq m*(A) + m*(B)$ |
| = 0 + 100 * (0) |
| (100) < 100 + (0) |
| JE HUB Ond |
| So m* (B) < m* (AUB). |
| From * and ** |
| m*(AUB) = m*(B). |
| - HI (B). |
| iii) As $\{T_n\}$ |
| intervals such that account |
| intervals such that ACUIn and |
| DOPIN NOTAY, (a) |
| |
| |
| =7 m (10,11) < m * (UIn) < 5 m * (7) |
| m* is montone and countably |
| |
| $= 7 m*(]o,1[) \leq S m*(In) = S l(In)$ $= 7 1 \leq S l(I_n)$ |
| -> 1 < S l (In) |
| => S l (In) > 1 Gentleman Traders Gentleman Foto State Market |
| Near Govt. Post Graduate College |
| PROPOSITION: Asghar Mall, Rawalpindi Ph: 4410622 |
| . 4 1 1 |
| district to an open cot |
| D. 4 |
| 7800): |
| By dezinition m*(A)=9nf { S (In): Ac UIn} |
| where In is a countable sequence of open interval |
| -als |
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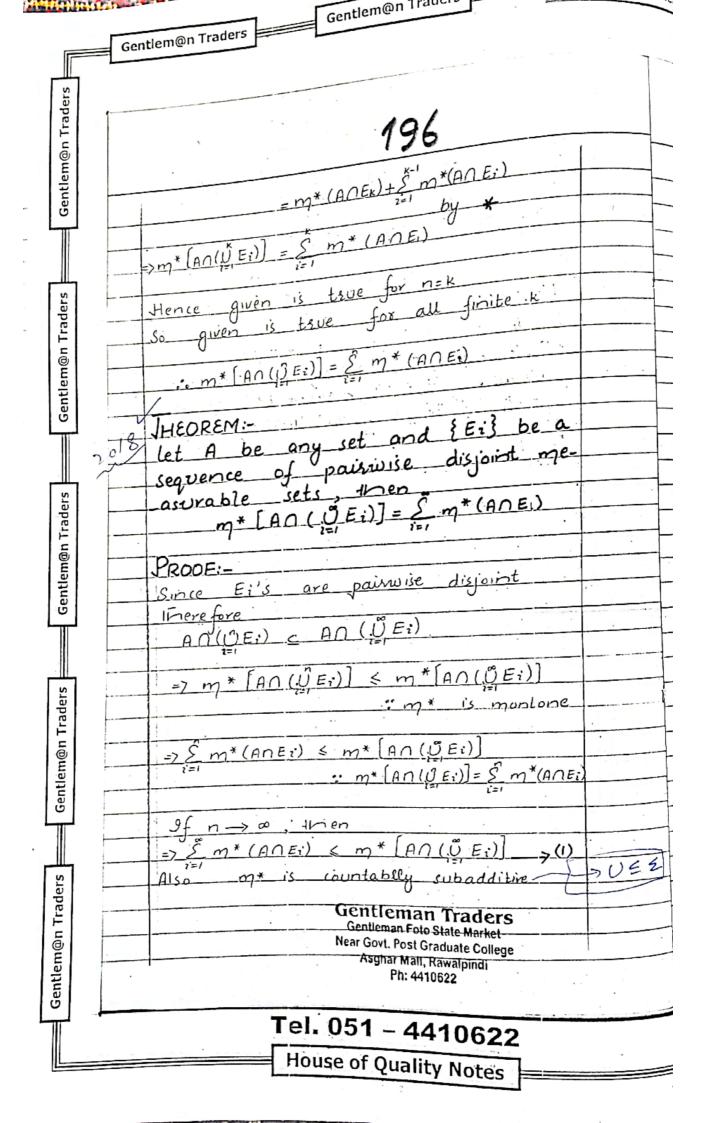




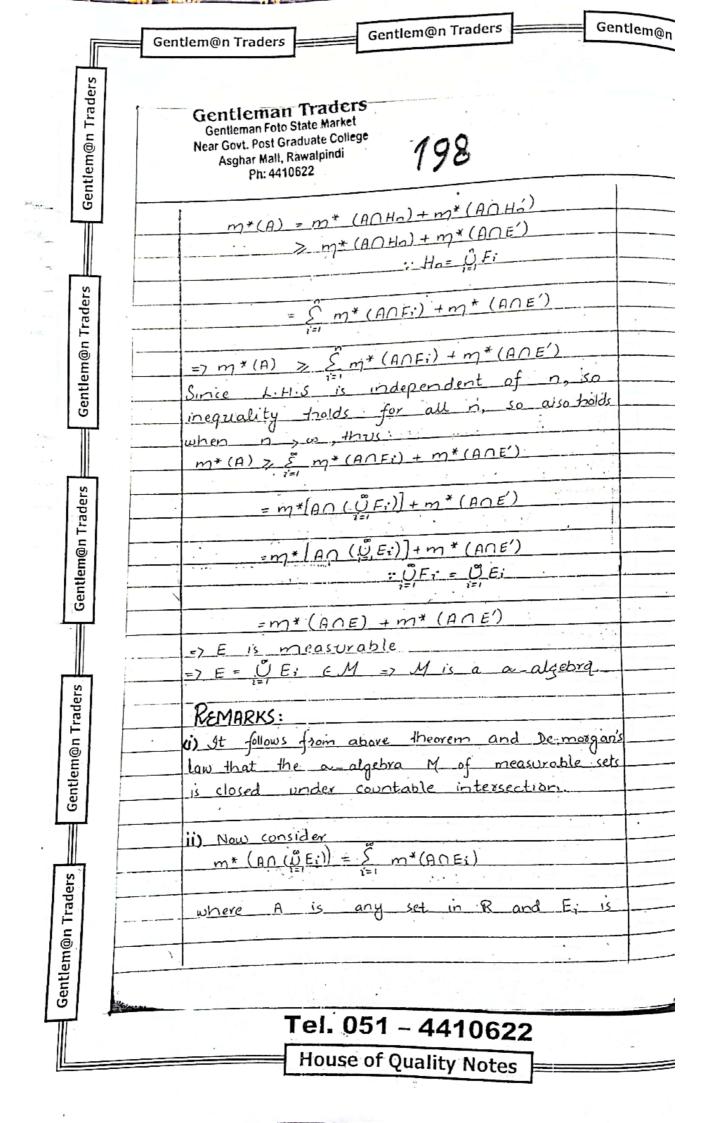


| | Tahir Mahmood | 1 |
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| | Torus Institute | |
| | 051-4421549 | |
| | 0333-5126581,0312-5126581 | |
| (2)21 | LEMMA:- | |
| 2 -08-2021 | LEMINA. | |
| | Let A be any set of real numbers and {E, E, E, E,, En} be a finite family of | |
| | Eti, Es, Es, min, Ens de a girito Ja sets then | |
| • | paiswise disjoint measurable sets, then | |
| | m* [An (DE;)] = & m* (AnE;) | |
| | Prof. | |
| | Proof: We use principal of mathmatical indu- | |
| | -ction to prove mis restilt | |
| | -ction to prove the for n=1. | |
| | Obviously given is true for n=1. Now suppose given is true for n=:k-1 | |
| | Tie soppose green | <u> </u> |
| | m* [An (UE;)] = 5 m* (AnE;) >* | |
| | 1 and will discount | |
| | So An(E;) DEx = An (E; DE) = ANEx | ı |
| | | |
| | also $A \cap (0, E_i) \cap E_k = A \cap [0, (E_i \cap E_k)]$. | ÷ |
| | | |
| | Now as Ex is measurable, so if we use | |
| | An (OE;) as test set, then we have | |
| | (2) | |
| | $m^*(A\cap(\overset{\circ}{U}E_i))=m^*(A\cap(\overset{\circ}{U}E_i)\cap E_k)$ + $m^*(A\cap(\overset{\circ}{U}E_i)\cap E_k)$ | |
| | m* (An(OE:) D. Ex) | |
| | () () () () () () () () () () | |
| | Gentleman Traders = m* (A \(\Omega\) + m* (A \(\Omega\) \(\Omega\) (A \(\Omega\) (A \(\Omega\) \(\Omega\) (A \(\Omega\) \(\Omega\) (A \(\Omega\) (A \(\Omega\) (A \(\Omega\) (A \(\Omega\) \(\Omega\) (A \(\Omega\ | |
| | Near Court Post Graduate College | |
| | Asghar Mall, Rawalpindi Ph: 4410622 | 1 |
| | File da 100s- | |

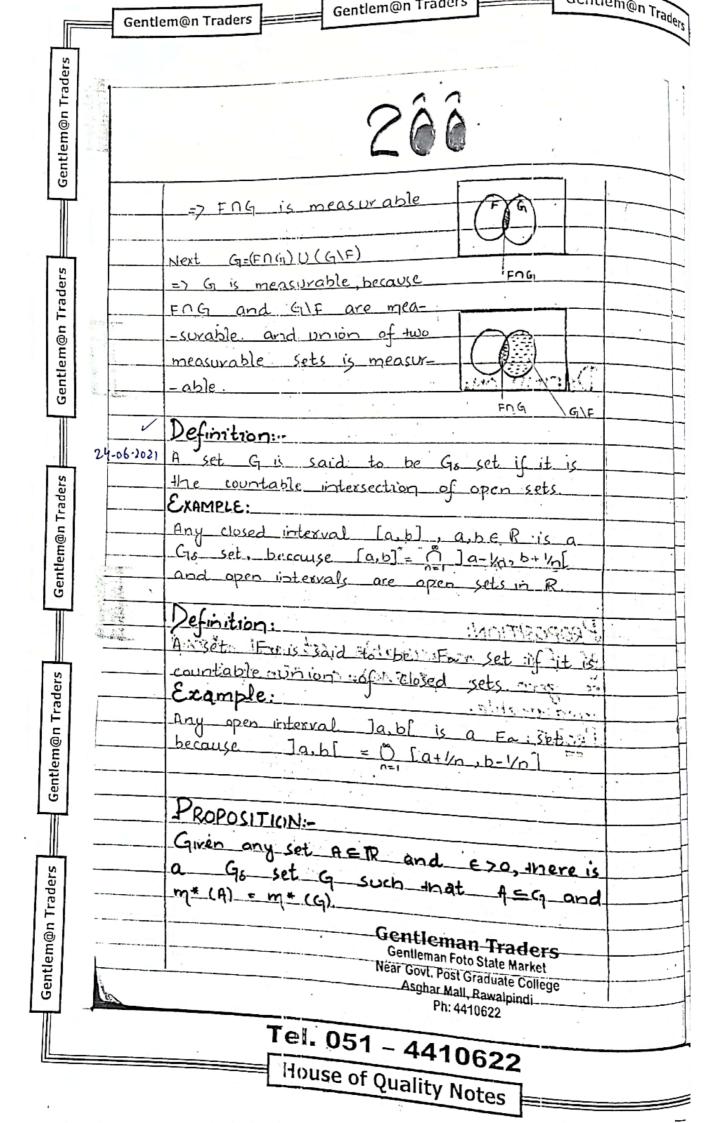
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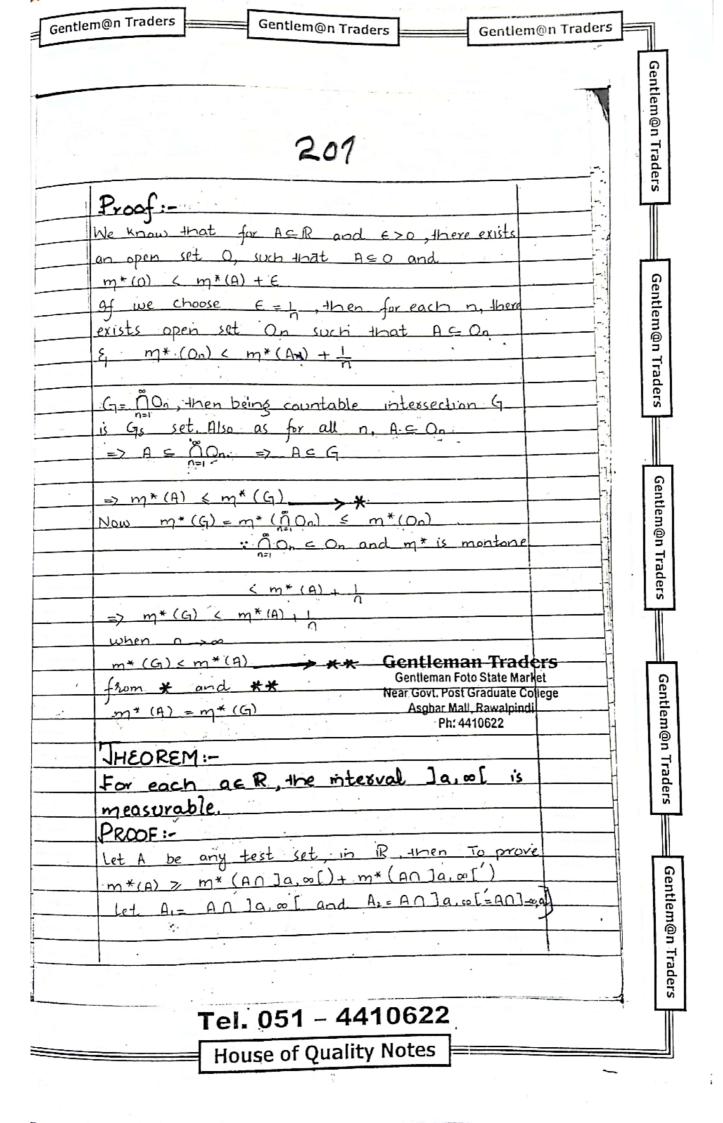


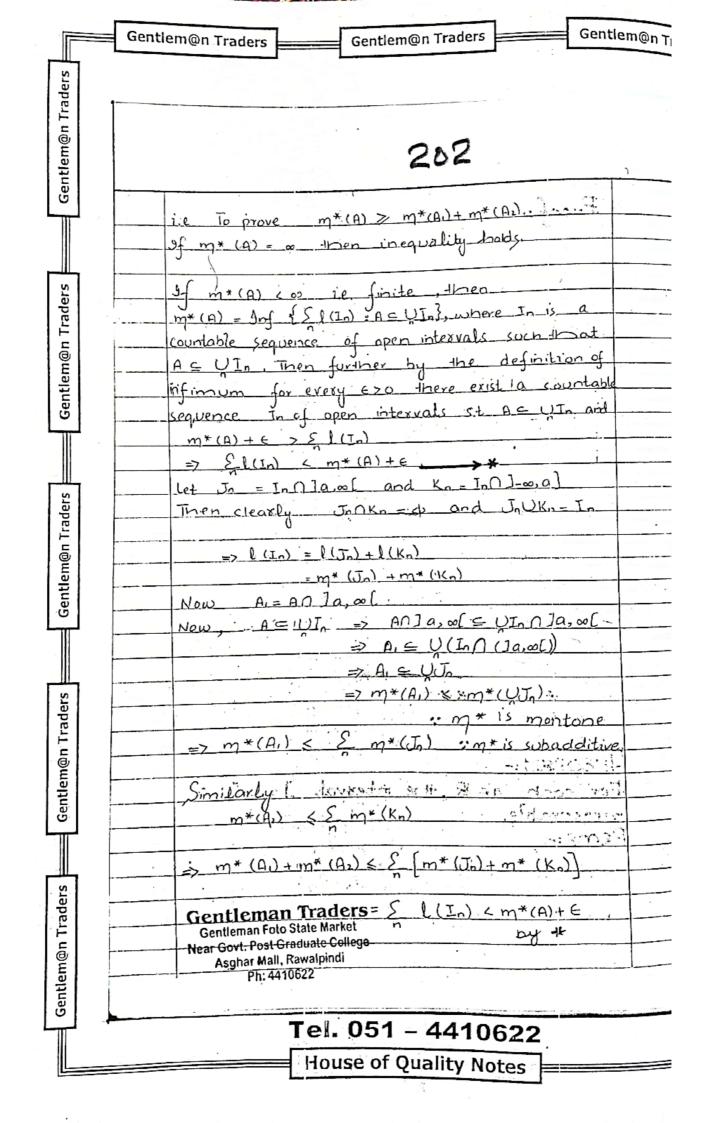
| | Gentleman Traders Gentleman Foto State Market |
|--|--|
| 197 | Near Govt. Post Graduate College Asghar Mall, Rawalpindi Ph: 4410622 |
| | 37 Pate 180 |
| Therefore, \$ m*(AnEi) > m*(Ani) Ei) | (2) |
|) m (H(121) | |
| Comparing (1) and (2) | |
| (omparing (1) and (2) = > 5 m* (AN (), E | <i>i))</i> |
| 1=1 | 7. |
| Licoped | |
| JHEOREM:- The class M of Lebesgu set is a-algebra | e measurable |
| cet is a - alsebra. | |
| 3 | |
| PROOF:- | |
| We know that union of two set is a measurable and | alco comple- |
| · · · · · · · · · · · · · · · · · · · | et is preasu- |
| 17 Mic on alse | bra. |
| 11 let { E; } be a seave | nce of sets |
| M TO OXOVE UE; EM. | Let E= UEi |
| in all known th | eorem, Triere |
| of measurable sets such | inat UE:= UF: |
| of measurable sets Put the OF, then for | each n, Ho |
| 2-1 | |
| Next Hn= ÜF; C ÜF; = E | |
| =7 Hn = E => E' | C H' |
| $= 7 H_n \subseteq E = 1 L$ | very ACR. |
| | × |
| ·. ** | is montone |
| Now as Hn is measurable, so | |
| | |
| | |
| " And the second of the second | |



Pentiement maners



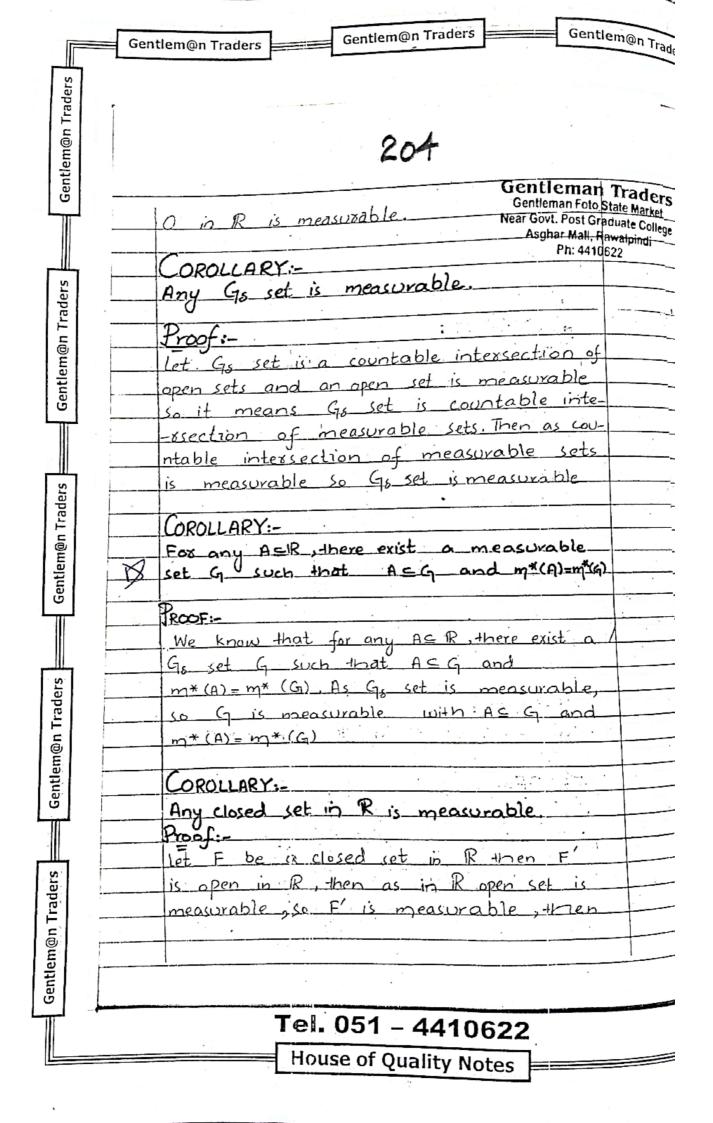




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| | Since E is arbitrary so | |
|-------------|--|--------------|
| | $m^*(A_1) + m^*(A_2) \leq m^*(A)$ | |
| | => m* (A) > m* (A1) + m* (A2) | |
| | =)]a, o[is measurable. | |
| | 17 | |
| - | LEMMA: | |
| | Fox any a, b & R,] a, b[is measurable | |
| | , 55, 75, 75, 75, 75, 75, 75, 75, 75, 75 | |
| | Proof:- | * 1 TZ |
| | We know that Ja.of is measurable | |
| | => la, os[' =]-os, as is measurable, heca= | |
| 1 | use complement of a measurable set | 1 = = > |
| | is meastirable | |
| - | => for each ne N,]-0, b-1] is measurable | |
| | Then, as countable union of measur- | |
| | -able set is measurable | 1 |
| | so, $0 - 0$ $0 - 0$ $0 - 0$ = $0 - 0$, $0 = 0$ is measurable | |
| | [Naw | |
| | $]a,b[=]a,\infty[\cap]-\infty,b[$ Gentleman Gentleman Foto Sta | Traders |
| | =7 70 bl is measurable. Near Govt. Post Grad | uate College |
| | Asghar Mall, Raw | |
| | JHEOREM: | |
| | Any open set O in R is measurable. | |
| -11.7 | | |
| | Proof:- | 1 |
| | We know that any open sets can be expressed | |
| | as union of open intervals and an open | |
| 2-17 | interval is a measurable set and also | |
| error and a | union of any number of measurable | |
| | sets is measurable, so any open set | |
| - | | |
| | | |
| | | |

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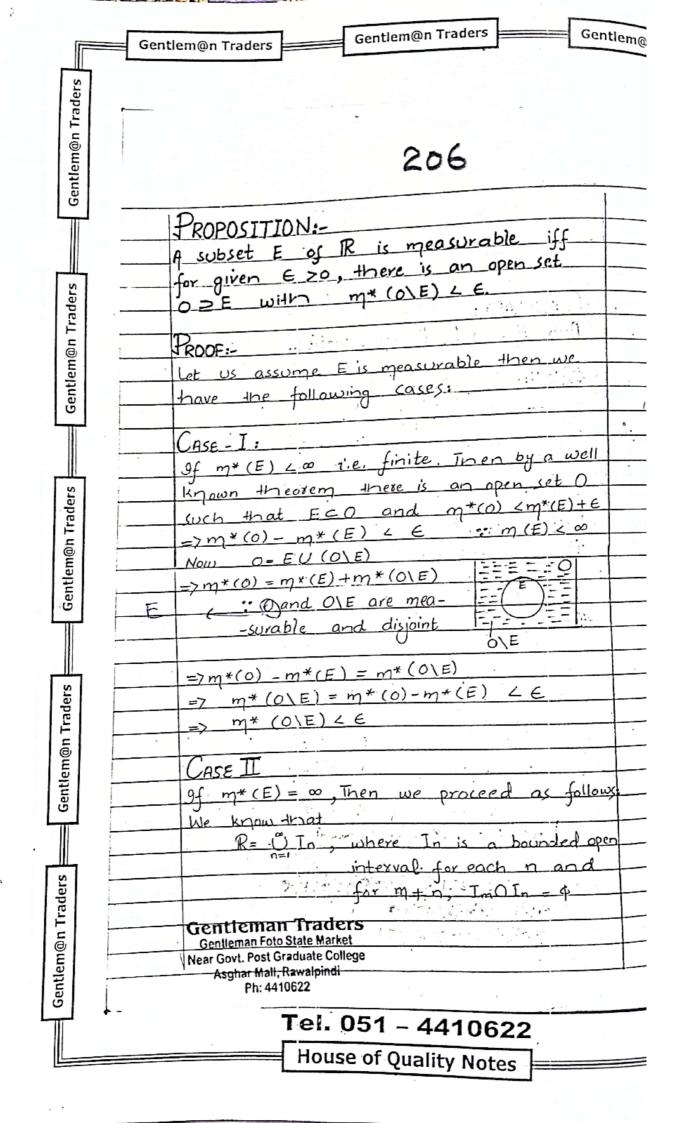


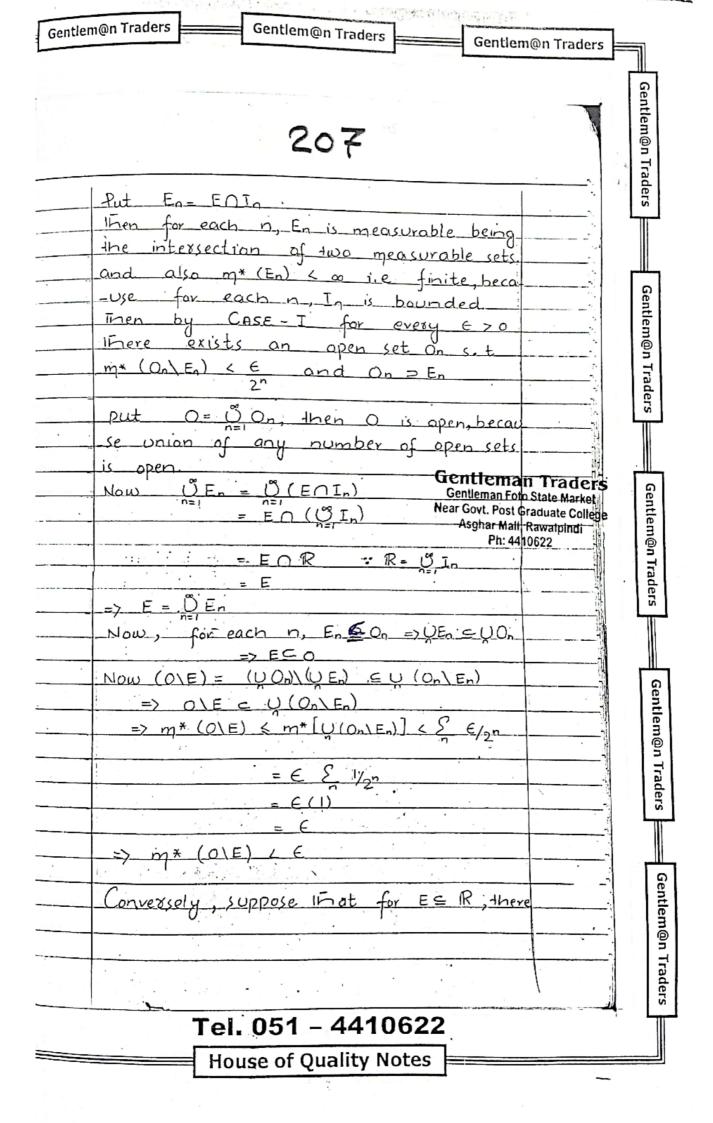
Gentlem@n Irauers

COROLLARY: measurable. countable union of closed countable union Fa set is measurable REMARKS: (i) The complement of Fa set is 98 set every open set is measurable but not true in general Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpindi Ph: 4410622

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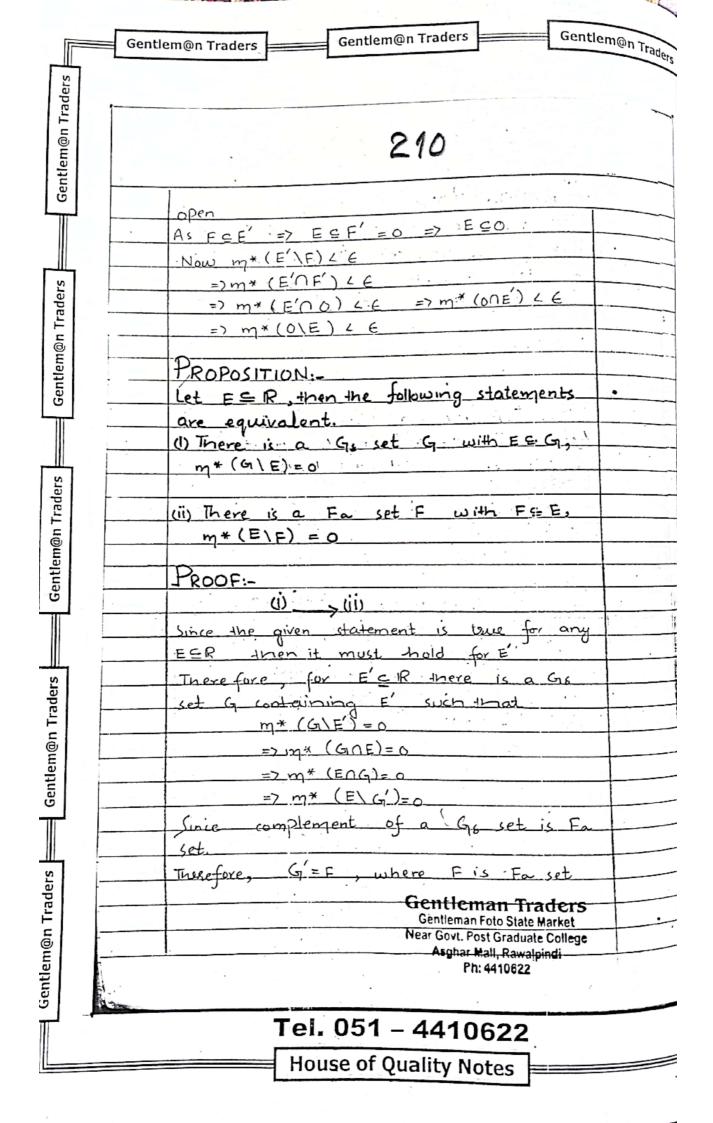


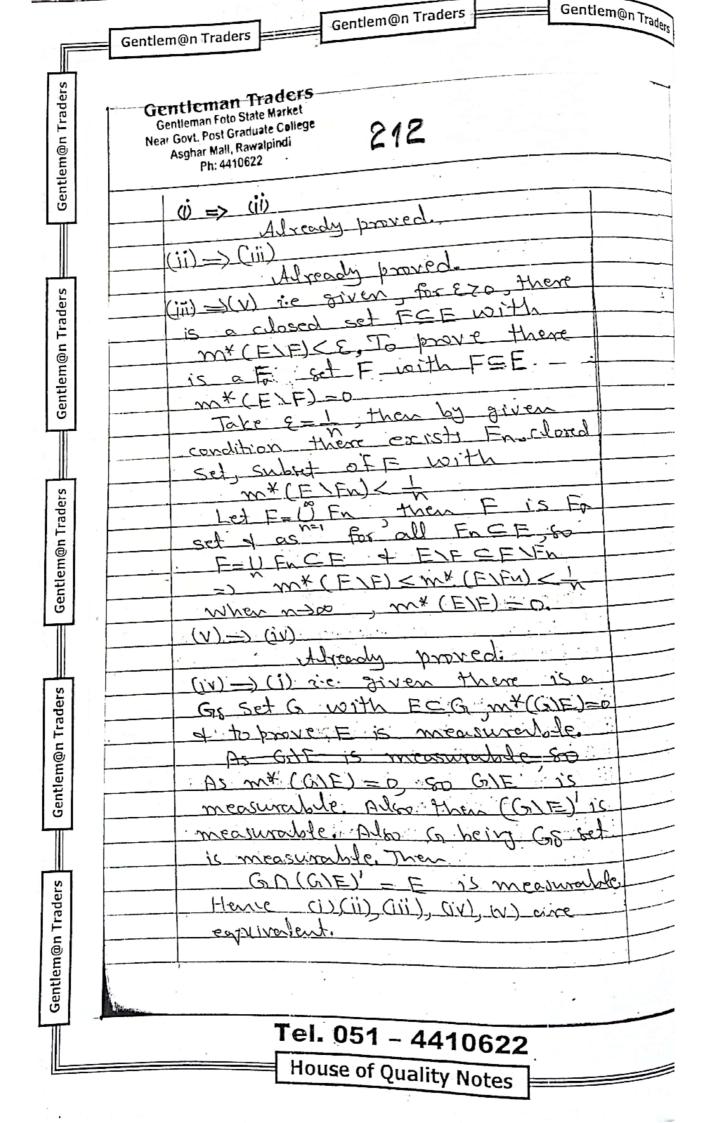
| | exists an open set 02 E with | |
|---|--|-----|
| | m* (OIE) CE for every E >0 | |
| | To prove E is measurable | |
| | Chanse 6 - 1 the ender suite | |
| | Choose E= 1, then by given condi- tion, there exists an open set On | |
| | Chon, we leve exists an open set On | |
| | Sate On = E and m* (On E) 21 | |
| | for all n | |
| | | |
| | Put G= non, the G is measurable, | |
| | being the countable intexsection of | |
| | measurable sets | · |
| , | | _ |
| | Further as 5.50 (l'open set is measurable). | |
| | Further as E = On, for all n, so | |
| | E C QO, => F C Q | : |
| | Neut | , |
| | Next as G= non => G= on, for all n | |
| | => G/E = On/E | |
| | | |
| | => m * (G/E) < m * (On/E) < 1 | |
| | · n | |
| | -> m = (G/E) < 1 , for all 10 | |
| | 7) for all is | |
| | $\Rightarrow m*(G\backslash E)=0$ | |
| | | |
| | => G\E | , . |
| | 4s E = CAO (GLE) | |
| | => E (C) | |
| | => E is measurable. | |
| | | |
| | Gentleman Traders Gentleman Foto State and Gen | |
| | Gentleman Foto State Market | |
| | | |
| | Asghar Mall, Rawalpindi Ph: 4410622 | • |
| | 410022 | , |

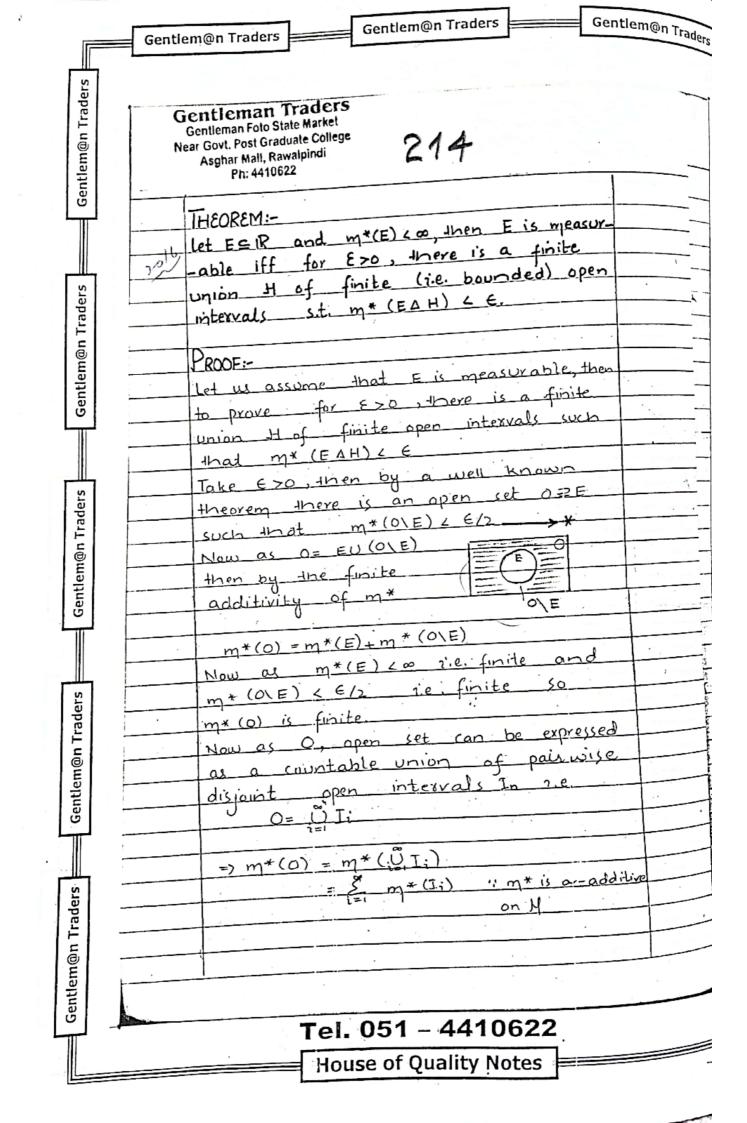
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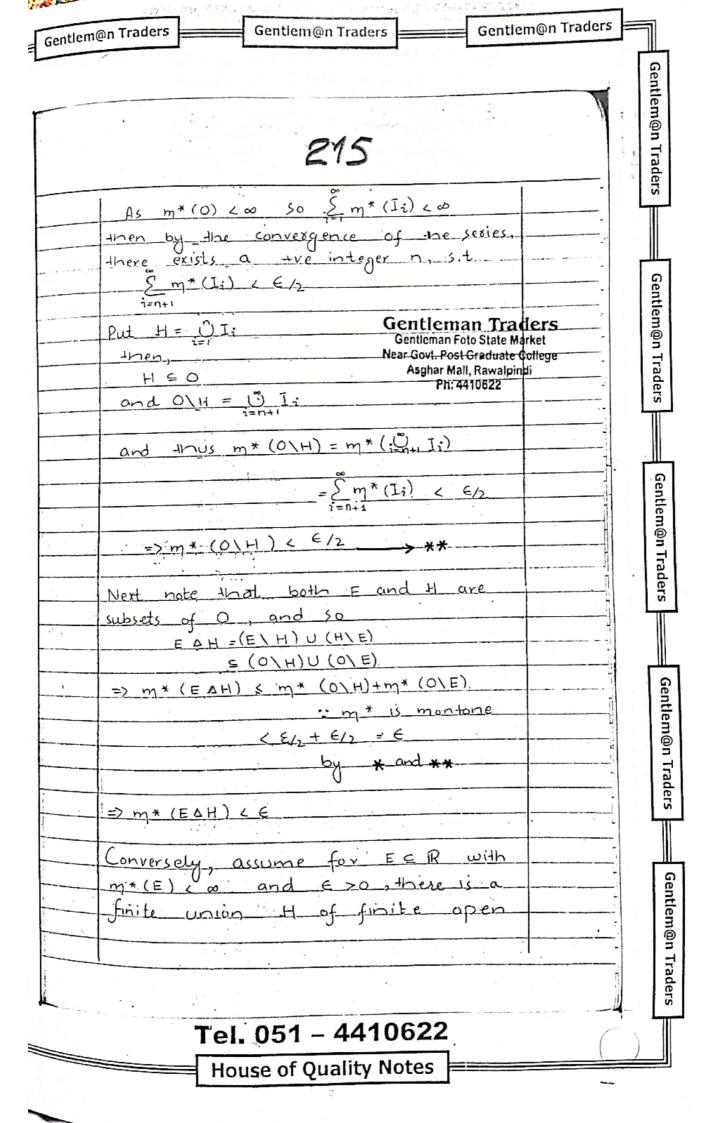
| PROPOSITION: | ~. |
|--|--|
| For a subset E of R and given Examples an open set 025 | |
| there is an analyticand given exa | `. |
| there is an open set OBE and mx (OLE) | - 1 |
| | |
| and m* (E/F) < E | ٦. |
| PROOF:- | ``. • . |
| | -:·. |
| et us assume there is an open set 0≥ E and | •••••••••••••••••••••••••••••••••••••• |
| | |
| 7/010 | _ إ |
| | , |
| an open set 02 E' s.t m* (OLE') < E. | _ |
| | _ |
| Then as offis open, so of the Filis | |
| closed Next a = " | |
| | _ |
| -> 0'E E -> F E E | |
| Next: | 7 |
| () m * (() - : : : : : | -4 |
| Gentleman Foto State Control | |
| Near Govt Post Graduate College = m * (on E) = m * (En o) Asghar Mall, Rawalpindi | - |
| Asghar Mall, Rawalpineli = m * (end) Ph: 4410622 | |
| = m * (E/F) | |
| -/ m* (E/E) | |
| Conversel | |
| Conversely assume there is a closed set FEE such that m*(E/F) c E Since it bolds for every | |
| Since it 111 | _ |
| Since it bolds for every ECR, so in | _ |
| particular it holds for E ill for Exa | |
| there is a closed set FCF and m * (E'IF) < F | _ |
| m*(E'(F) LE and | |
| Put 0= F' 110 | |
| · Then as I | |
| , then as F is closed so F' is | |
| put 0= F', then as F is closed so F' is | _ |

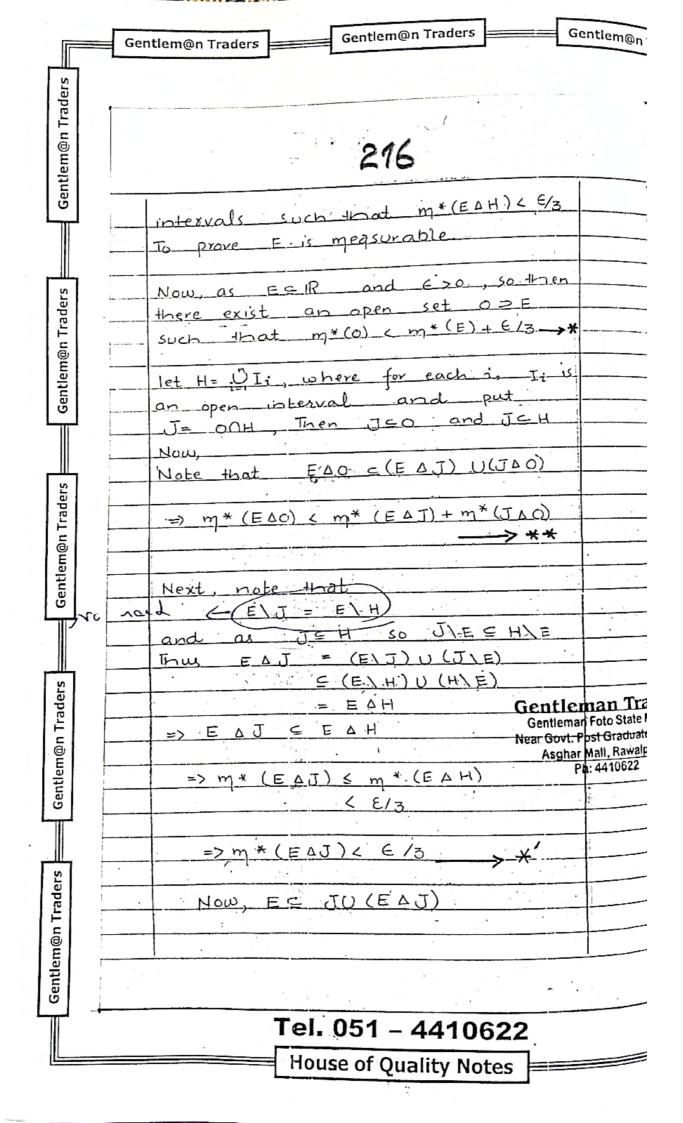
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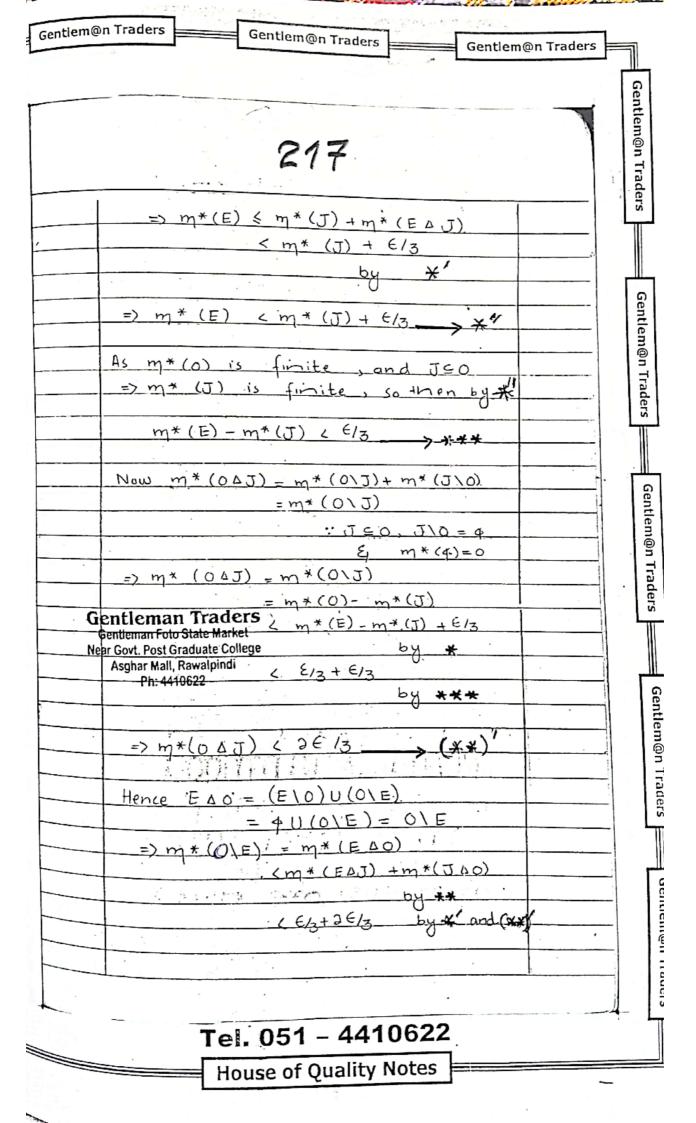


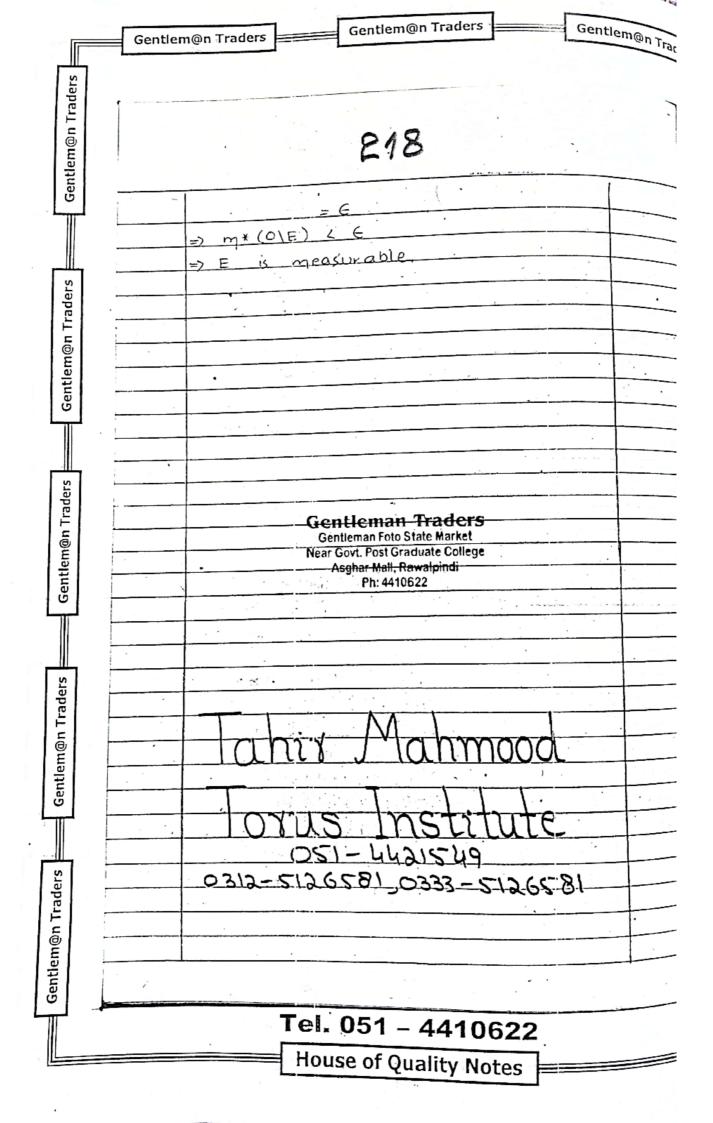






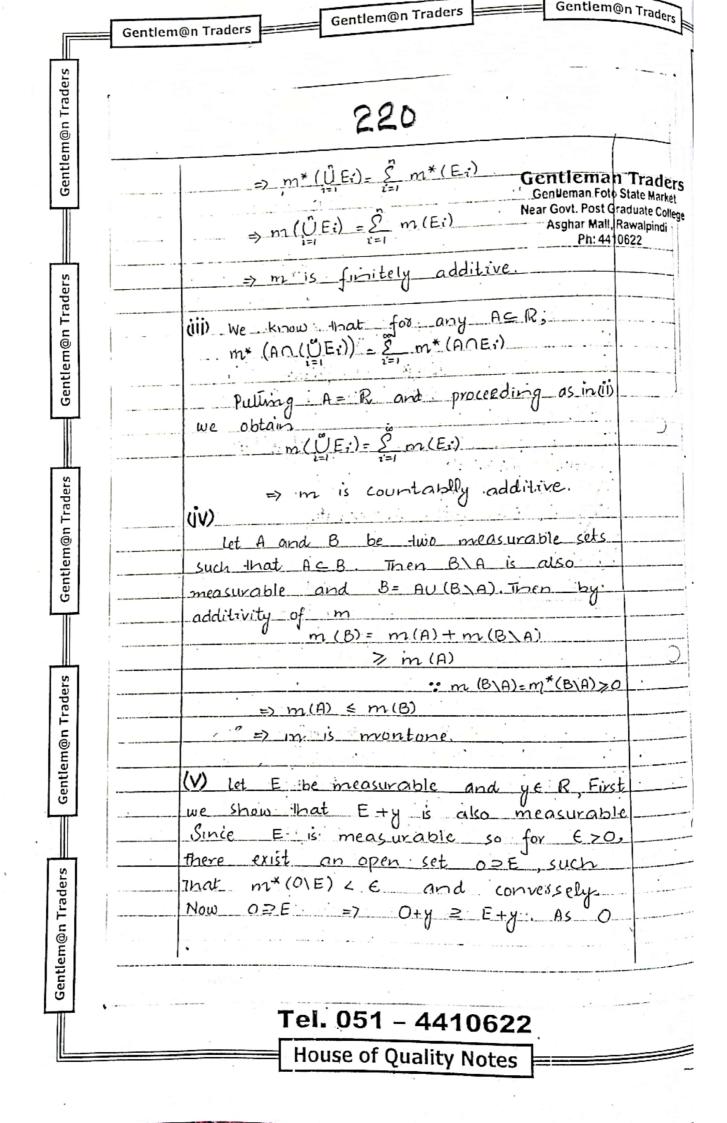


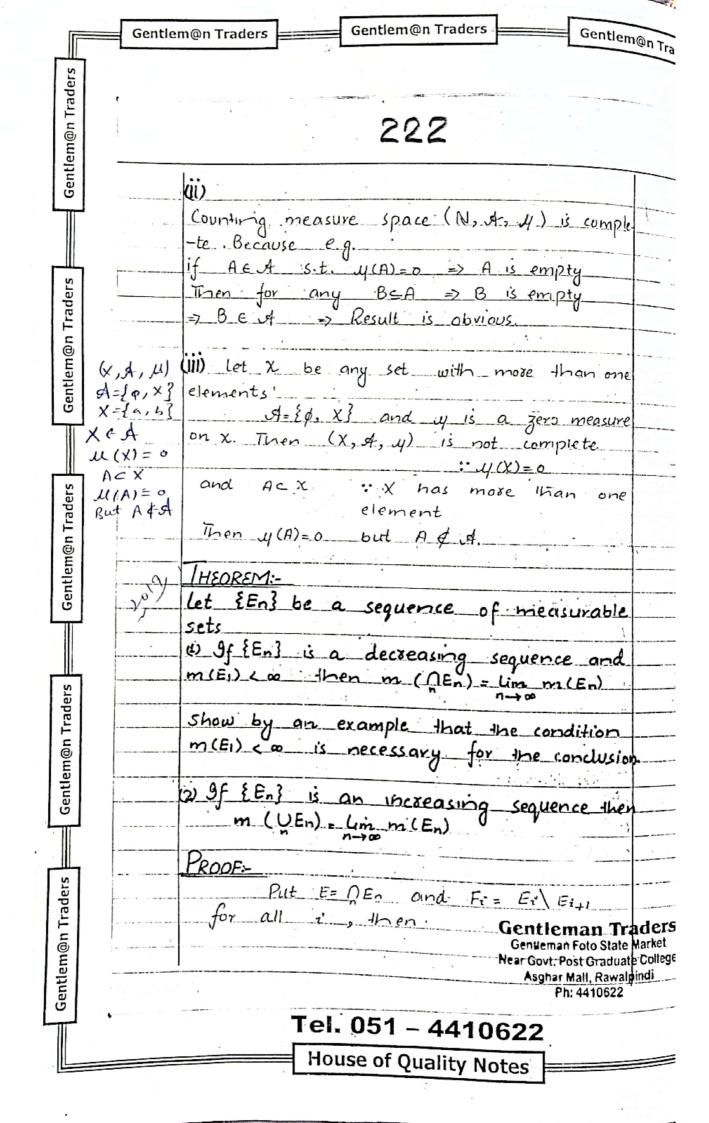




| Definition:- | 1 |
|--|-------------|
| let E be a measurable | |
| let E be a measurable set, then lebesgue me- -asure of E is defined to be lebesgue outer measure of E and is doubt | |
| measure of E and is denoted by m(E) | |
| Menoiced by m(E) | |
| HEOREM: | |
| Let {Ei} be a sequence of measurable sets | |
| Then measurable sets | |
| i) m is countably subadditive | |
| (ii) m is finitely additive provided {Ei} are | |
| pariurise disjoint. | |
| (ii) m is countably additive provided [Ei] are | |
| pauluise disjoint | |
| (iv) m is montone. | |
| (v) m is translation invariant. | |
| | |
| PROOF:- | |
| (1) As {Ei} is a sequence of measurable | |
| sets, so UE; is also measurable. Then | |
| $m(UEi) = m^*(UEi)$ | |
| ₹ £ m*(Ei) | |
| (110) (-/5 | |
| = Sm(Ei) => m(UE;) < Sm(E | 19 |
| => yp is countably cubadditive | |
| 1 | |
| (11) We know that for any ACR | |
| | |
| m* (AA (ÜEi)) = S m* (AAEi) | |
| i=i | |
| Put A = R, then | |
| (201/13E)) = S' m' (KILE3) | Dadors |
| m* (RO Gentleman Gentleman Foto Sta | ate market |
| Near Govt, Post Grad | uate Conege |
| Asghar Mall, Rav | 22 |
| | |

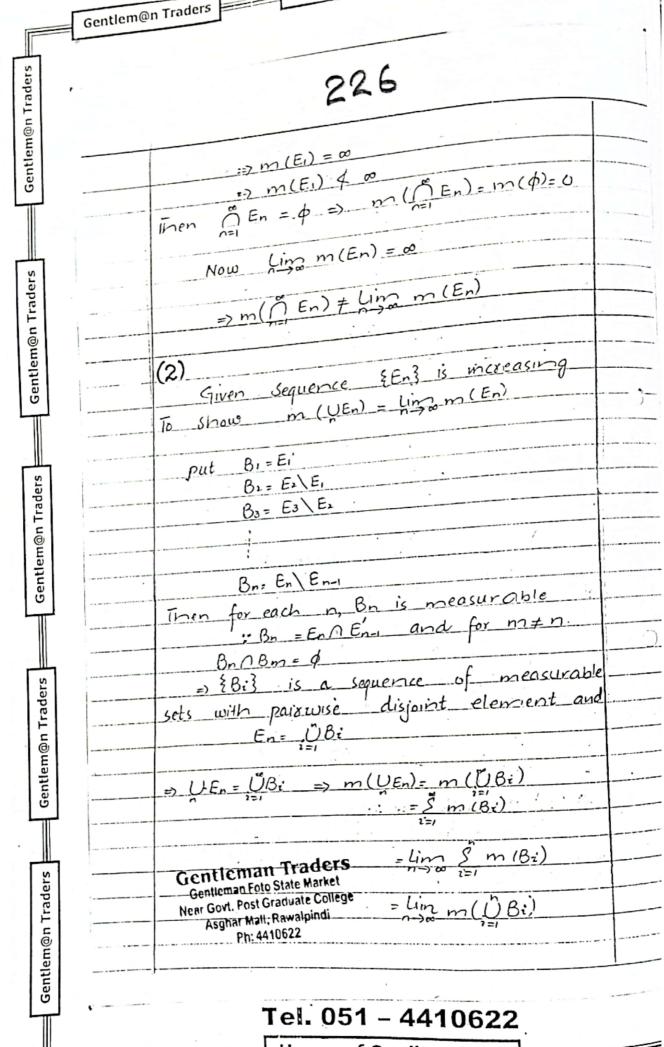
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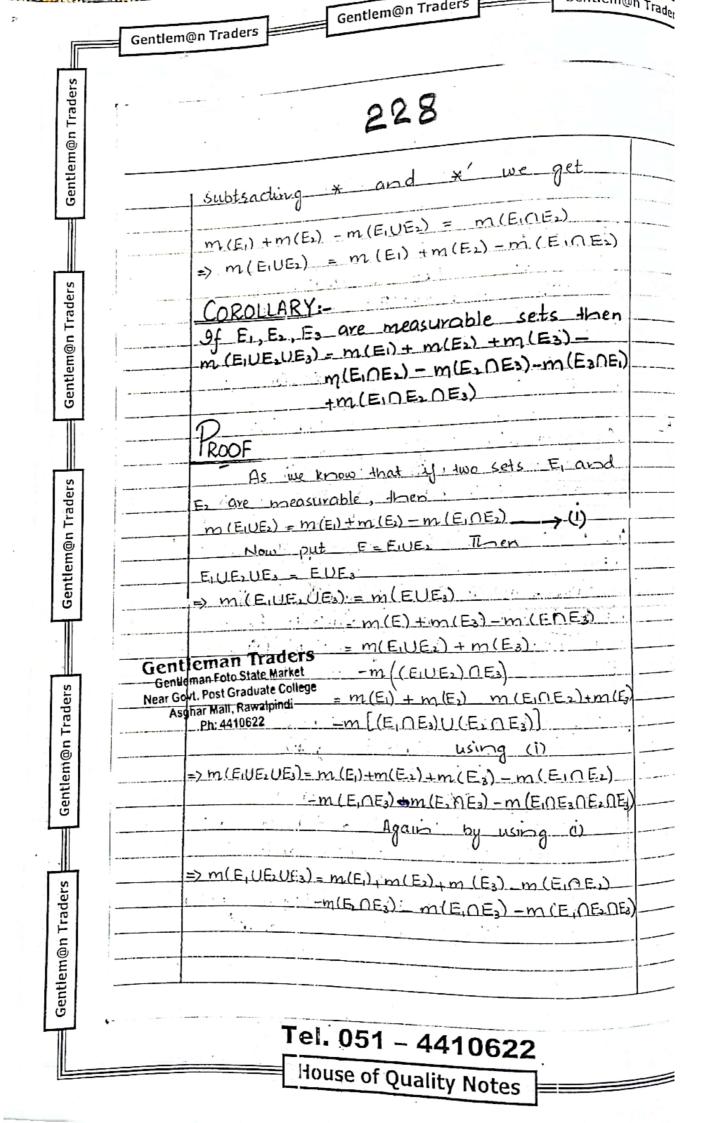
Here m(E) = m(]1, o[) = m*(]1, o[=0

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| | -> m(UE) 1: n-> m(En) | - |
|-----|--|------------------------------|
| | $\Rightarrow m(UEn) = \lim_{n \to \infty} m(En)$ | |
| | The second secon | |
| | JHEOREM:- | |
| | of E. E. are time | |
| | m(EIUE) = m(E)+m(E) - m(EIDE) | |
| | | |
| | PROOF: | |
| | Since IE is meaning | |
| | A = R Since El is measurable, so for any set | - |
| - | m*(A) = m* (A) + m* (A) (A) | |
| • 1 | In particular for Erc R | |
| | m*(E2) = m*(E2NE1) + m*(E2NE1) | |
| | => m* (E2) = m*(E10E2) + m*(E10E2) -> (i) | |
| | (: intersection is commutative) | |
| • | As Ez is also measurable, so in the same | |
| | way | |
| | m*(E) = m* (E, \cap E_1) + m* (E, \cap E'_2) ; (ii) | |
| | Since E1 and E2 are measurable so we | |
| | write m in place of m* in in and | |
| 1 | (ii) and then add we get | |
| | · · · · · · · · · · · · · · · · · · · | |
| L | $m(E_1)+m(E_2)=m(E_1\cap E_2)+m(E_1\cap E_2)+m(E_1\cap E_2)$ | |
| | +m (E(NE,) * | |
| | As | |
| } | (E,UE)= (EINE;) U (E2NE;) U (E1NE) + | |
| | Since EINEZ, EINE and EINE, all | |
| | are disjoint so we can write | |
| | | |
| | $m(E_iUE_i) = m(E_i \cap E_i) + m(E_i \cap E_i) + m(E_i \cap E_i)$ | |
| | Gentleman Traders -> * Gentleman Foto State Market | to the first one of the same |
| | Near Govt. Post Graduate College | |
| | Asghar Mall, Rawalpindi Ph: 4410622 | |
| 1. | | |

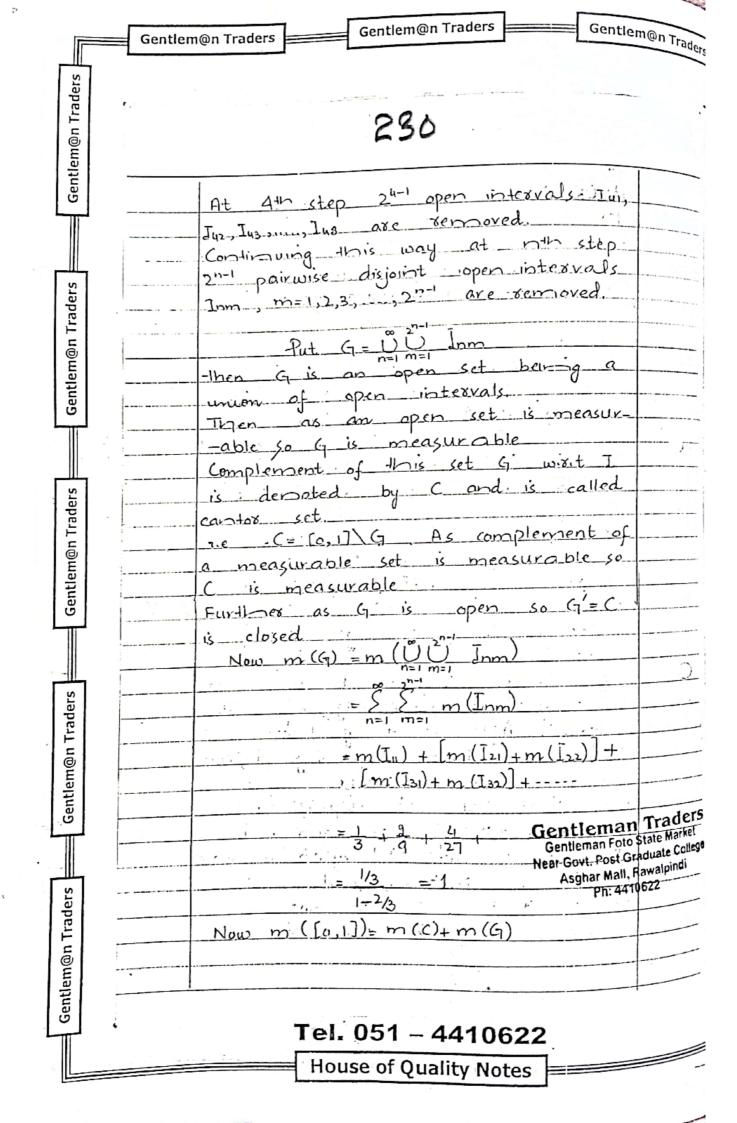
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| | A |
|-----|--|
| 114 | PROPOCITION |
| V/- | PROPOSITION:- |
| | has Lebecoup |
| | tras Lebesque measure zero. |
| | D DETO. |
| | TROOF:- |
| | The state of the s |
| | First we introduce the concept of |
| | cantoo set Let $I = [0,1]$ and $I_{11} = \frac{1}{3}, \frac{2}{3}$ |
| | 0.1 |
| . (| THE PER PORT OF THE PROPERTY O |
| | De the date |
| | T TE IMMANDING IT I ACL |
| | |
| - 1 | 1 |
| 1 | 33-4-1211 |
| | +/// : (m / a -) |
| | |
| | intervals we have eight closed open |
| | intervals. |
| | let In T T |
| - | third of these remaining eight closed intervals. After removing these |
| | intervals. After removing eight closed thirds we have removing these middle |
| | thirds we have remaining sixteen |
| | closed interior |
| | closed intervals |
| | Note that at 1st step 21-1 open |
| | At second cless 22-1 |
| | At second step 22-1 apen intervals |
| | At Hard the semoved |
| | Tra step 23-1 open intex |
| | At third step 23-1 open intervals 1.e. 131, I32, I33, I34 are removed. |
| | Gentla |
| | Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate |
| | OUVI DOOL OF THE MARKON |
| | Asghar Mall, Rawalpindi Ph: 4410622 |
| | Tel. 051 - 4410622 |

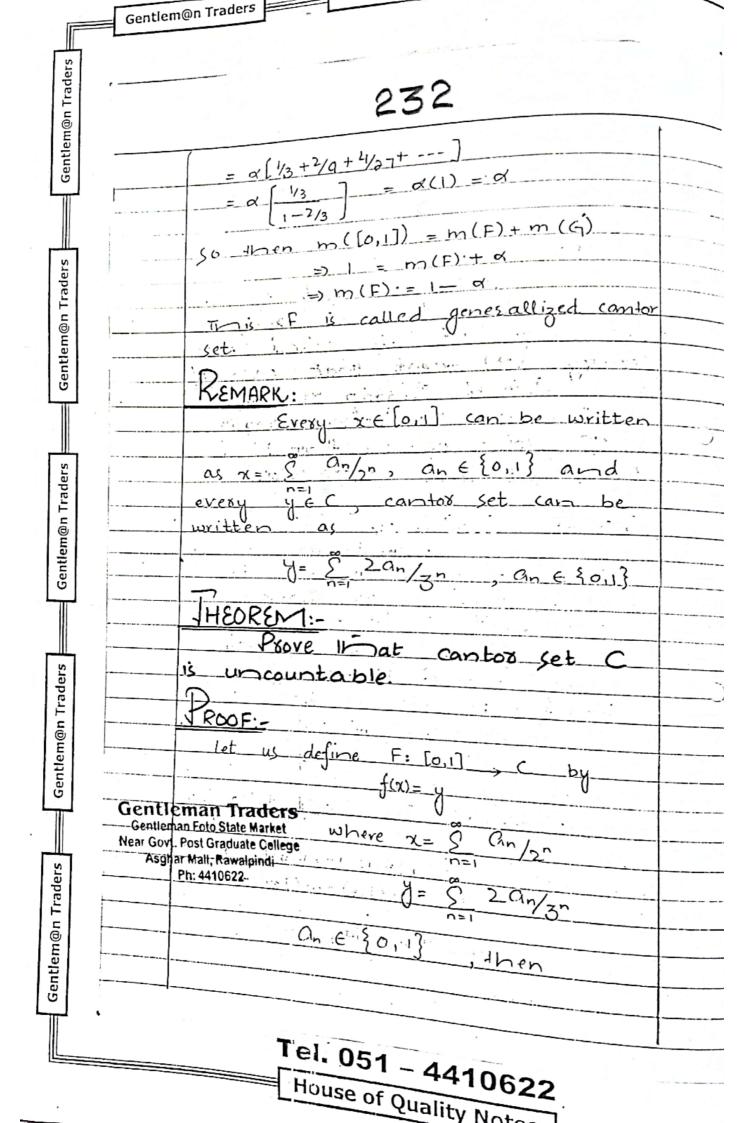
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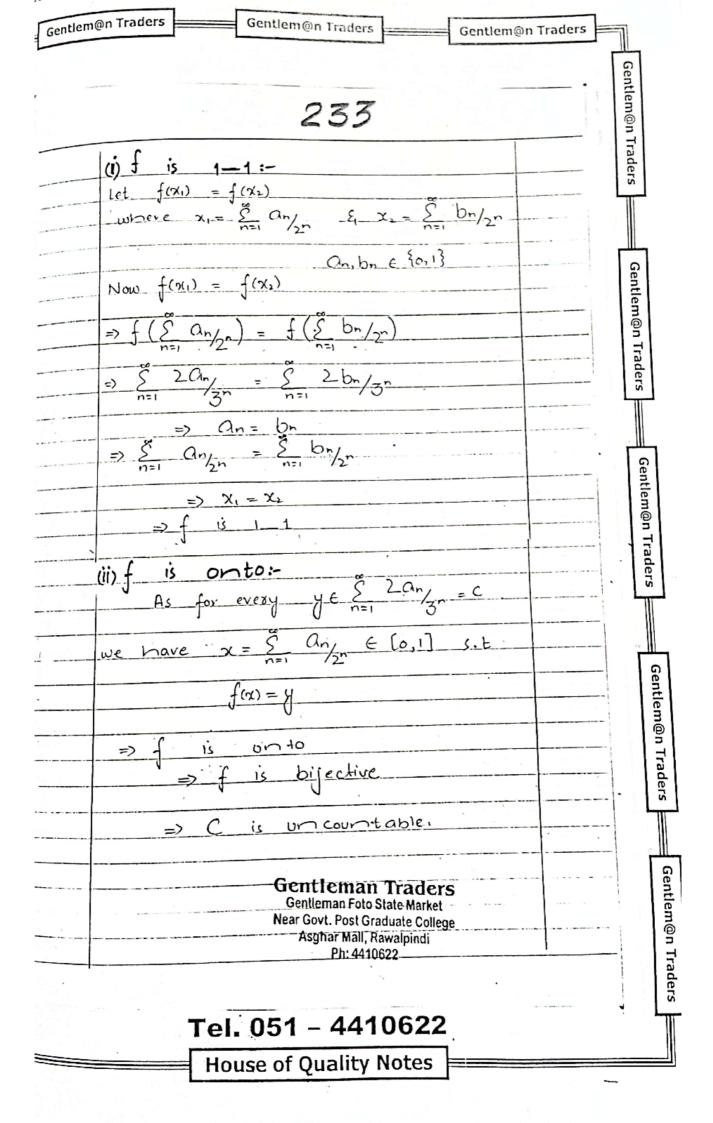
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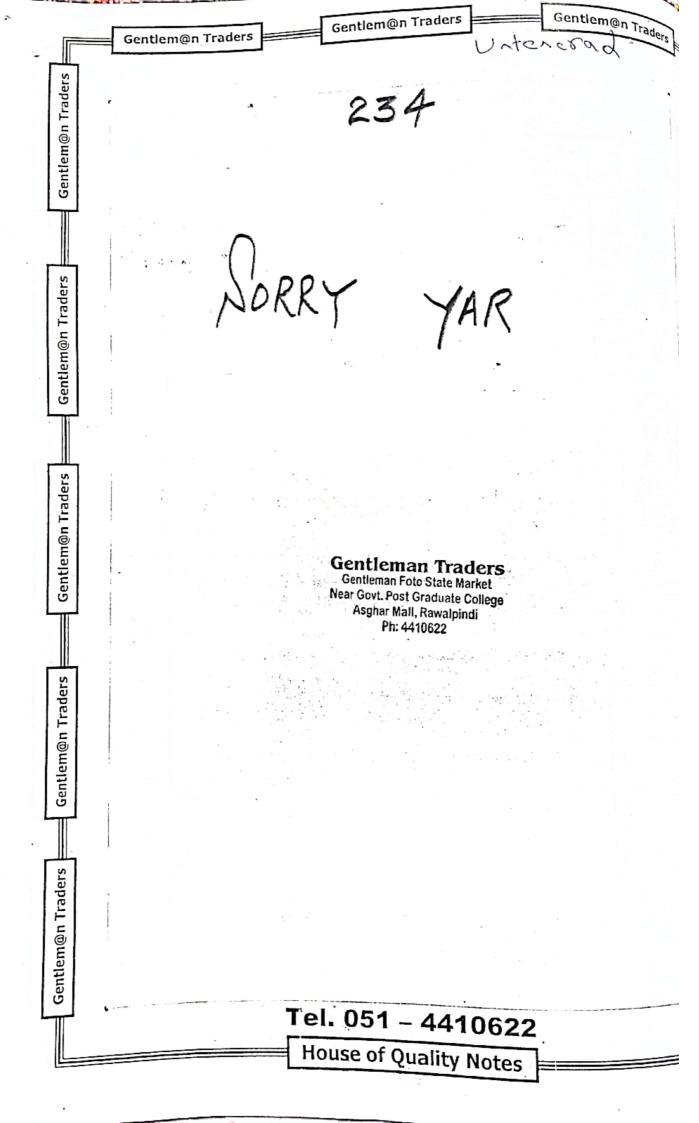


| | : [0,1]= CUG and cog= |
|---|--|
| | => 1- 0 = m (c)+1 |
| | => m (c) = 0 |
| | D |
| | ROPOSITION:- |
| | Let F be a subset of {0,13 |
| | constaucted in the same mannex as |
| | the cantoo set (also called contoo |
| | ternery set) except that each of |
| | the interval length removed at the 1th step has length |
| | at the nin step has length |
| | x.3" with oxxx1, then Filis |
| | closed set and m(F) |
| | Pems. |
| | = As in the construction of cantos |
| 7 | set at the non sept we removed 2n-1 |
| | paisuuse disjoint/ lopen intervals |
| | Inm, m=0,1,2,3, -2n-1 and each of len- |
| | -9th 3-n but by given condition, |
| _ | there in the construction of F at |
| 4 | the 1th step we sernove 2n-1 pais- |
| | - misé disjoint open intervals Inm, |
| - | m=1,2, 2n-1 and each of length |
| - | ckx 61 so 4 men |
| 1 | if G= (0,1) [27] Inm and F= [0,1] G |
| - | (() () () () |
| - | then $m(G) = m(I_1) + [m(I_{21}) + m(I_{22})] + [m(I_{31})]$ |
| + | m(J32) +m (J33) +m (J34)] + |
| + | 201 1 401 1 |
| | Gentleman Traders 20/1 + 40/27+ |
| | Gentleman Foto State Market Near Govt. Post Graduate Gollege |
| | Asghar Mall, Rawalpindi |
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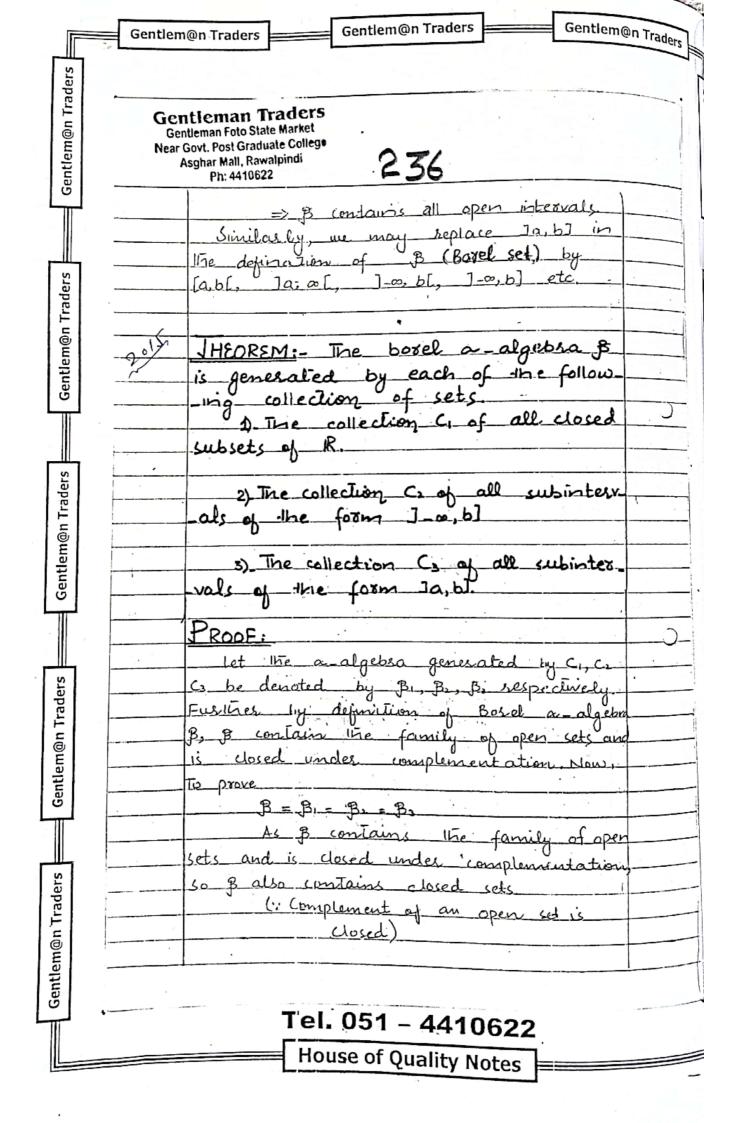


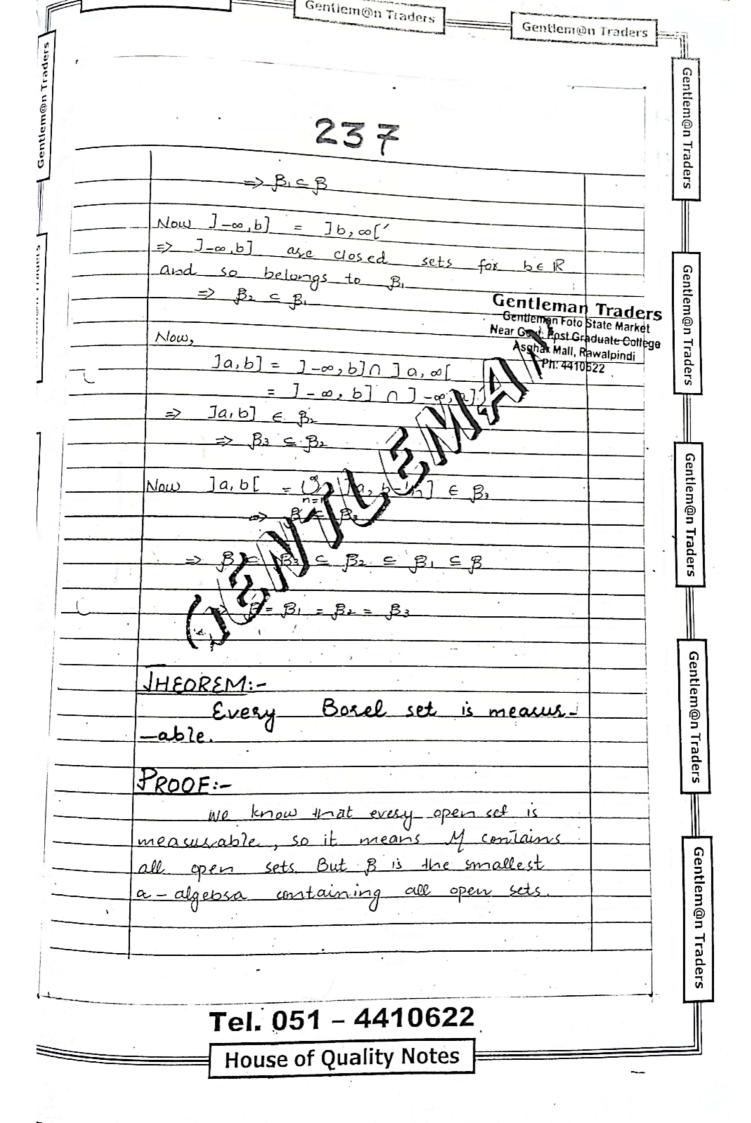


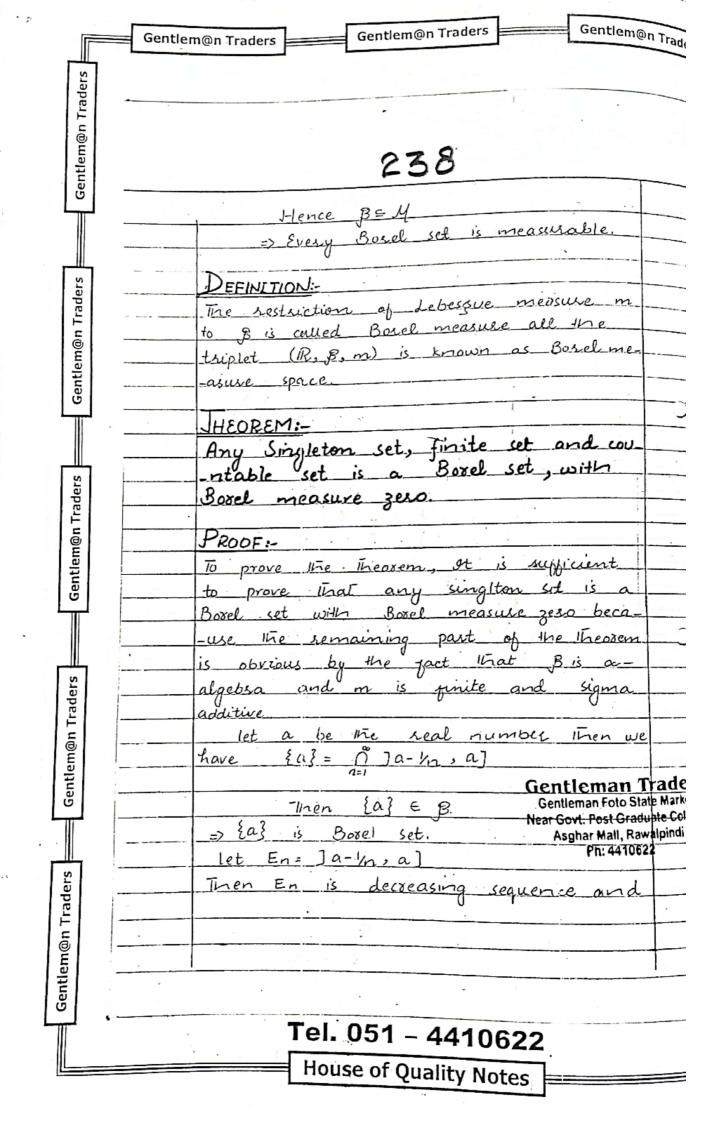
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Gentleman Foto State Market
Near Govt. Post Graduate College
Asghar Mall. Rawalpindi

| | sghar Mall, Rawalpindi Ph: 4410622 |
|--|---------------------------------------|
| | |
| Measure of an open set is alway | us non |
| a consed cal | andet lak |
| m(c)=0. Cantox set c is closed | and |
| m(c)=0. | |
| | |
| ii- If the measure of set is non zero | then it |
| 15 uncountable But if a set is un | acountat |
| -ble then its measure may be zero. | for exa- |
| -uple Cantox set c is uncountat | ole and |
| has measure zero. | |
| | |
| in Note that it might be possible | That |
| And but both has different me | easule. |
| e.g. R~ [o,1]~ c and m(R)= 0 | and |
| m(0,1) = 1 and $m(c) = 0$ | |
| | |
| iv Any finite set in R is closed and | so is |
| measuable. | |
| D | |
| BOREL DET:- | |
| Dollinition - Transportion B of | has al cat |
| Definition: The collection B of | · · · L |
| is defined to be a algebra gene | |
| by the collection of the intervals of |) the |
| form Jabl, a, b & R. The existence | eot |
| B is guaranteed by " let q be | a family |
| of subsets of X, then there is | small- |
| lest a - algebra containing G | " |
| of subsets of X, then there is a -est a - algebra containing G. Since open interval la, bl = 0.000 | 66-1/2] |
| | |
| | |
| | |

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({a}) = 0

closed set

measurable.

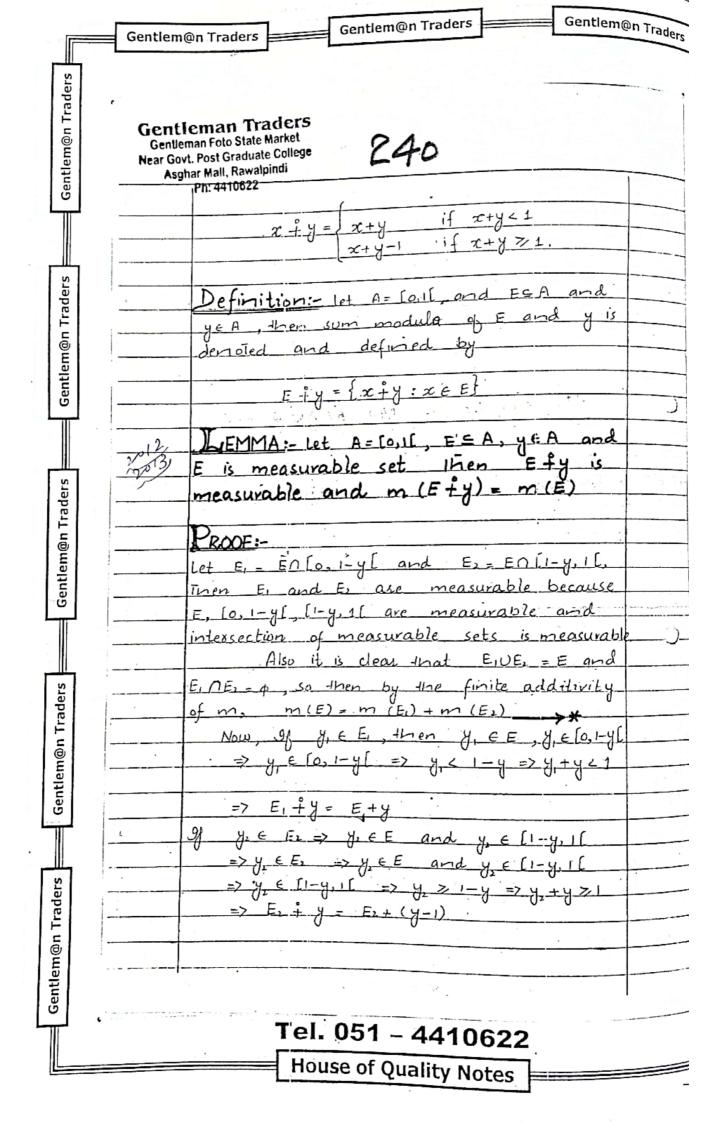
A= [0,1[

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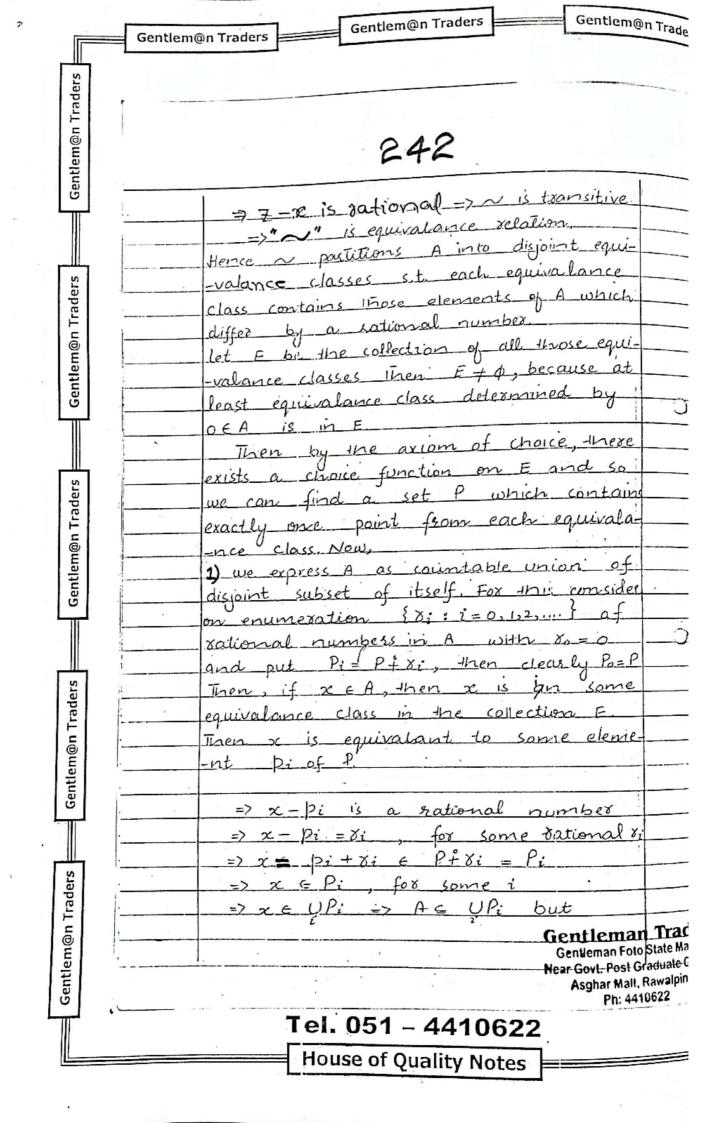
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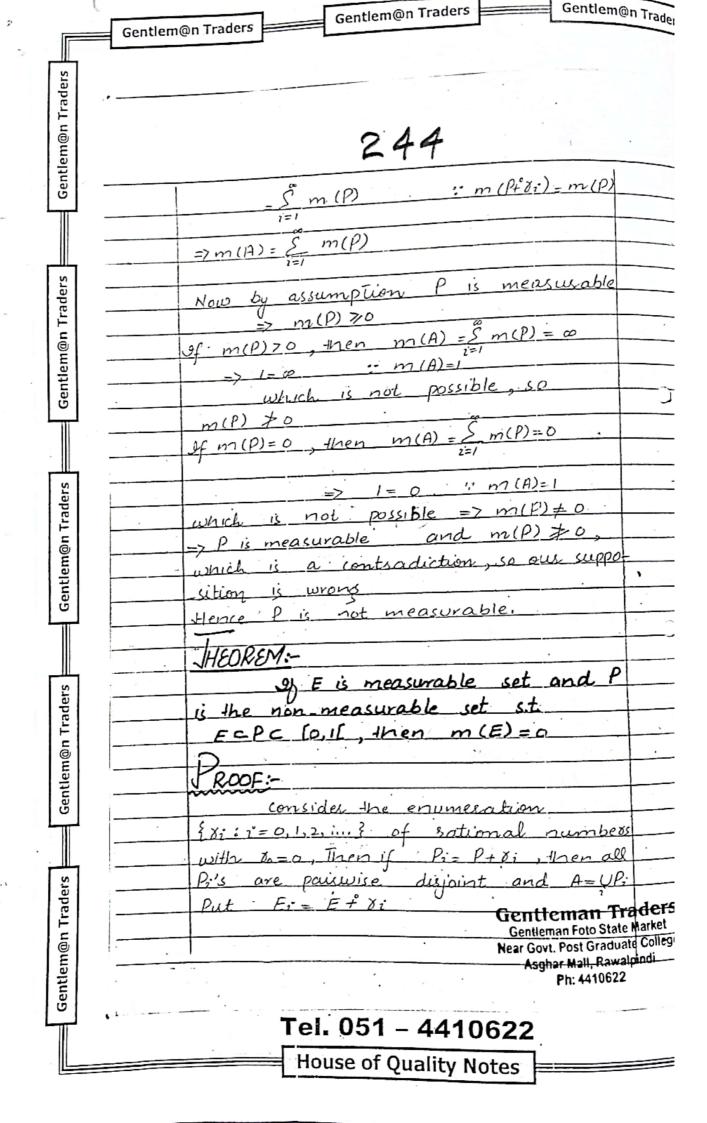
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| | the same of the sa |
|---|--|
| | also F_i 's are as: $P + \delta_i = P_i$ and |
| | With Dall Will a |
| | |
| | Thus $m(A) \ge m(UE_i)$ |
| | $=$ $\sum_{i=1}^{n} (i \in I_i)$ |
| | $As = \sum_{i} m(E_{i}) = \sum_{i} m(E)$ |
| | The contrable so m (F) 30 |
| | 2) m(E) >0, then & m(E) = 0 |
| | \Rightarrow $m(A) = \infty$ |
| | which is a contradiction because |
| - | m(A) = m((0,1) = 1 |
| | Hence m(E) to and thus m(E) = 0. |
| | $\frac{1}{1}$ |
| | JHEOREM:- |
| | |
| | y is a translation invariant |
| | measure defined on the a algebra |
| | containing the set P, then |
| | |
| | 4([0,1[)=0 08 4([0,1[)=0 |
| | Do |
| | PROOF: |
| | Let A = [0,1[and define relation "~" on |
| | A by x, y & A => x xy if x - y is |
| | sational number upto X |
| | Now 4(A) = 4 (Fort) = 4 (UP) |
| | 2 110:1-2 110:20 -2 1100 |
| | 2 M(P) |
| | 5 110 |
| | => M([o.1[) = < M(1)) |
| | 9 f u(D) = 0, then u(oil) = 0 |
| | AFU(D) >0 then U([oil]) =0 |
| | 1 le co enther ul ([OII) is |
| | |
| | Gentleman Traders |
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| | Gentleman Foto State Market |
| | Gentleman Foto State MarNet Near Govt. Post Graduate College Asghar Mall, Rawalpindi |

Tel. 051 - 4410622

Ph: 4410622

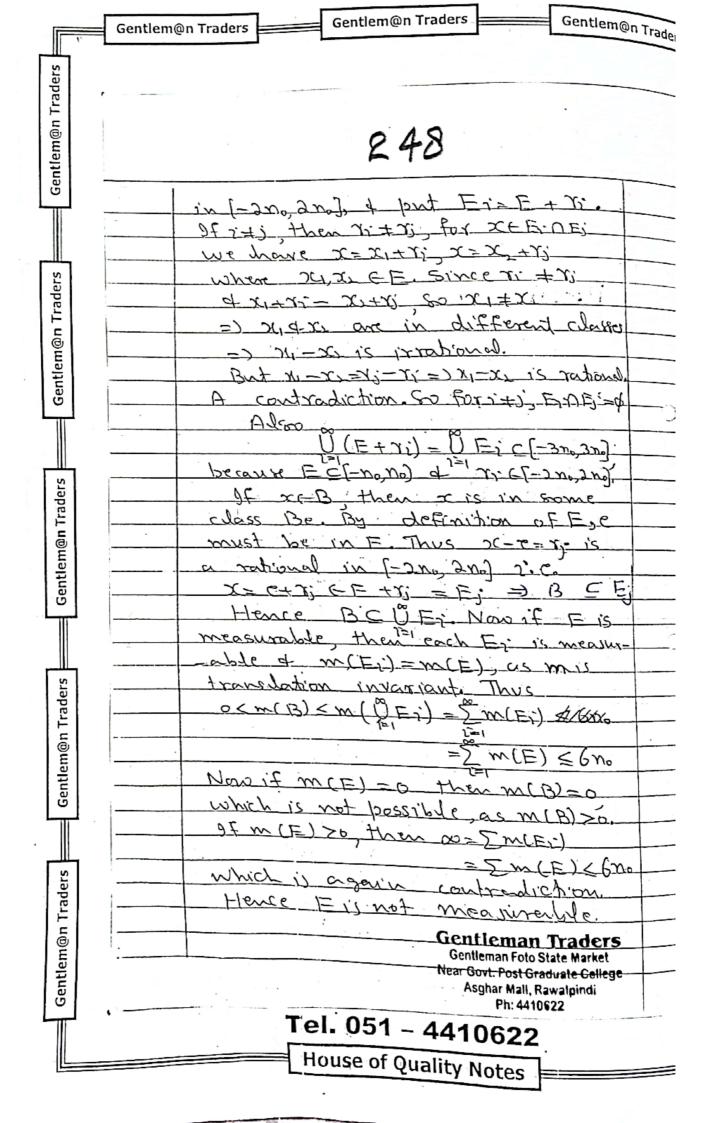
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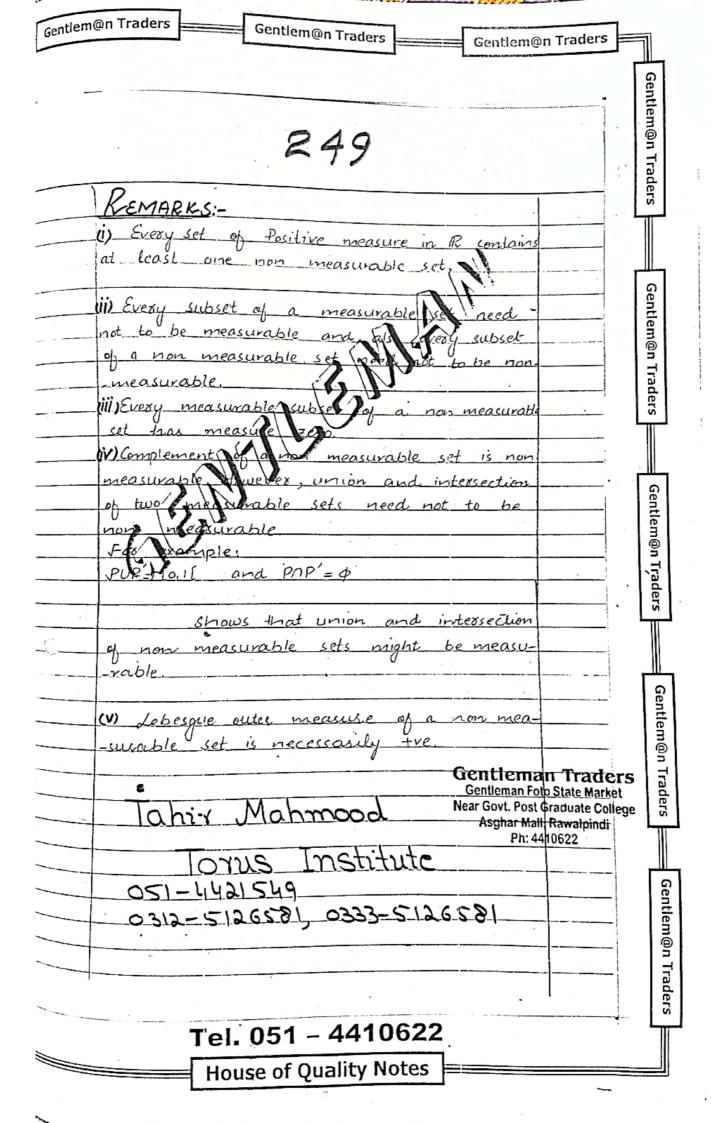
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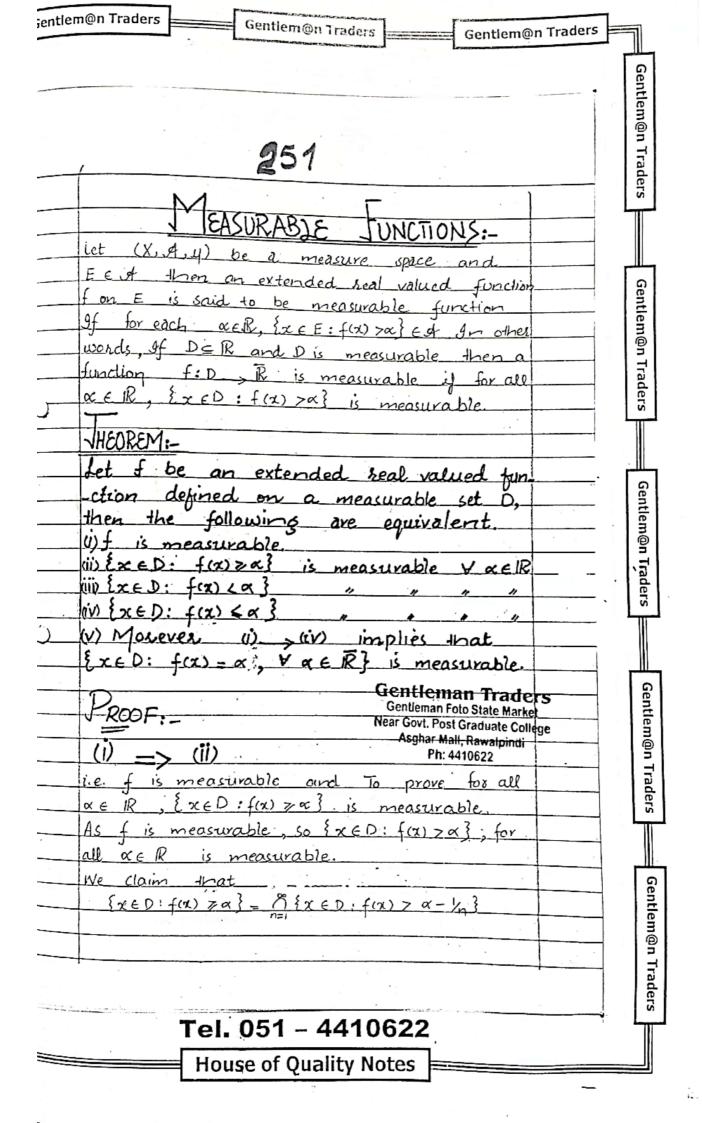


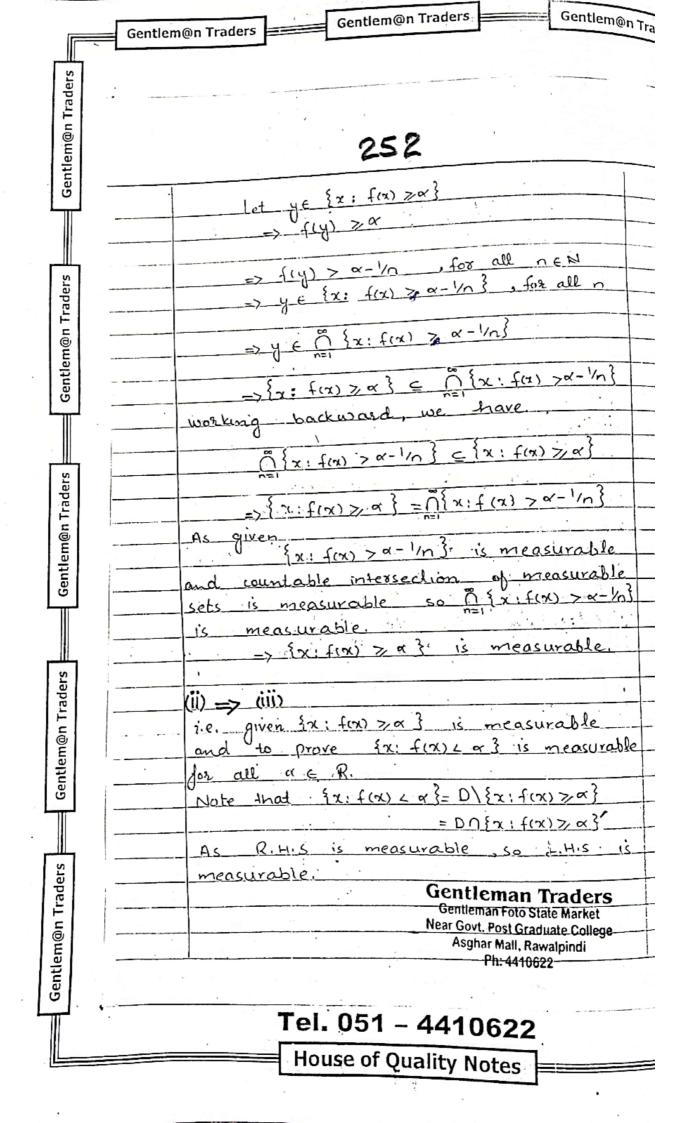


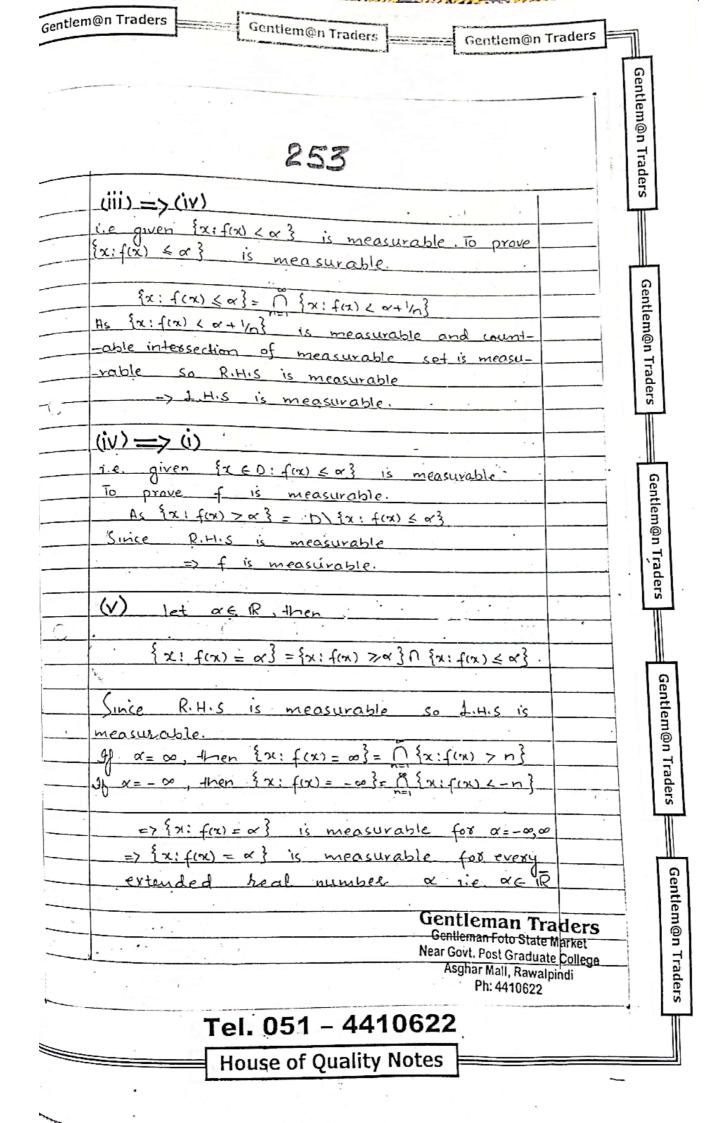
ONCE AGAIN

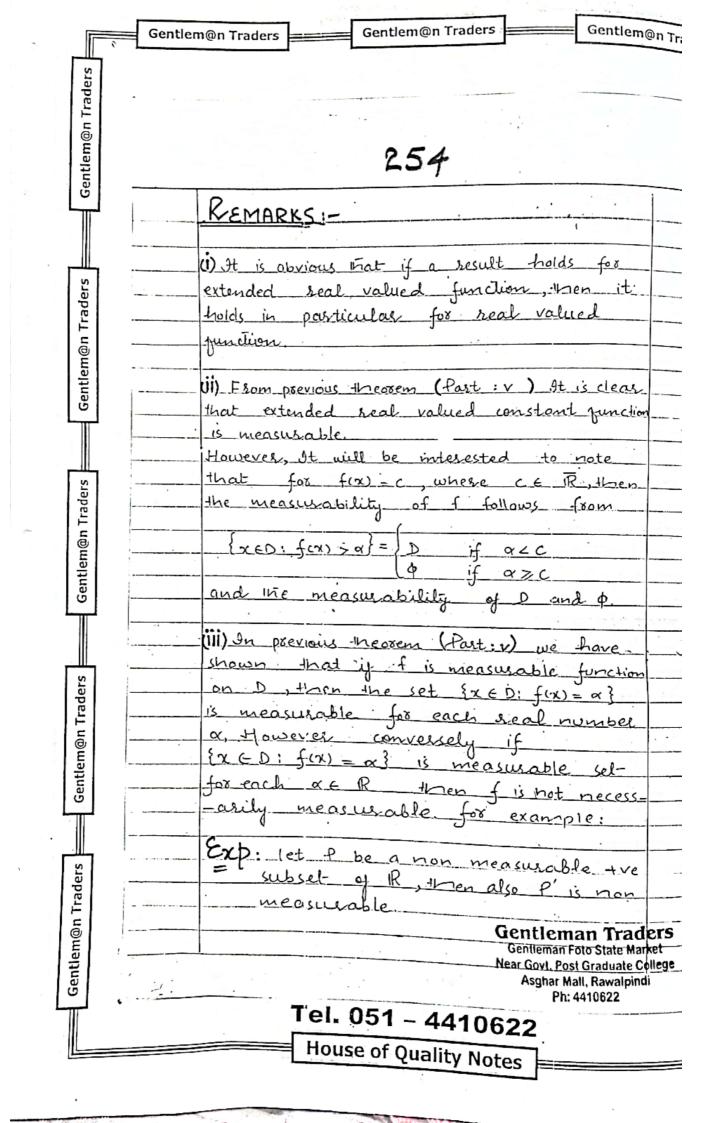
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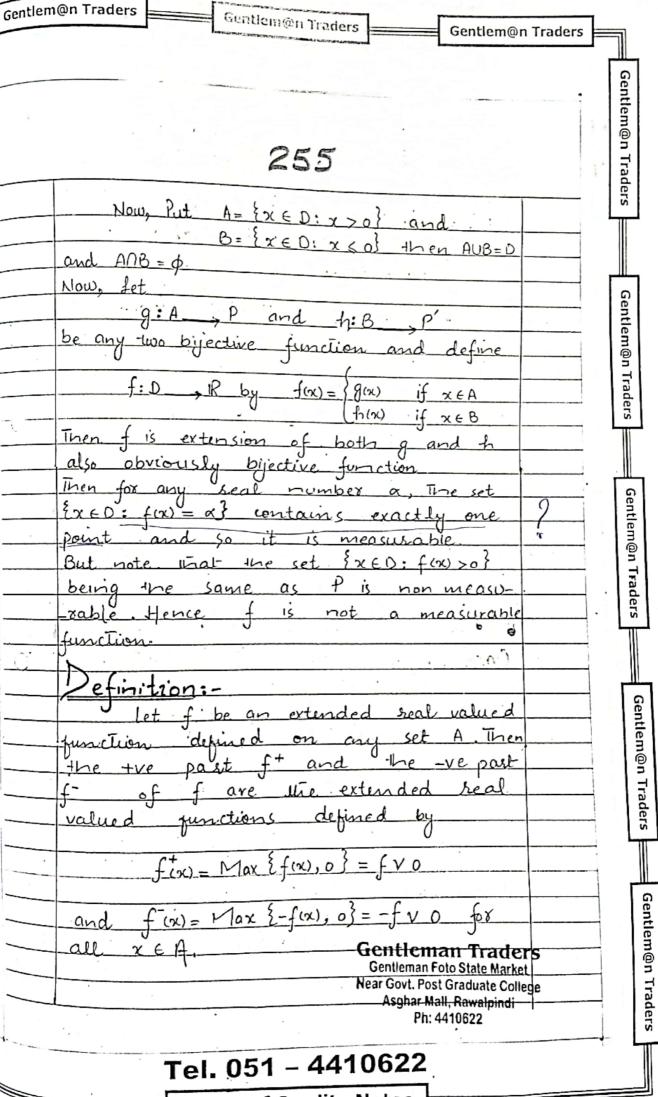
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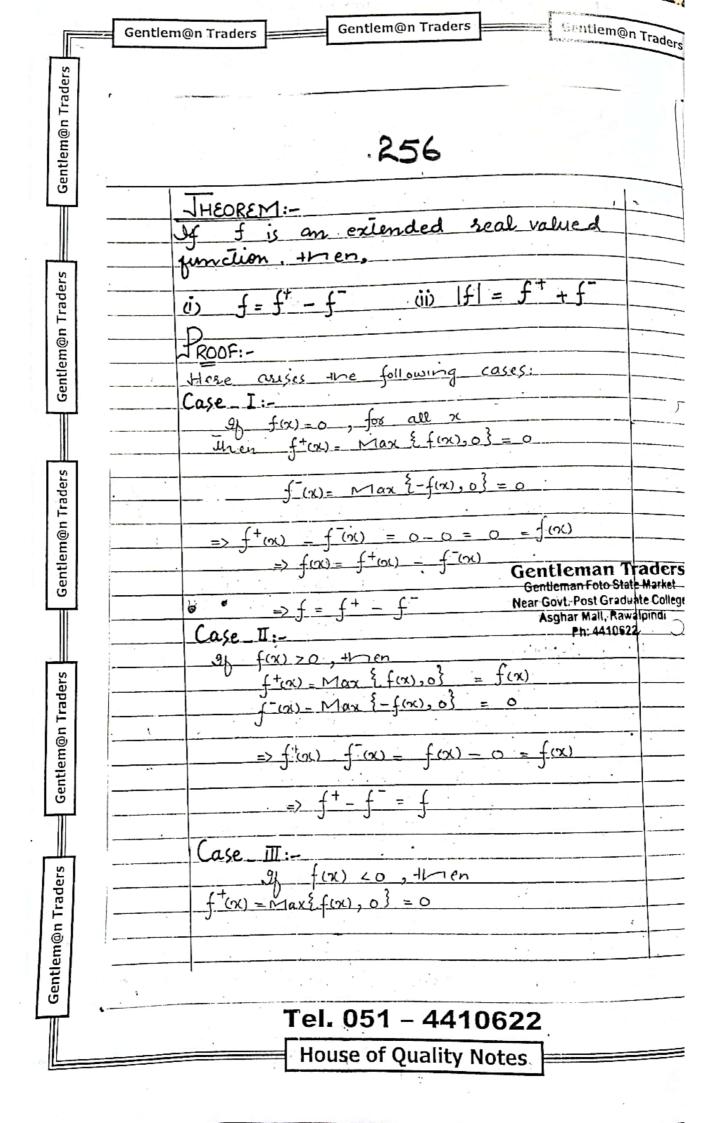












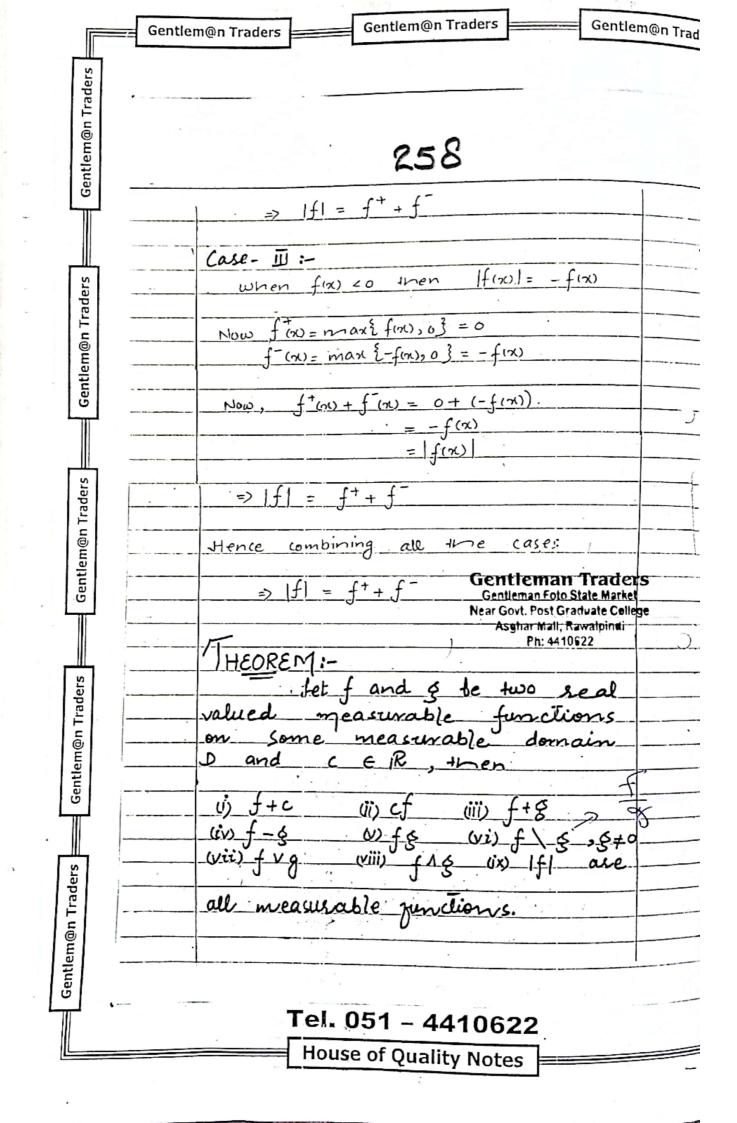
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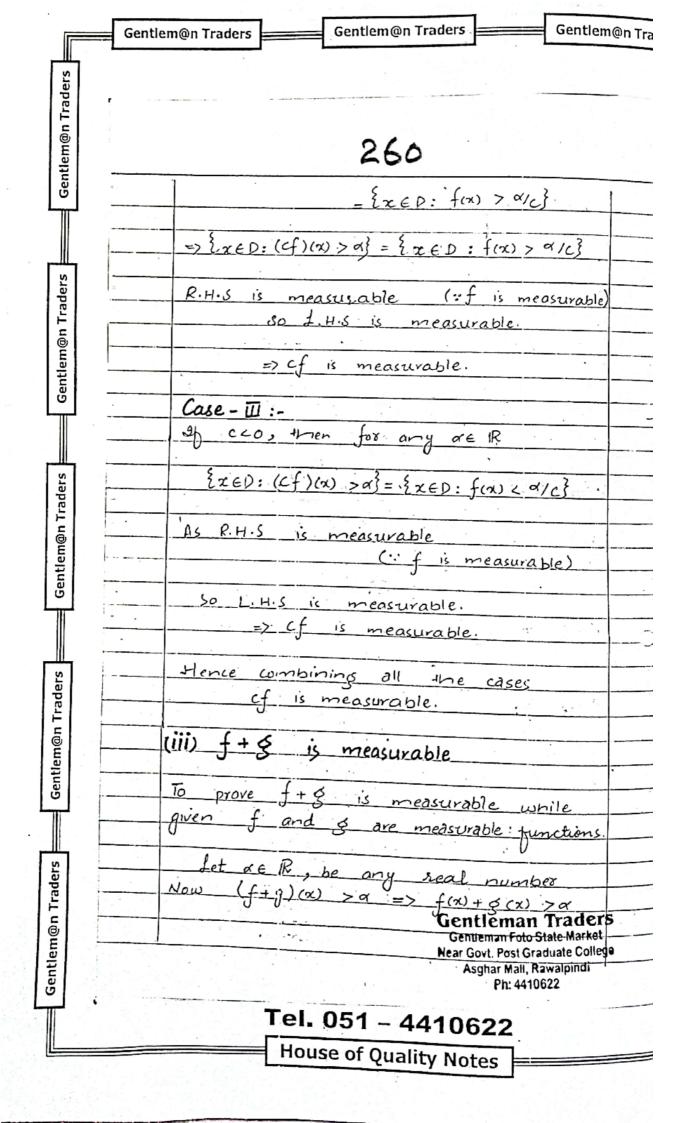
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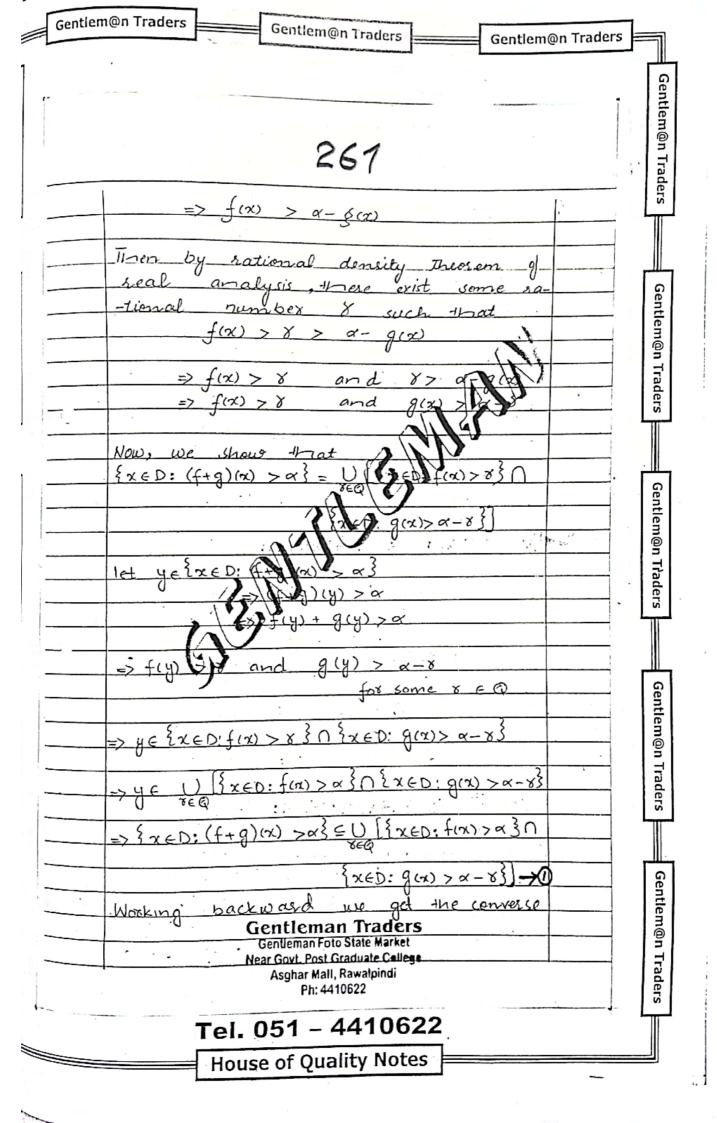
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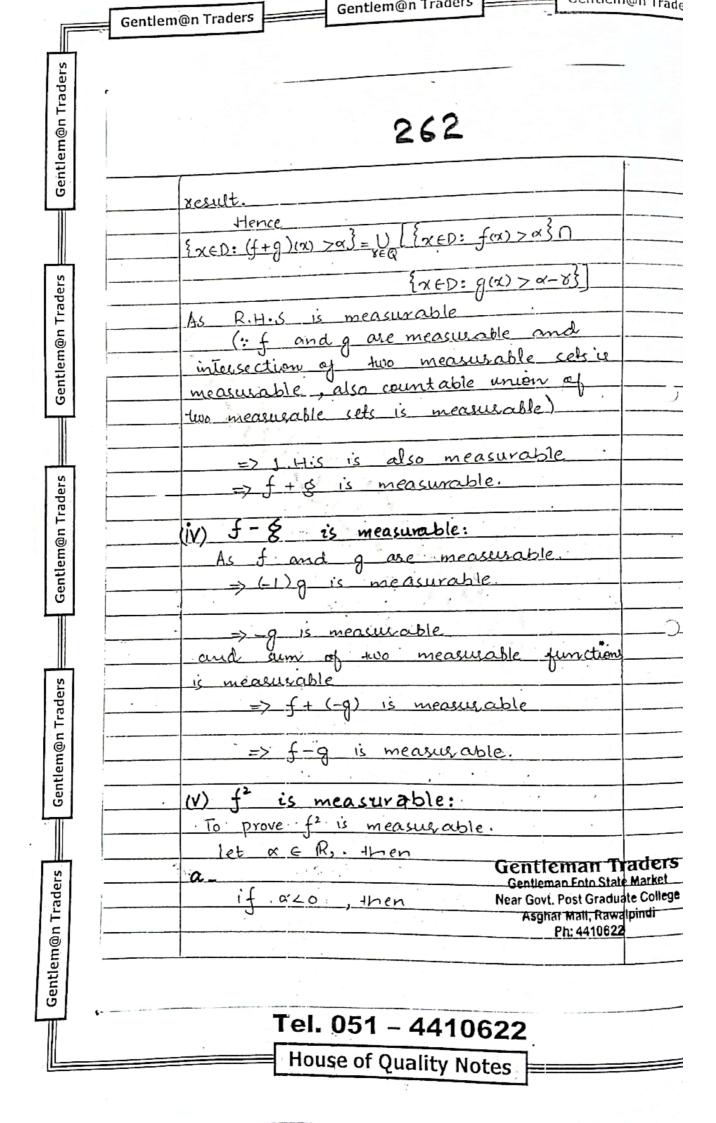
| Thus $ f'(x) = Max \left\{ -f(x), o \right\} = -f(x) $ $ f'(x) = f(x) = 0 - (-f(x)) = f(x) $ $ f'(x) = f(x) = 0 - (-f(x)) = f(x) $ $ f'(x) = f'(x) = f'(x) $ Thence (ombining all the cases) $ f = f' - f' = f' $ Gentleman Foto State Market Near Govt, Post Graduate College Asghar Mall, Rawalpind Ph: 4410622 Case I: If $f(x) = 0 = f(x) = f(x)$, $o = 0$ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = f'(x) + f'(x) = 0 + 0 = 0 = f(x) $ Now, $ f'(x) = Max \left\{ -f(x), o \right\} = f(x) $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = Max \left\{ -f(x), o \right\} = 0 $ $ f'(x) = f'(x) + f'(x) = f'(x) = f'(x) = f'(x) $ | Thus $ f^{+}(\alpha) = f(\alpha) = 0 - (-f(\alpha)) = f(\alpha) $ $ = $ | 10 U 20 C | |
|--|--|--|---|
| Thus $ \int_{-\infty}^{+\infty} f(x) = \int_{-\infty}^{+\infty} f(x) = \int_{-\infty}^{+\infty} f(x) $ $ = \int_{-\infty}^{+\infty} f(x) = $ | Thus $ f^{+}(\alpha) = f(\alpha) = 0 - (-f(\alpha)) = f(\alpha) $ $ = $ | f(x) = Max {-f(x) | $ x \circ y = -f(x)$ |
| $f'(x) = f(x) = 0 - (-f(x)) = f(x)$ $\Rightarrow f' - f = f$ Hence combining all the cases $f = f' - f$ Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mail, Rawarpind Ph: 4410622 $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | Frus $f^{+}(\alpha) = f(\alpha) = 0 - (-f(\alpha)) = f(\alpha)$ $\Rightarrow f^{+} - f = f$ Hence (ombining all the cases) $f = f^{+} - f$ Gentleman Foto State Market Near Govt. Post Graduate Colleg Asghar Mail, Rawapind Ph: 4410622 Case I:- if $f(\alpha) = 0 \Rightarrow f(\alpha) = 0$, $\forall \alpha \in A$ Then $f^{+}(\alpha) = Max + f(\alpha), o = 0$ $\Rightarrow f^{+}(\alpha) = Max + f^{+}(\alpha), o = 0$ $\Rightarrow f(\alpha) = f^{+}(\alpha) = f^{+}(\alpha) = f^{+}(\alpha)$ $\Rightarrow f = f^{+} + f^{-}(\alpha) = f^{+}(\alpha) = f^{+}(\alpha)$ Now, $f^{+}(\alpha) = Max + f^{-}(\alpha), o = f^{+}(\alpha)$ | | : -f(x) 70 |
| Hence (ombining all the cases $f = f^{+} - f^{-}$ Hence (ombining all the cases) $f = f^{+} - f^{-}$ Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpind Ph: 4410622 Fig. = 0 => $ f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = f(x) = f(x) = f(x) $ Case - II : $f(x) = f(x) = f(x) = f(x) $ Now $f(x) = f(x) = f(x) = f(x) $ $f(x) = f(x) = f(x) = f(x) $ $f(x) = f(x) = f(x) = f(x) $ | Hence combining all the cases $f = f^{+} - f^{-}$ Gentleman Trader Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mail, Rawaipind Ph: 4410622 $Case - I:-$ $f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = Max ^{2} - f(x), o^{2} = 0$ $= 7 f^{+}(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $Case - II:-$ $if f(x) > 0, then f(x) = f(x)$ $Now, f(x) = Max ^{2} - f(x), o^{2} = f(x)$ $f(x) = Max ^{2} - f(x), o^{2} = 0$ | Trus | V |
| Hence (ombining all the cases $f = f^{+} - f^{-}$ Hence (ombining all the cases) $f = f^{+} - f^{-}$ Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpind Ph: 4410622 Fig. = 0 => $ f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = f(x) = f(x) = f(x) $ Case - II : $f(x) = f(x) = f(x) = f(x) $ Now $f(x) = f(x) = f(x) = f(x) $ $f(x) = f(x) = f(x) = f(x) $ $f(x) = f(x) = f(x) = f(x) $ | Hence combining all the cases $f = f^{+} - f^{-}$ Gentleman Trader Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mail, Rawaipind Ph: 4410622 $Case - I:-$ $f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), o^{2} = 0$ $f(x) = Max ^{2} - f(x), o^{2} = 0$ $= 7 f^{+}(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $Case - II:-$ $if f(x) > 0, then f(x) = f(x)$ $Now, f(x) = Max ^{2} - f(x), o^{2} = f(x)$ $f(x) = Max ^{2} - f(x), o^{2} = 0$ | f (n) - f (n) - 0 - | (-f(n)) = f(n) |
| Hence (ombining all the cases) $f = f^{+} - f$ Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpind Ph: 4410622 $Case - I := f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max + f(x), 0 = 0$ $= f(x) = Max + f(x), 0 = 0$ $= f(x) = f(x) = f(x)$ $Case - II := f(x)$ $f(x) = f(x) = f(x) = f(x)$ Now, $f(x) = Max + f(x), 0 = f(x)$ $f(x) = Max + f(x), 0 = f(x)$ $f(x) = Max + f(x), 0 = f(x)$ | Hence (ombining all the cases $f = f^{+} - f$ Gentleman Trader. Gentleman Foto State Market Near Govt. Post Graduate Colleg Asghar Mail, Rawalpind Ph: 4410622 Case - I:- if $f(x) = 0 = f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max \frac{1}{2} f(x), 0 = 0$ $= f(x) = Max \frac{1}{2} - f(x), 0 = 0$ $= f(x) + f(x) = 0 + 0 = 0 = f(x)$ Case - II:- if $f(x) \neq 0$, then $f(x) = f(x)$ Now, $f^{+}(x) = Max \frac{1}{2} - f(x), 0 = 0$ $f^{+}(x) = Max \frac{1}{2} - f(x), 0 = 0$ | | |
| $f = f^{+} - f$ $(ii) f = f^{+} + f^{-}$ Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpind Ph: 4410622 $Case - I:-$ $if f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ $Then f^{+}(x) = Max \{f(x), a\} = 0$ $f(x) = Max \{-f(x), o\} = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $Case - II:-$ $if f(x) > 0, then f(x) = f(x)$ $Now, f(x) = Max \{-f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | $f = f^{+} - f$ Gentleman Trader Gentleman Foto State Market Near Govt, Post Graduate Colleg Asghar Mall, Rawalpind Ph: 4410622 Case _ I:- if $f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), a^{2} = 0$ $f(x) = Max ^{2} - f(x), a^{2} = 0$ $f(x) = f^{+}(x) = f(x) = f(x)$ Case _ II:- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max ^{2} - f(x), a^{2} = f(x)$ $f(x) = Max ^{2} - f(x), a^{2} = f(x)$ $f(x) = Max ^{2} - f(x), a^{2} = f(x)$ | J J | J |
| Gentleman Fraders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawatpind Ph: 4410622 Case $I:$ if $f(x) = 0 \Rightarrow f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max & f(x), a & = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ Case $II:$ if $f(x) \neq 0 \Rightarrow f(x) = f(x)$ $= f(x) + f(x) \Rightarrow 0 \Rightarrow f(x) = f(x)$ Now, Now, $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ | Gentleman Frader Gentleman Foto State Market Near Govt. Post Graduate Colleg Asghar Mall, Rawalpind Ph: 4410622 Case I:- if $f(x) = 0 \Rightarrow f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ $= \int f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $= \int f(x) + f(x) = 0 + 0 \Rightarrow f(x) = f(x)$ if $f(x) \neq 0$, then $ f(x) = f(x)$ Now, $f^{+}(x) = Max ^{2} f(x), 0^{2} = f(x)$ $f(x) = Max ^{2} f(x), 0^{2} = f(x)$ $f(x) = Max ^{2} f(x), 0^{2} = f(x)$ | Hence Combining | all the cases |
| Gentleman Fraders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawatpind Ph: 4410622 Case $I:$ if $f(x) = 0 \Rightarrow f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max & f(x), a & = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ Case $II:$ if $f(x) \neq 0 \Rightarrow f(x) = f(x)$ $= f(x) + f(x) \Rightarrow 0 \Rightarrow f(x) = f(x)$ Now, Now, $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ $f(x) = Max & f(x), a & = f(x)$ | Gentleman Frader Gentleman Foto State Market Near Govt. Post Graduate Colleg Asghar Mall, Rawalpind Ph: 4410622 Case I:- if $f(x) = 0 \Rightarrow f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ $= \int f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $= \int f(x) + f(x) = 0 + 0 \Rightarrow f(x) = f(x)$ if $f(x) \neq 0$, then $ f(x) = f(x)$ Now, $f^{+}(x) = Max ^{2} f(x), 0^{2} = f(x)$ $f(x) = Max ^{2} f(x), 0^{2} = f(x)$ $f(x) = Max ^{2} f(x), 0^{2} = f(x)$ | $f = f^{+} - f^{-}$ | |
| Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mail, Rawalpind Ph: 4410622 Case \overline{I} : If $f(x) = 0 \Rightarrow f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ $= f(x) = Max ^{2} f(x), 0^{2} = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ Case \overline{I} : if $f(x) \neq 0$, then $ f(x) = f(x)$ Now, Now, $f(x) = Max ^{2} f(x), 0^{2} = f(x)$ $f(x) = Max ^{2} f(x), 0^{2} = 0$ | (ii) $f = f + f$ Gentleman Foto State Market Near Govt. Post Graduate Colleg Asghar Mall. Rawalpind Ph: 4410622 Case $J := f(x) = 0$ $f(x) = 0 = f(x) = 0$ $f(x) = f(x) = f(x)$ Case $-II := f(x)$ if $f(x) = f(x) = f(x)$ Alow, $f(x) = f(x) = f(x)$ | | Gentleman Traders |
| Asghar Mall, Rawatpind Ph: 4410622 Case I:- if $f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ $f(x) = Max ^{2} - f(x), 0^{2} = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ if $f(x) \neq 0$, then $ f(x) = f(x)$ Now, $f^{+}(x) = Max ^{2} f(x), 0^{2} \Rightarrow f(x) $ $= f(x) = Max ^{2} f(x), 0^{2} \Rightarrow f(x) $ | Sol Asghar Mall, Rawalpind Ph: 4410622 Then $f(x) = 0 \Rightarrow f(x) = 0, \forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0 ^{2} = 0$ $f(x) = Max ^{2} - f(x), 0 ^{2} = 0$ $= f(x) + f(x) = 0 + 0 = 0 \Rightarrow f(x) $ Case $-II$: if $f(x) > 0$, then $ f(x) = f(x)$ Now, Now, $f(x) = Max ^{2} - f(x), 0 ^{2} = f(x)$ $f(x) = Max ^{2} - f(x), 0 ^{2} = 0$ | $f(ii) f = f^{+} + f^{-}$ | Gentleman Foto State Market |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | From $f(x) = 0$ => $ f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ $f(x) = Max ^{2} - f(x), 0^{2} = 0$ => $f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ (=>) $ f = f + f $ Case - $ I = f $ if $f(x) > 0$, then $ f(x) = f(x) $ Now, Now, $f^{+}(x) = Max ^{2} f(x), 0^{2} = f(x) $ $f^{+}(x) = Max ^{2} f(x), 0^{2} = 0$ | | Asghar Mall, Rawalpindi |
| if $f(x) = 0$ => $ f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max \{f(x), 0\} = 0$ $f(x) = Max \{f(x), 0\} = 0$ => $f(x) + f(x) = 0 + 0 = 0 = f(x) $ => $ f = f^{+} + f$ Case - $II := f(x) = f(x) = f(x)$ Now, $f(x) = Max \{f(x), 0\} = f(x)$ $f(x) = Max \{f(x), 0\} = 0$ $f(x) = Max \{f(x), 0\} = 0$ | if $f(x) = 0$ => $ f(x) = 0$, $\forall x \in A$ Then $f^{+}(x) = Max \{f(x), o\} = 0$ $f(x) = Max \{f(x), o\} = 0$ => $f^{+}(x) + f(x) = 0 + 0 = 0 = f(x) $ | Sol | Ph: 4410622 |
| Then $f^{+}(x) = Max \frac{1}{2} f(x), 0 = 0$ $f^{-}(x) = Max \frac{1}{2} - f(x), 0 = 0$ $= f^{-}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= f^{-}(x) + f^{-}(x) + f^{-}(x) = 0$ $= f^{-}(x) + f^{-}(x) + f^{-}(x) = 0$ $= f^{-}(x) + f^{-}(x) + f^{-}(x) = 0$ | Then $f^{+}(x) = Max \frac{1}{2} + f(x), 0 = 0$ $f^{-}(x) = Max \frac{1}{2} - f(x), 0 = 0$ $= 7 f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= 7 f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= 7 f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= 7 f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= 7 f^{+}(x) + f^{-}(x) = 0 + 0 = 0 = f(x) $ $= 7 f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{+}(x) + f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{+}(x) + f^{-}(x) = f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) + f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x) = f^{-}(x) = f^{-}(x)$ $= 7 f^{-}(x) + f^{-}(x) = f^{-}(x)$ | - Case I:- | VI-O X X FA |
| f(x) = Max - f(x), 0 = 0 $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f(x) + f(x) + f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 7 f(x) + f($ | f(x) = Max - f(x), 0 = 0 $= 7 f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= 2 f = f + f$ $Case - II :-$ $= f(x) = f(x) = f(x)$ $= f(x) = f(x) = f(x)$ $= f(x) = f(x) = f(x) $ | $\int \frac{f(x) = 0}{f(x)} = \int \frac{f(x)}{f(x)} dx$ | (40) 23 - 0 |
| $= \int f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= \int f = f^{+} + f$ $Case - II := f(x) = f(x) = f(x)$ if $f(x) > 0$, then $ f(x) = f(x)$ $= \int f(x) = Max \{f(x), o\} = f(x)$ $= \int f(x) = Max \{-f(x), o\} = 0$ | $= \frac{1}{f(x)} + \frac{1}{f(x)} = 0 + 0 = 0 = f(x) $ $= \frac{1}{f(x)} = \frac{1}{f(x)} + \frac{1}{f(x)} = \frac{1}{f(x)}$ | | |
| $= \int f(x) + f(x) = 0 + 0 = 0 = f(x) $ $= \int f = f^{+} + f$ $Case - II := f(x) = f(x) = f(x)$ if $f(x) > 0$, then $ f(x) = f(x)$ $= \int f(x) = Max \{f(x), o\} = f(x)$ $= \int f(x) = Max \{-f(x), o\} = 0$ | $= \frac{1}{f(x)} + \frac{1}{f(x)} = 0 + 0 = 0 = f(x) $ $= \frac{1}{f(x)} = \frac{1}{f(x)} + \frac{1}{f(x)} = \frac{1}{f(x)}$ | f(x) = Max 2- | -f(x),0 = 0 |
| Case - \overline{II} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | Case - \overline{I} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{f(x), o\} = 0$ | | |
| Case - \overline{II} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | Case - \overline{I} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{f(x), o\} = 0$ | = 7 f'(x) + f(x) = 0 | 0+0=0= f(x) |
| Case - \overline{I} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | Case - \overline{U} :- if $f(x) > 0$, then $ f(x) = f(x)$ Now, $f(x) = Max \{f(x), a\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | | |
| if $f(x) > 0$, then $f(x) = f(x)$ Now, $f(x) = Max \{f(x), 0\} = f(x)$ $f(x) = Max \{-f(x), 0\} = 0$ | if $f(x) > 0$, then $f(x) = f(x)$ Now, $f(x) = Max \{f(x), 0\} = f(x)$ $f(x) = Max \{-f(x), 0\} = 0$ | (=> f + f | |
| if $f(x) > 0$, then $f(x) = f(x)$ Now, $f(x) = Max \{f(x), 0\} = f(x)$ $f(x) = Max \{-f(x), 0\} = 0$ | if $f(x) > 0$, then $f(x) = f(x)$ Now, $f(x) = Max \{f(x), 0\} = f(x)$ $f(x) = Max \{-f(x), 0\} = 0$ | The second secon | |
| Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = 0$ | Now, $f(x) = Max \{f(x), o\} = f(x)$ $f(x) = Max \{-f(x), o\} = o$ | Case - 11:- | f(x) = f(x) |
| f(x) = Max (x), 0 = 0 $f(x) = Max (-f(x), 0) = 0$ | f(x) = Max (2 + (x), 0) f(x) = Max (2 - (x), 0) = 0 | if 1(x) 70, 11.6 | |
| $f(x) = \max \left\{-f(x), 0\right\}$ | $f(x) = \max\{-f(x), 0\}$ | Now, (+ , fox), | $a^{\frac{1}{2}} = f(x)$ |
| $\int (x) = \int (x) = \int (x) + 0 = \int (x) = f(x) $ $\int (x) = \int (x) + \int (x) = \int (x) + 0 = \int (x) = f(x) $ | $\int (x) = \int (x) = \int (x) + 0 = \int (x) = \int (x)$ $\int (x) + \int (x) = \int (x) + 0 = \int (x) = \int (x$ | $\frac{f(x) = N(0x)}{\xi - f(x)}$ | , 0} = 0 |
| $50 f^{+}(x) + f^{-}(x) = f(x) + 0 = f(x) = \int_{0}^{\infty} f($ | $50 f^{+}(x) + f^{-}(x) = f(x) + 0 = f(x) = \int_{-\infty}^{\infty} f(x) + \int_{-\infty}^{\infty} f(x) = \int_{$ | f (x)= Max_b | - 1 Cm) |
| 70 1 (| 70 (31.) | $(\alpha f^{+}(x) + f^{-}(x)) = f(x)$ | $\chi) + 0 = \int (\chi) = \int (\chi)$ |
| | | 70 (27) | |

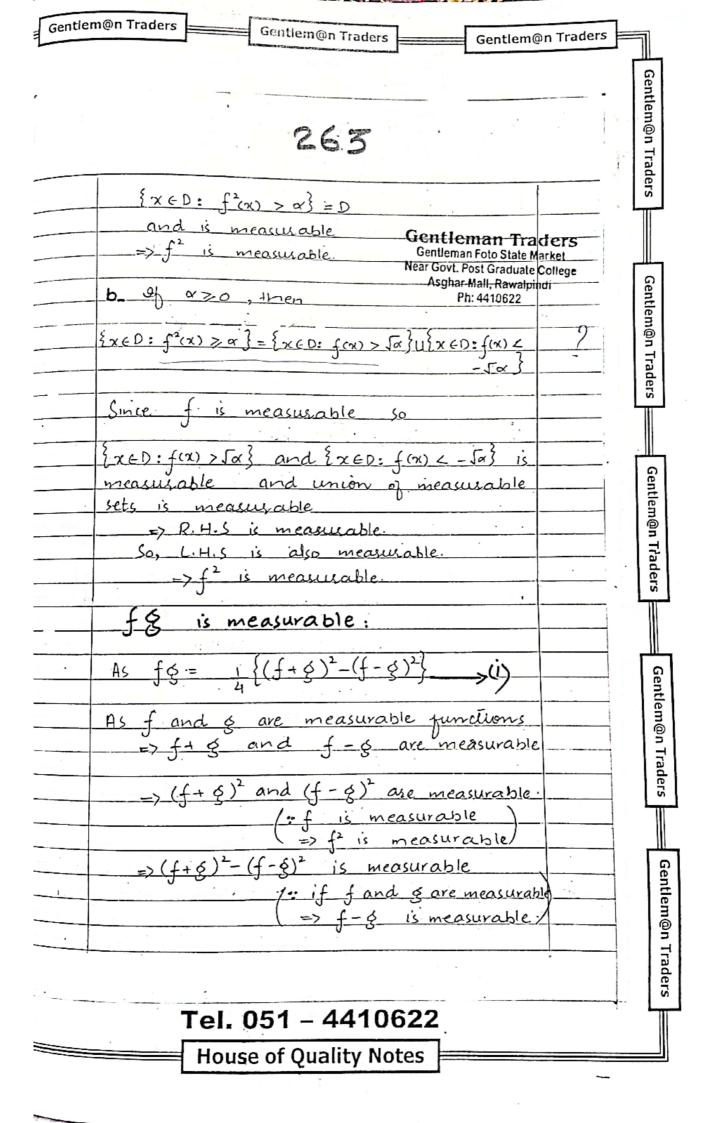
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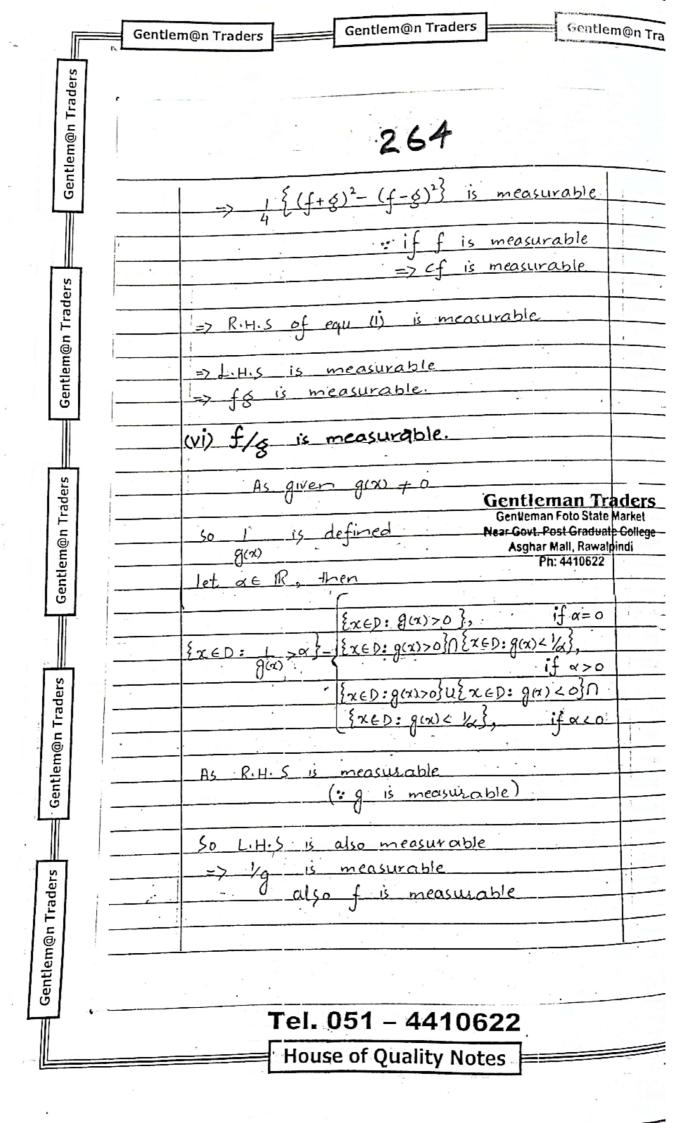


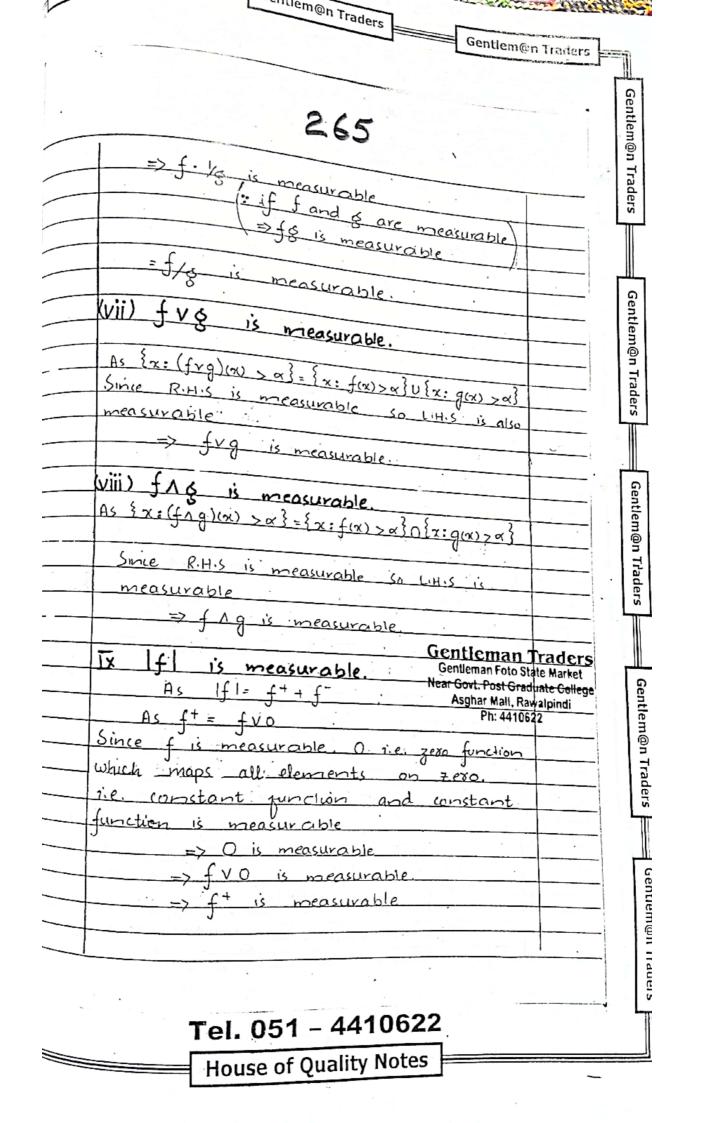


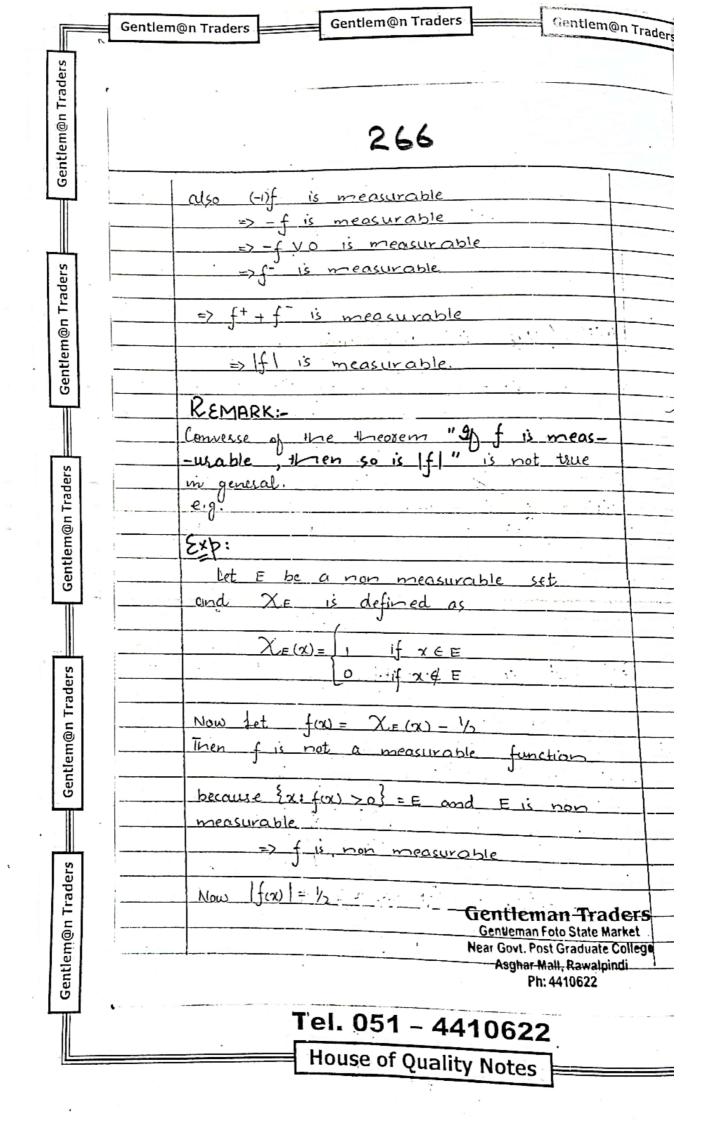


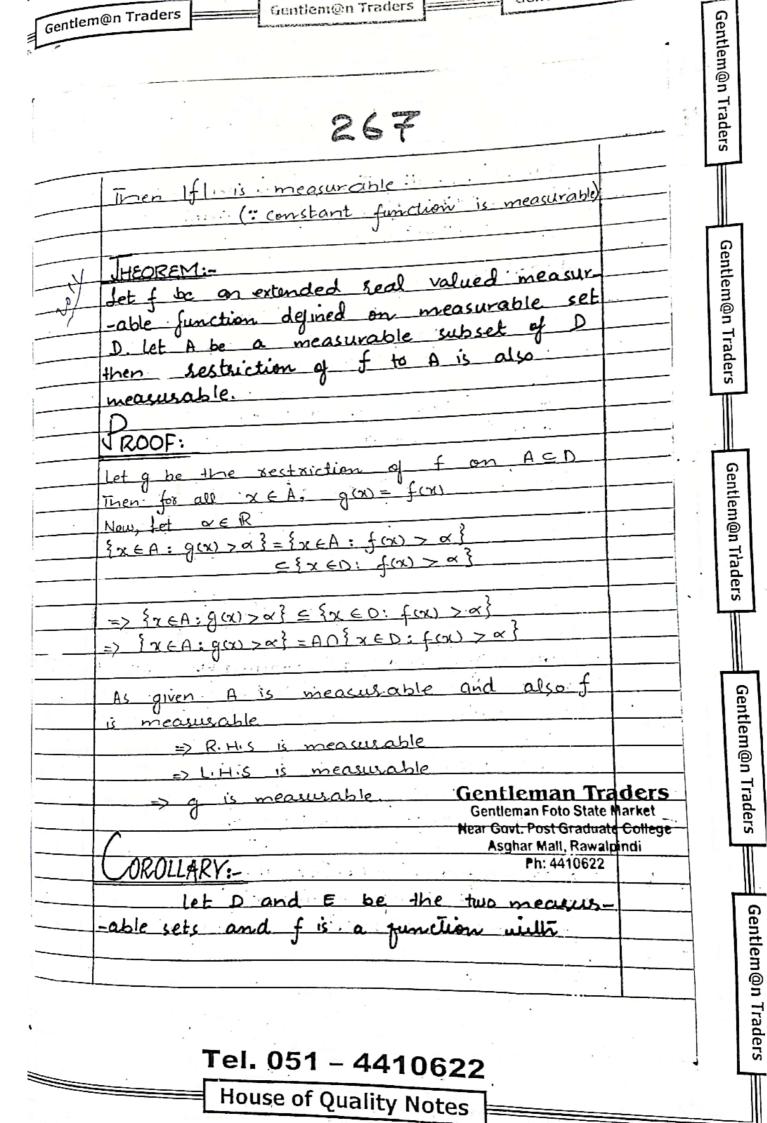


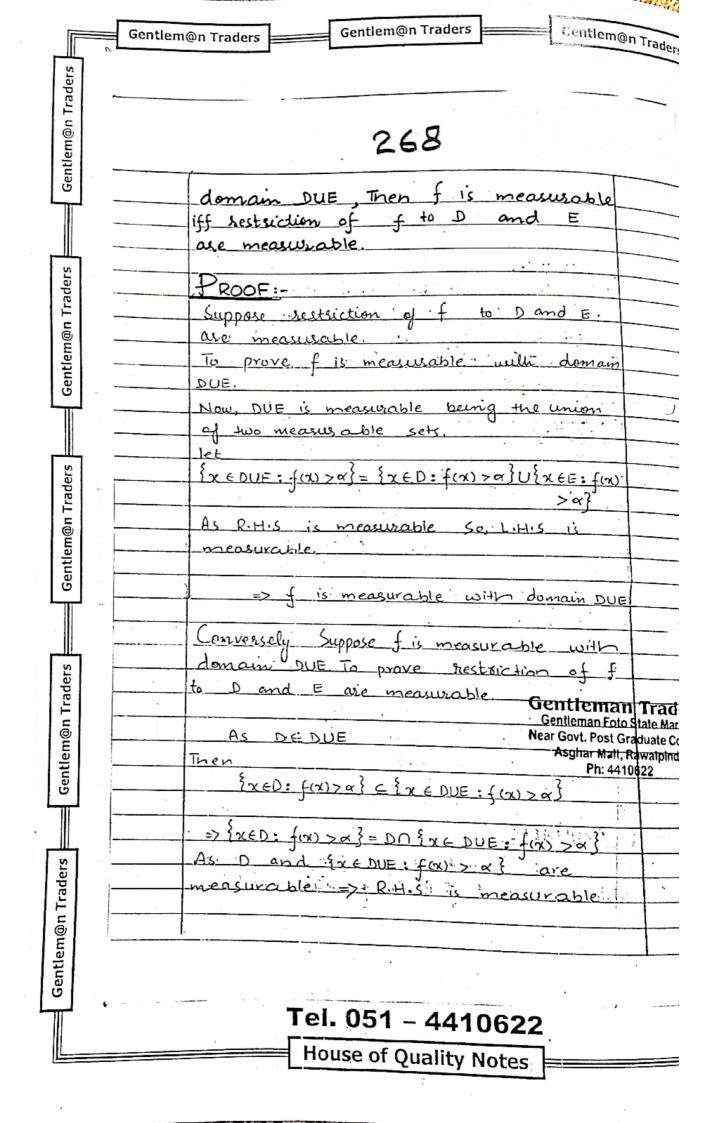


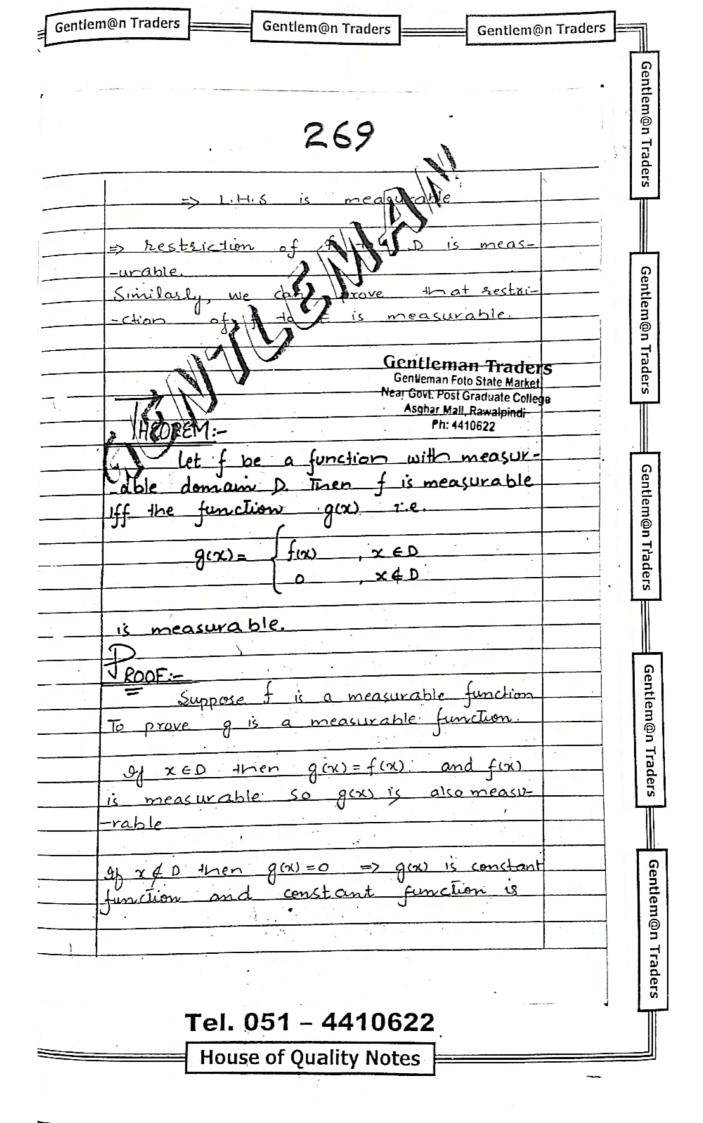


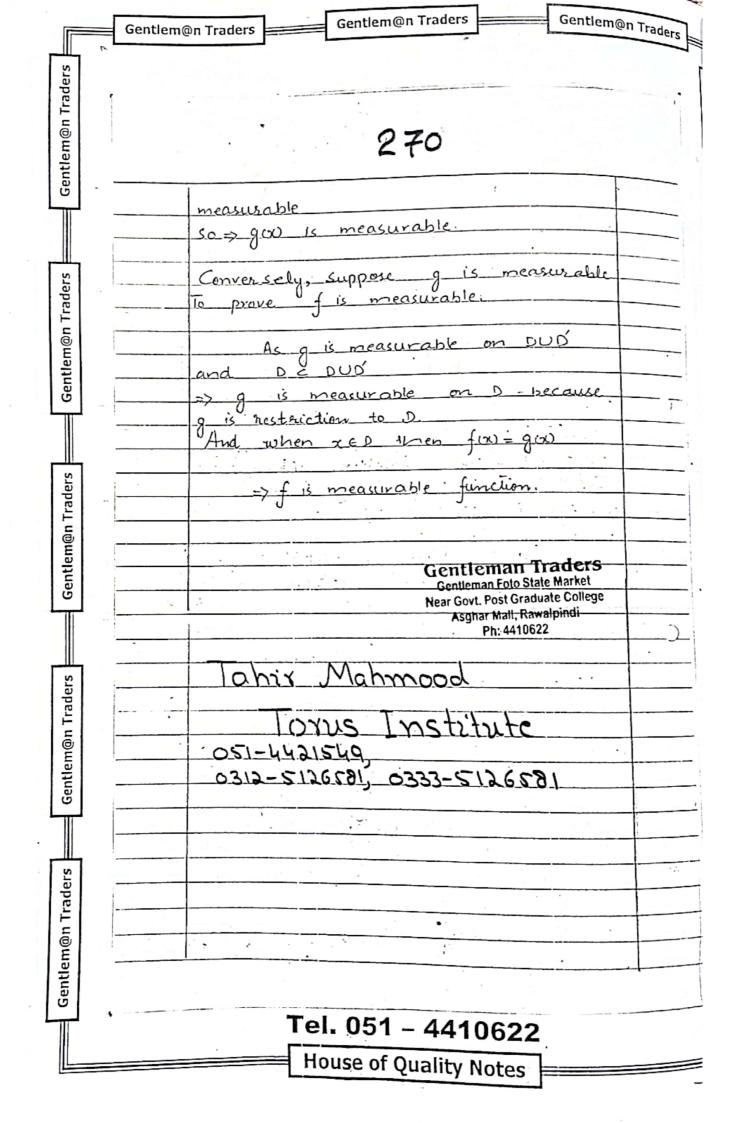


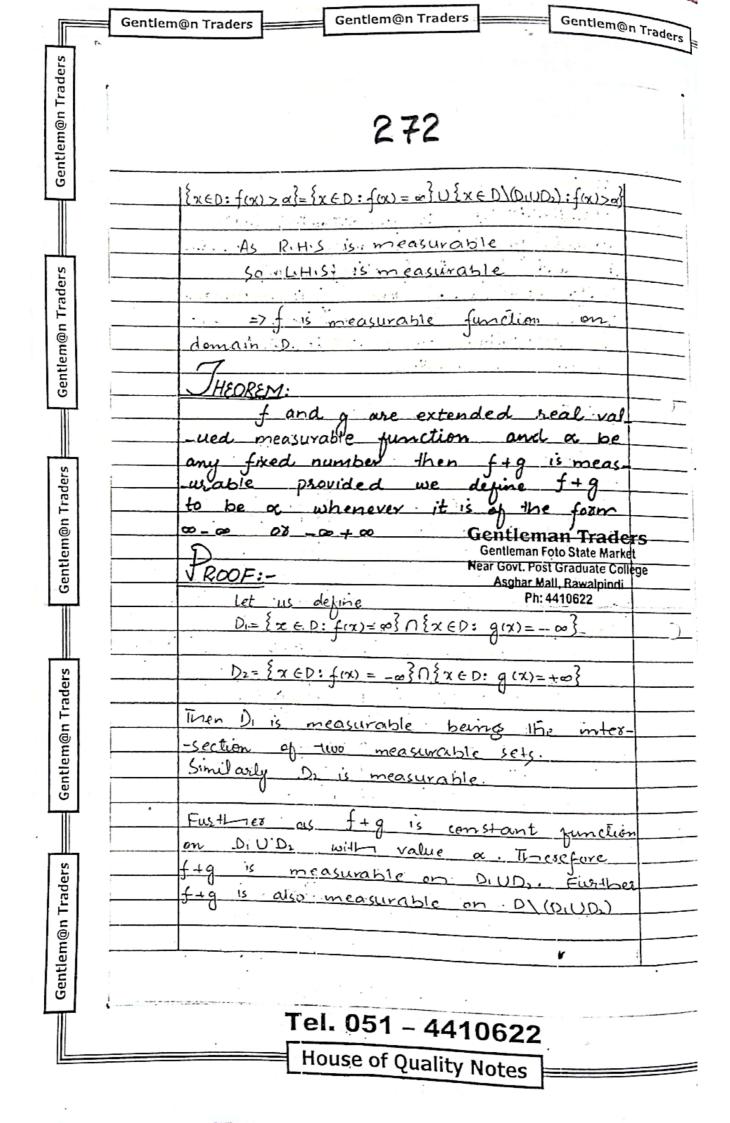


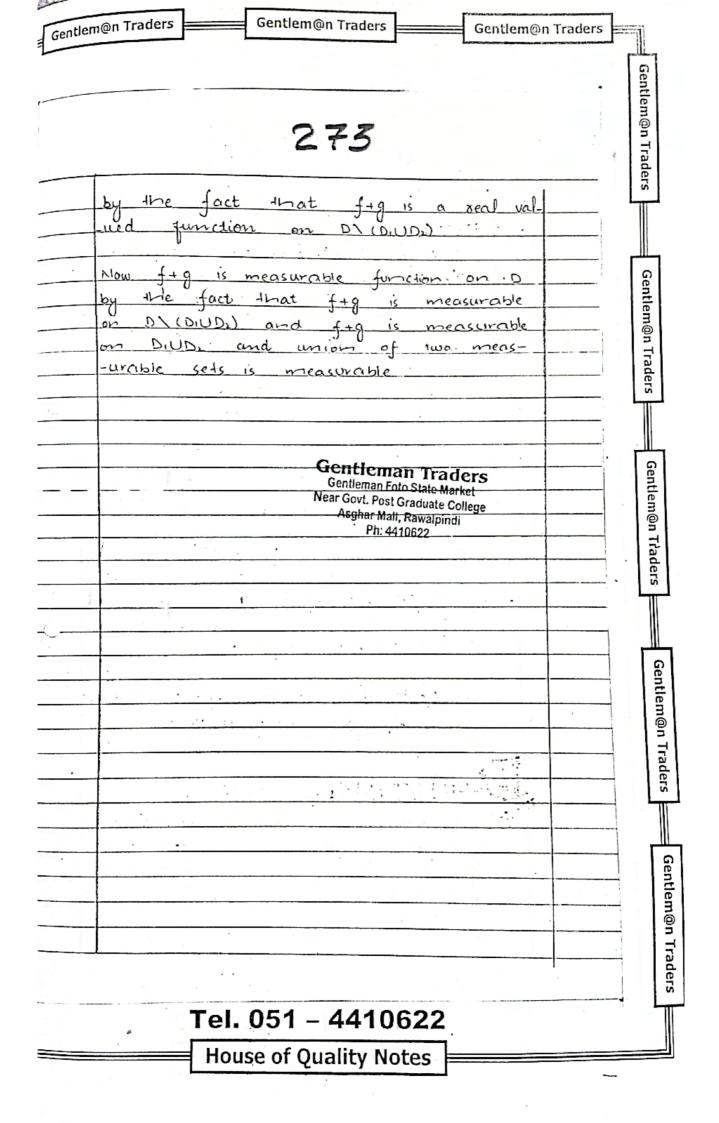




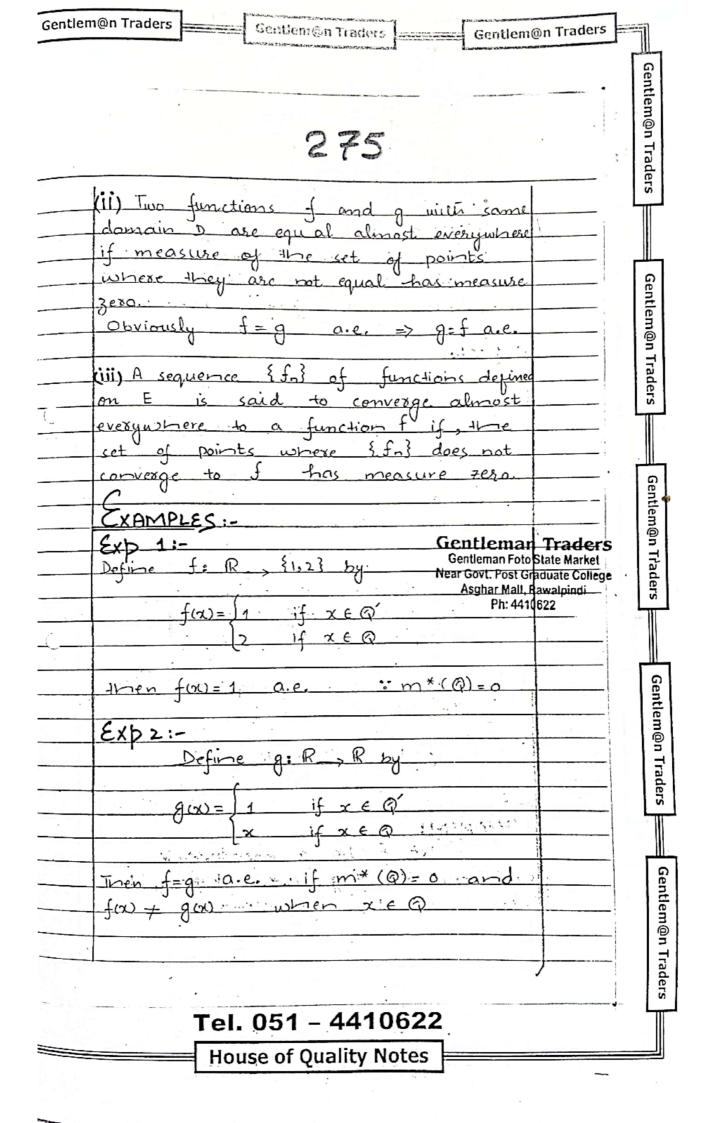


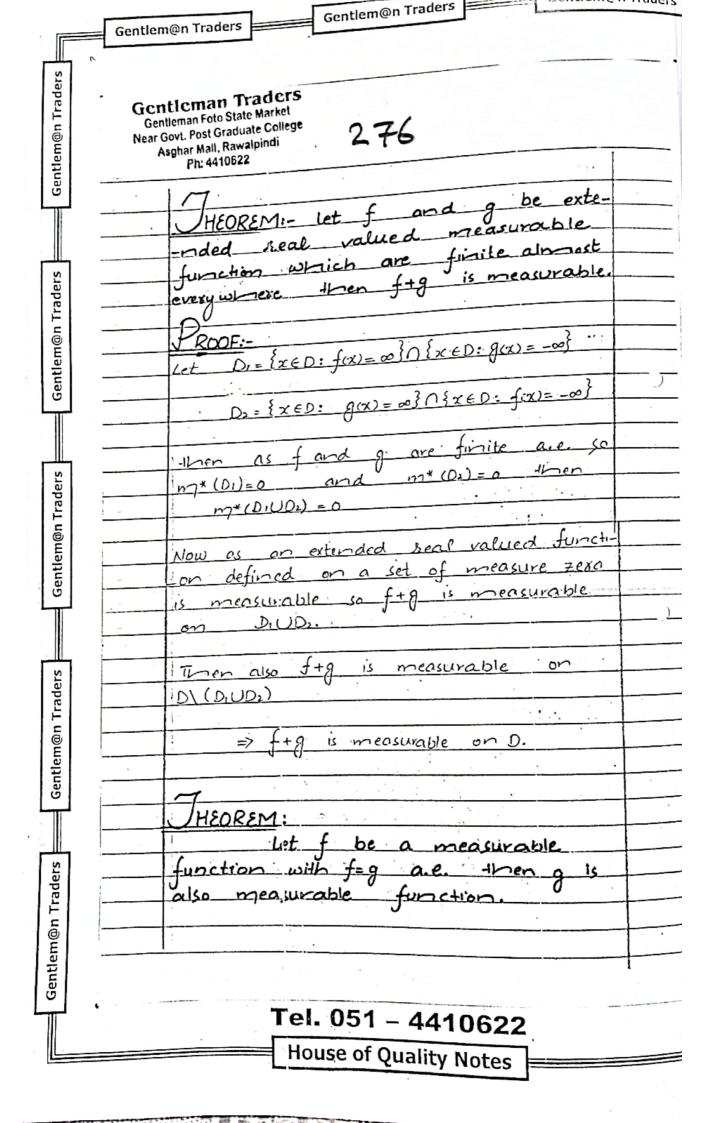


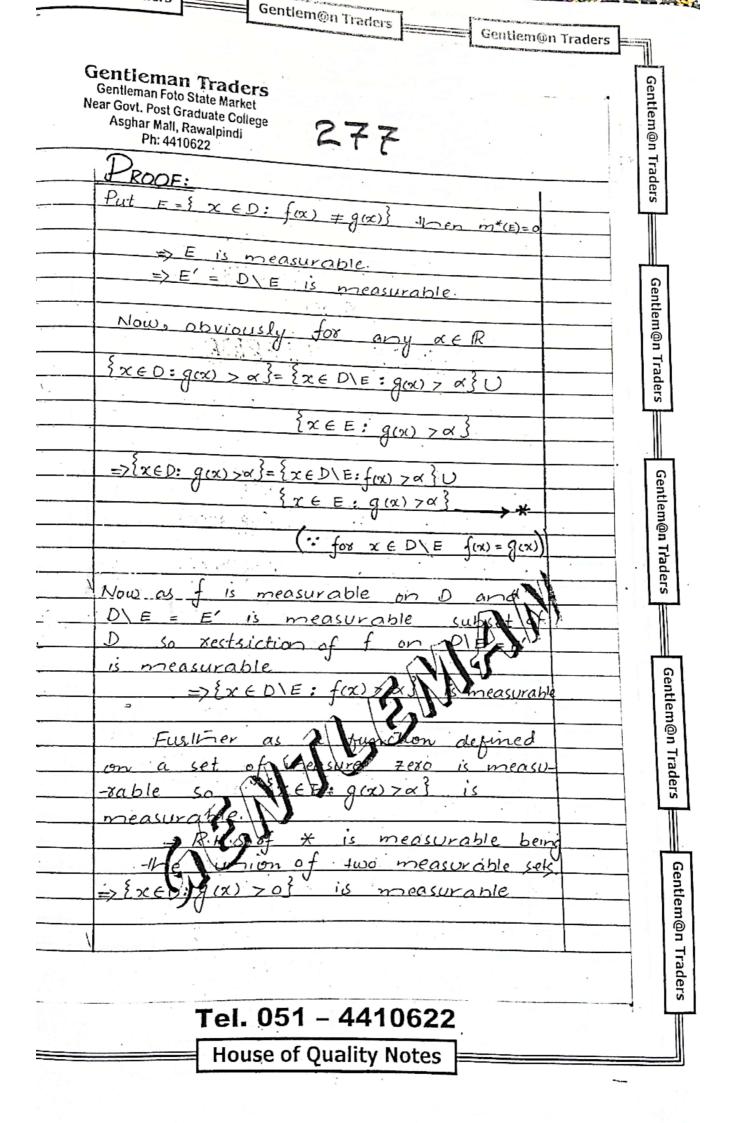


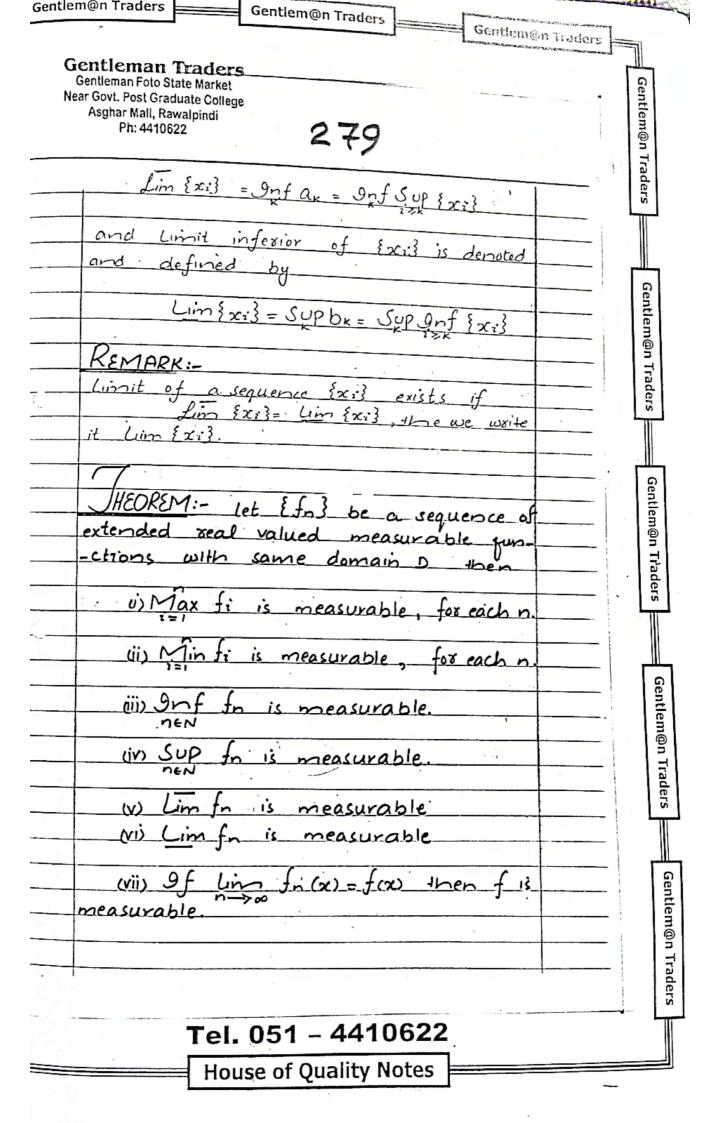


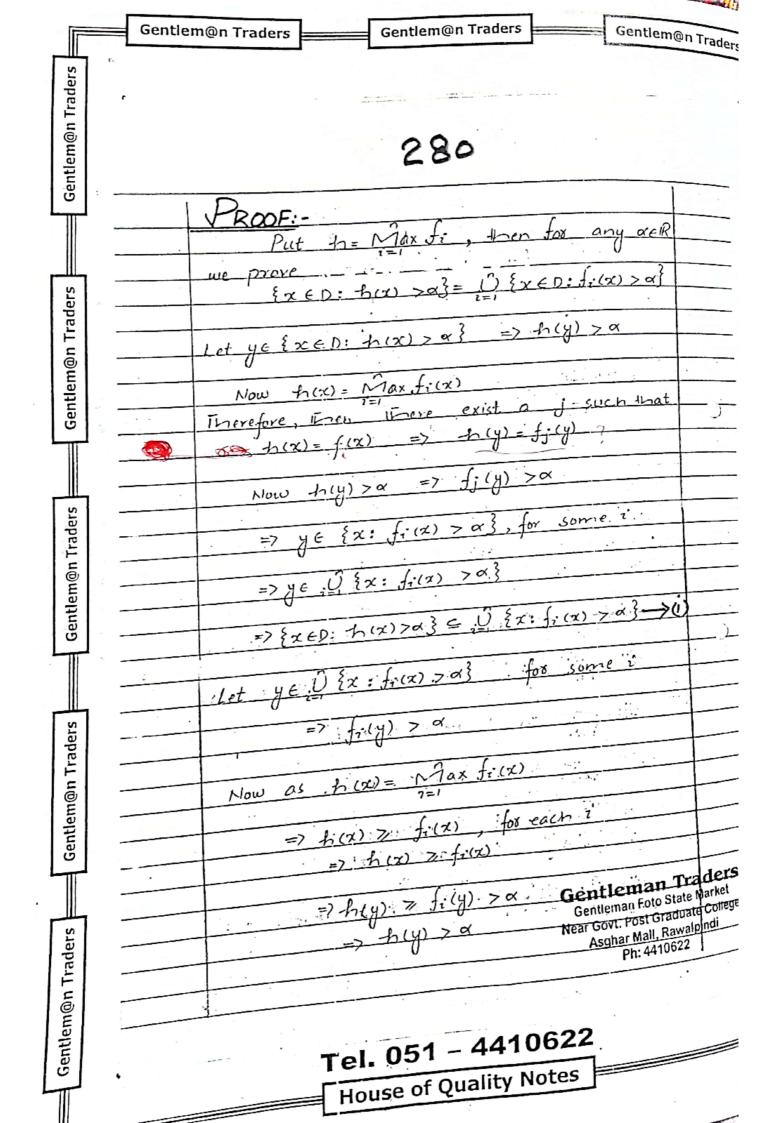
| Gentlem@n Traders | Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpindi Ph: 4410622 | |
|-------------------|--|-----|
| | | |
| | HEOREM:- | |
| | Any extended seal valued | |
| lers | function define on a set of | |
| Traders | measure zero is measurable. | |
| | P | |
| Gentlem@n | TROOF:- | |
| Sent | let f be defined on D, then by | |
| | given condition $m*(n)=0$ | |
| | => D is measurable. | |
| | Now, For any real number a | |
| ders | The second second | |
| Tra | $\{x \in D: f(x) > \alpha\} \subseteq D$ | |
| n@ | | |
| Gentlem@n Traders | >m*({x∈D: f(x) 7 α}) ≤ m*(D) | . 1 |
| l ger | : m* is mantane | |
| | => m*({x < D: f(x) > x }) < 0 | |
| | */5 | |
| N. | $= m*(\{x\in D: f(x) > \alpha\}) = 0$ | |
| Gentlem@n Traders | 5 7 6 D 1 (1) 12 | |
| J F | => {x \in D: f(x) > \alpha } is measurable | 2 |
| n@ | f is measurable. | - |
| ıt leı | 11#10 | |
| Ger | EFINITIONS:- | |
| | (i) A property is said to hold almost | |
| | everywhere (written as a.e.) if the set | |
| Sis | appoints where it does not hold has | |
| rade | measure zero. | |
| = | | |
| E | | |
| Gentlem@n Traders | | |
| Ge | | |
| | Tel. 051 - 4410622 | |
| | House of Quality Notes | |
| - | TIOUSE OF QUAITLY INOTES | |

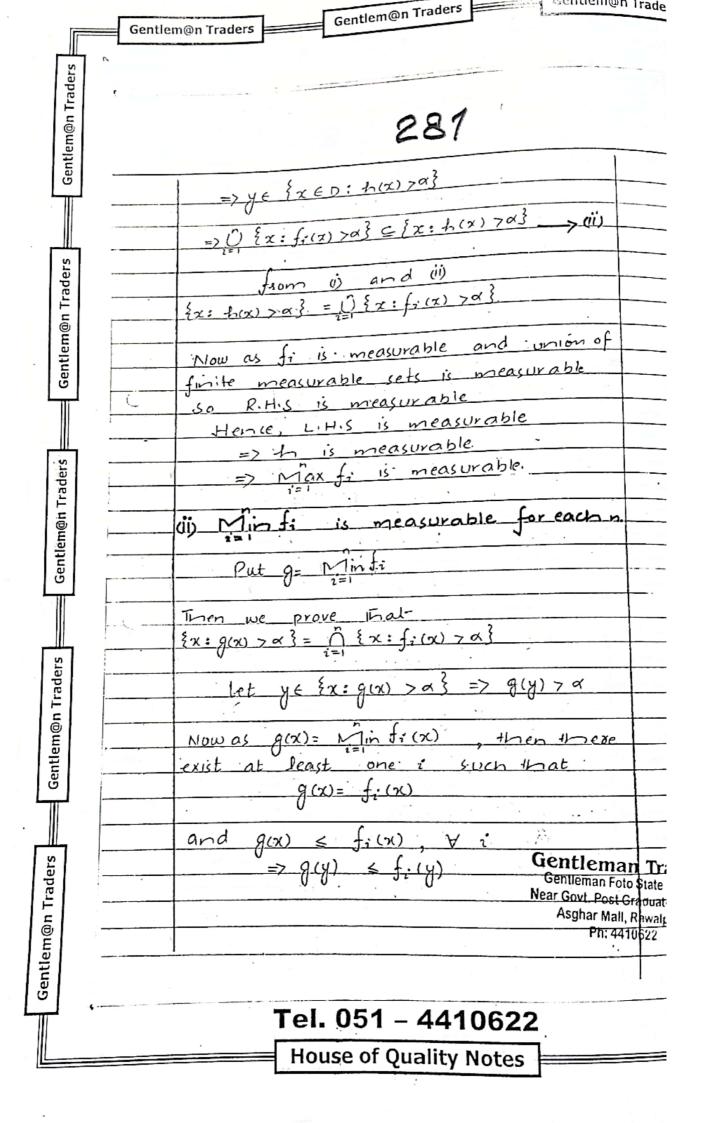


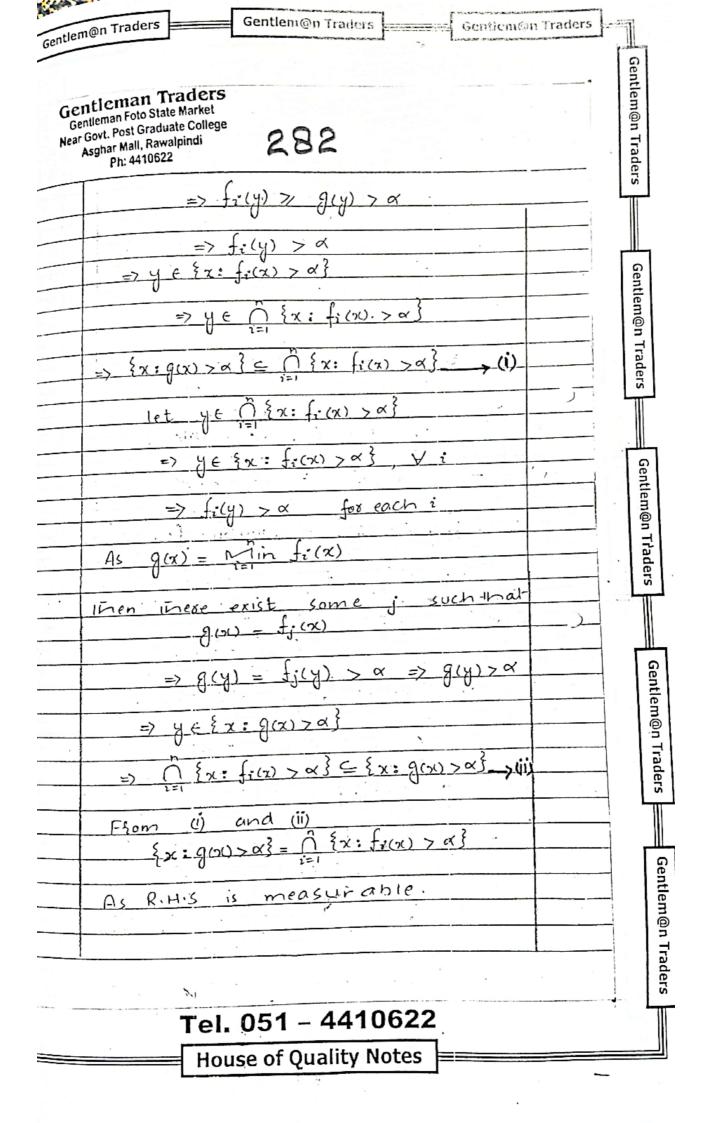










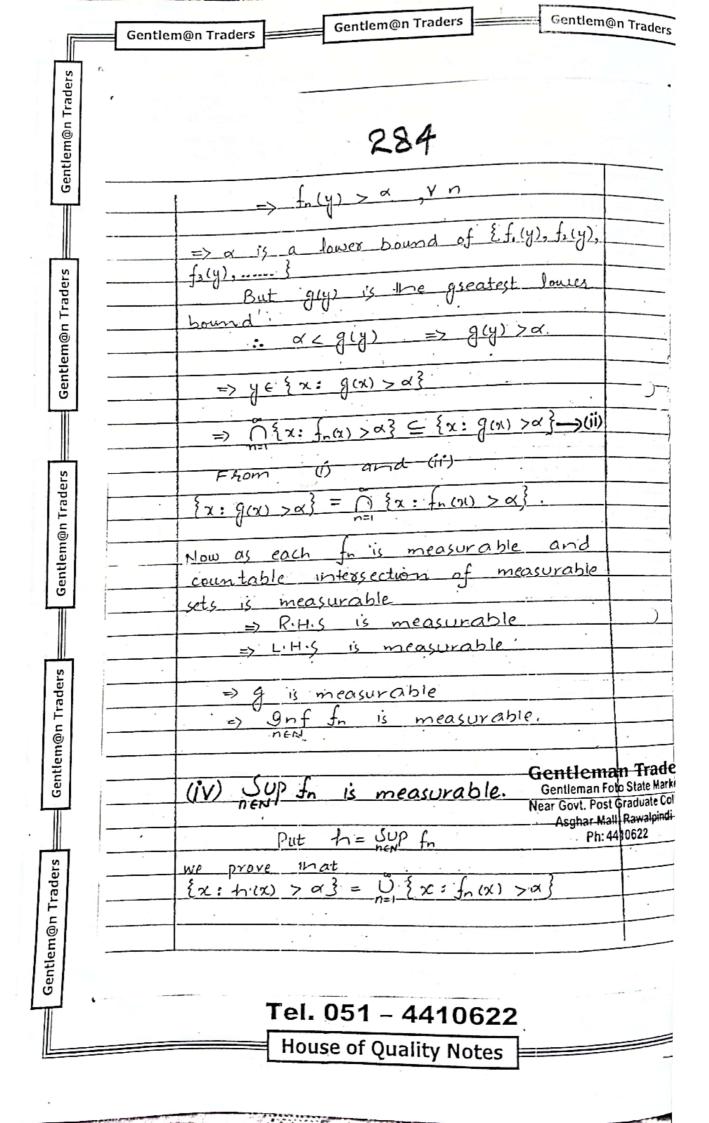


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| | Therefore 1.H.S is also measurable | |
|------------|--|---|
| | => 9 is measurable | |
| 14 1 | | |
| | =>. Min fi is measurable. | |
| | | |
| <u>(11</u> | i) Inf In is measurable. | |
| | D 1 2 2 C C | |
| | Put g= 9nf fn | |
| | low we prove -11-at | |
| 2 | $x: g(x) > \alpha $ = 0 $\{x: f_n(x) > \alpha \}$ | |
| | n=1 | |
| 4. | let y & {x: g(x) > a} => g(y) > a | |
| | | |
| | low as g = 9mf fn | - |
| | 2(4) | |
| 4 | => g(y) ≤ fn(y), Y n | |
| - | => fn(y) > g(y) > ~ | |
| | $\Rightarrow \int_{\Omega} (y) > \alpha$ | |
| | O . | |
| - | => y \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ | |
| | ~ () | |
| | => y ∈ ({x: fn(x) > «} | - |
| | > {x: g(x) > \alpha} \(\tilde{\gamma} \) \{x: \(\frac{\gamma}{2} \) \(\frac{\gamma}{2} \) \(\frac{\gamma}{2} \) | |
| | / (x. ga) > as = [(x. fa (x) / x) - y 0] | |
| | let y \(\hat{\gamma} \left\{ \chi \left\{ \chi} \left\{ \ | |
| | | |
| | => y \{x: \in(x) > \alpha}, \tag{n} | |
| | V | , |
| | | |

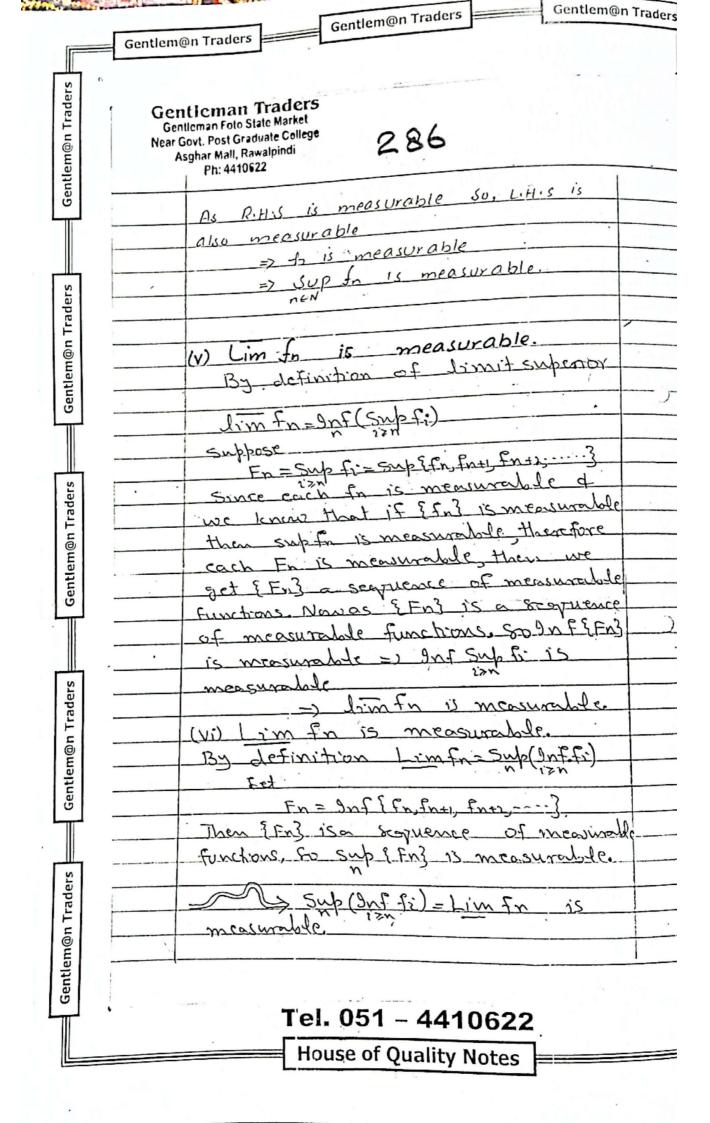
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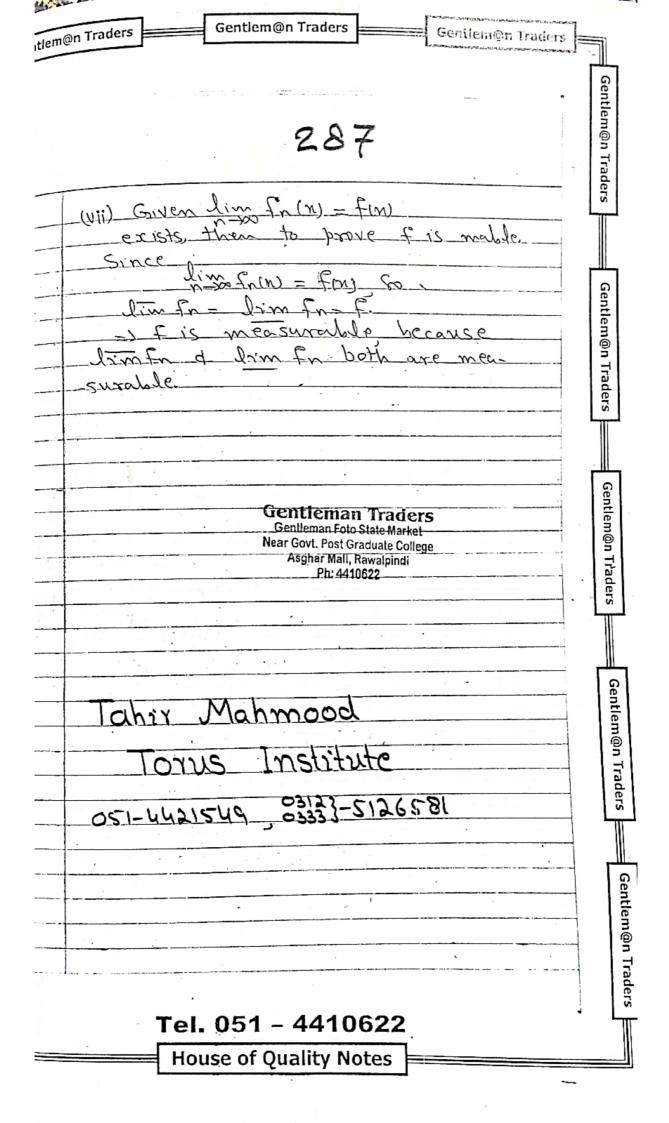


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| Now as $h(x) = \sup_{n \in \mathbb{N}} f_n(x)$ $\Rightarrow h(x) = \sup_{n \in \mathbb{N}} f_n(x)$ $\Rightarrow h(x) \Rightarrow f_n(x) \Rightarrow f_n(x) \Rightarrow f_n(x) \Rightarrow f_n(y) \Rightarrow f_n(x) \Rightarrow f_n(y) \Rightarrow f_n($ | |
|--|---------|
| $\Rightarrow h(x) \geqslant f_n(x) , \forall n \in \mathbb{N}$ $oR $ | |
| Now as $h(y) \gg f_n(y)$, $\forall n \in \mathbb{N}$ Now as $h(y) \gg f_n(y)$ and $h(y) > \alpha$ then there exist $m \in \mathbb{N}$, such that $f_m(y) > \alpha$ then $y \in \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : f_n(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ $\Rightarrow \{x : h(x) > \alpha\} \subseteq \mathcal{O} \{x : h(x) > \alpha\}$ | - |
| Now as $h(y) \gg f_n(y)$, $\forall n \in \mathbb{N}$ Now as $h(y) \gg f_n(y)$ and $h(y) \gg a$ then there exist $m \in \mathbb{N}$, such that $f_m(y) > \alpha$ then $y \in \mathcal{O}\{x: f_n(\alpha) > \alpha\}$ $\Rightarrow \{x: h(\alpha) > \alpha\} \subseteq \mathcal{O}\{x: f_n(\alpha) > \alpha\} - 7U$ let $y \in \mathcal{O}\{x: f_n(\alpha) > \alpha\}$ $\Rightarrow f_n(y) > \alpha$ Gentleman Foto State Mark Now as $h = \sup_{n \in \mathbb{N}} f_n(n) = \lim_{n \in \mathbb{N}}$ | |
| then these exist $m \in N$, such that $ f_{m}(y) > \alpha $ then $y \in \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: h(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: h(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: h(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: h(x) > \alpha\} $ $ = \sum \{x: h(x) > \alpha\} \subseteq \mathcal{O}\{x: h(x) > \alpha\} $ | - |
| $f_{m}(y) > \alpha$ then $y \in \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > \{x: h(\alpha) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > \{x: h(\alpha) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > y \in \{x: f_{n}(x) > \alpha\}$ $= > f_{n}(y) > \alpha \subseteq A$ Gentleman Trade Gentleman Foto State Mark Now as $h = \sup_{n \in \mathbb{N}} f_{n}$ $= > h(y) > f_{n}(y) > \alpha$ $\Rightarrow h(y) > f_{n}(y) > \alpha$ $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x: h(\alpha) > \alpha\}$ | |
| $f_{m}(y) > \alpha$ then $y \in \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > \{x: h(\alpha) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > \{x: h(\alpha) > \alpha\} \subseteq \mathcal{O}\{x: f_{n}(x) > \alpha\}$ $= > y \in \{x: f_{n}(x) > \alpha\}$ $= > f_{n}(y) > \alpha \subseteq A$ Gentleman Trade Gentleman Foto State Mark Now as $h = \sup_{n \in \mathbb{N}} f_{n}$ $= > h(y) > f_{n}(y) > \alpha$ $\Rightarrow h(y) > f_{n}(y) > \alpha$ $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x: h(\alpha) > \alpha\}$ | |
| $= \sum \{x : h(x) > \alpha\} \subseteq \bigcup \{x : f_n(x) > \alpha\} - \gamma U$ $= \sum \{x : h(x) > \alpha\} \subseteq \bigcup \{x : f_n(x) > \alpha\}$ $= \sum \{x : h(x) > \alpha\} \subseteq \bigcup \{x : f_n(x) > \alpha\} \subseteq \bigcup$ | |
| let $y \in \mathcal{D}\{x: f_{n}(x) > \alpha\}$ $\Rightarrow y \in \{x: f_{n}(x) > \alpha\}$, for some n $\Rightarrow f_{n}(y) > \alpha$ Gentleman Trade Gentleman Foto State Mark Now as $h = \sup_{n \in \mathbb{N}} f_{n}$ Near Govt. Post Graduate Co Asghar Mall, Rayalpindi $\Rightarrow h(y) > f_{n}(y) > \alpha$ Ph: 4410622 $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x: h(x) > \alpha\}$ | |
| $= y \in \{x: f_n(x) > \alpha\}, \text{ for some } n$ $= y \int_n (y) > \alpha. \qquad \text{Gentleman Trade}$ $= y \int_n (y) > \alpha. \qquad \text{Gentleman Foto State Mark Near Govt. Post Graduate Co}$ $= y \int_n (y) > \alpha. \qquad \text{Asghar Mall, Rawalpindi}$ $= y \int_n (y) > \alpha. \qquad \text{Ph: 4410622}$ $= y \int_n (y) > \alpha. \qquad \text{Ph: 4410622}$ | |
| $= 7 \int_{n} (y) > \alpha$ Gentleman Trade Gentleman Foto State Mark Now as $h = \sup_{n \in \mathbb{N}} \int_{n} \frac{\text{Gentleman Foto State Mark}}{\text{Near Govt. Post Graduate Co}}$ Asghar Mall, Ravalpindi $\Rightarrow h(y) > f_{n}(y) > \alpha$ $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x : h(x) > \alpha\}$ | |
| Now as $h = \sup_{n \in \mathbb{N}} f_n$ Near Govt. Post Graduate Co $n \in \mathbb{N}$ Asghar Mall, Rayalpindi $\Rightarrow h(y) \Rightarrow f_n(y) \Rightarrow \alpha$ Ph: 4410622 $\Rightarrow h(y) \Rightarrow \alpha \Rightarrow y \in \{x : h(x) > \alpha\}$ | |
| Now as $h = \sup_{n \in \mathbb{N}} f_n$ Near Govt. Post Graduate Co $n \in \mathbb{N}$ Asghar Mall, Rayalpindi $\Rightarrow h(y) > f_n(y) > \alpha$ Ph: 4410622 $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x : h(x) > \alpha\}$ | ders |
| $\Rightarrow h(y) \geqslant f_n(y) > \alpha$ $\Rightarrow h(y) > \alpha \Rightarrow y \in \{x : h(x) > \alpha\}$ | College |
| | |
| | |
| | |
| | |
| $\begin{cases} from & \text{(i)} \\ x: h(x) > \alpha \end{cases} = \bigcup_{n=1}^{\infty} \{x: f_n(x) > \alpha \}$ | |
| | |

Tel. 051 - 4410622





SORRY

Gentleman Traders
Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpindi Ph: 4410622

Gentlem@n Traders

Gentlem@n Traders

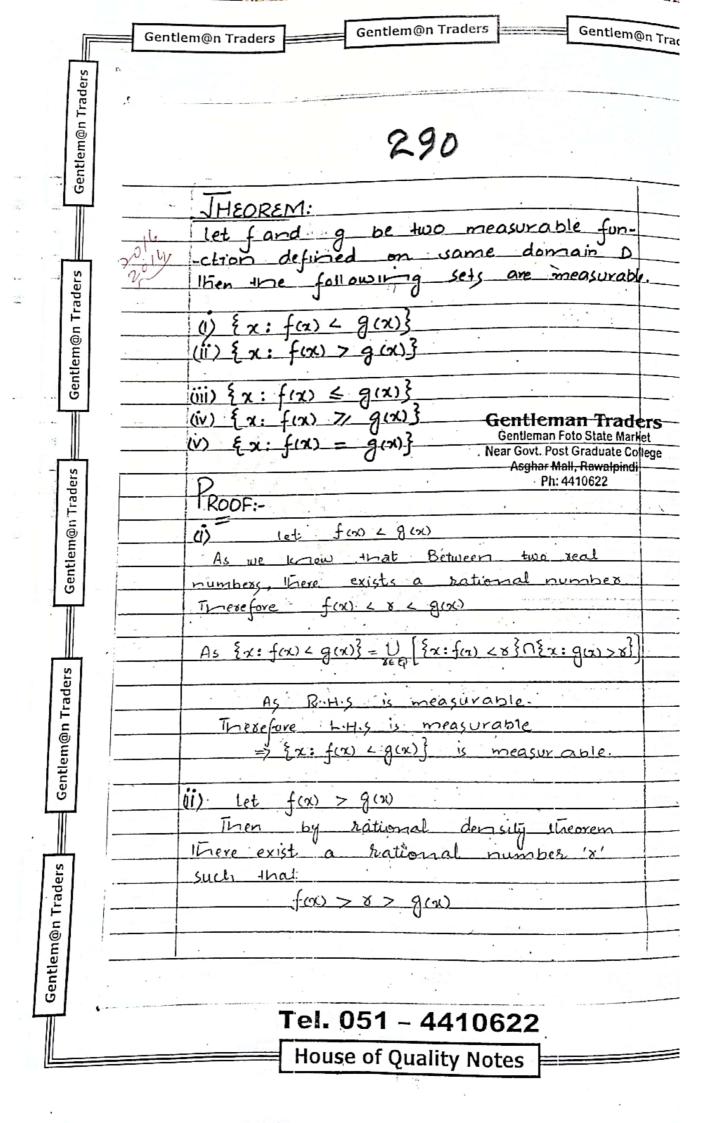
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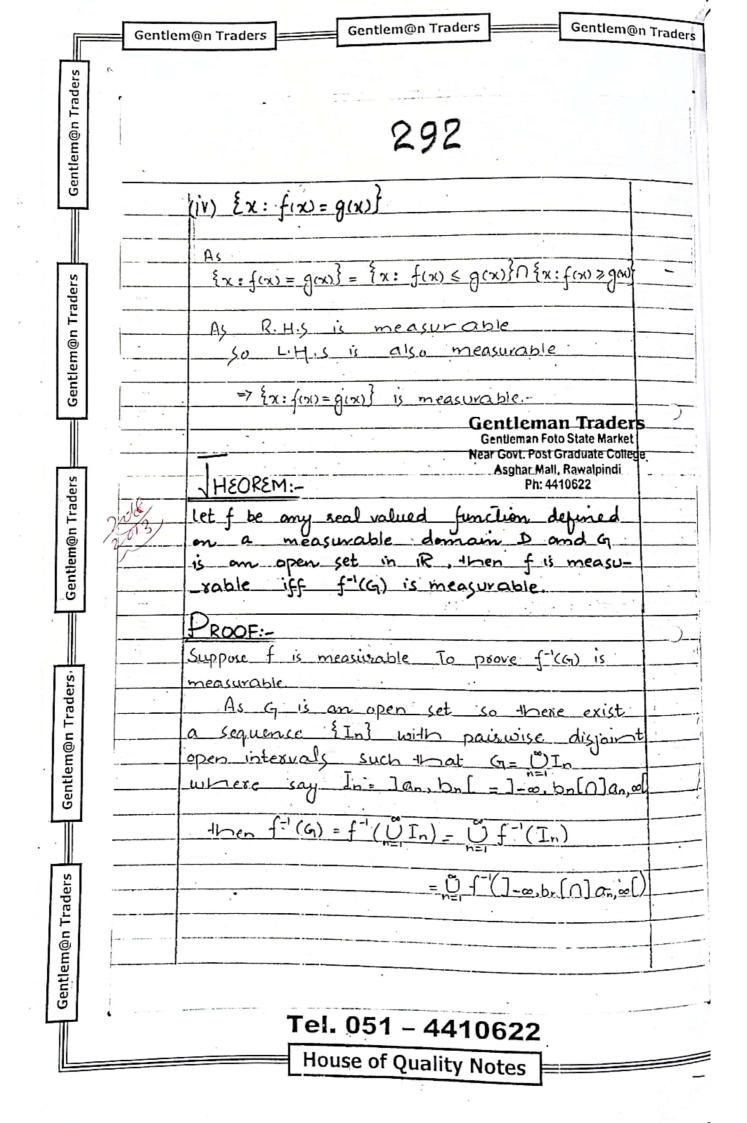
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HEOREM: measurable function and G open set then Ex: f(x) Eq 3 is POOF: Now measurable Gentleman Traders Gentleman Foto State Market Near Govt. Post Graduate College Asghar Mall, Rawalpindl Ph: 4410622

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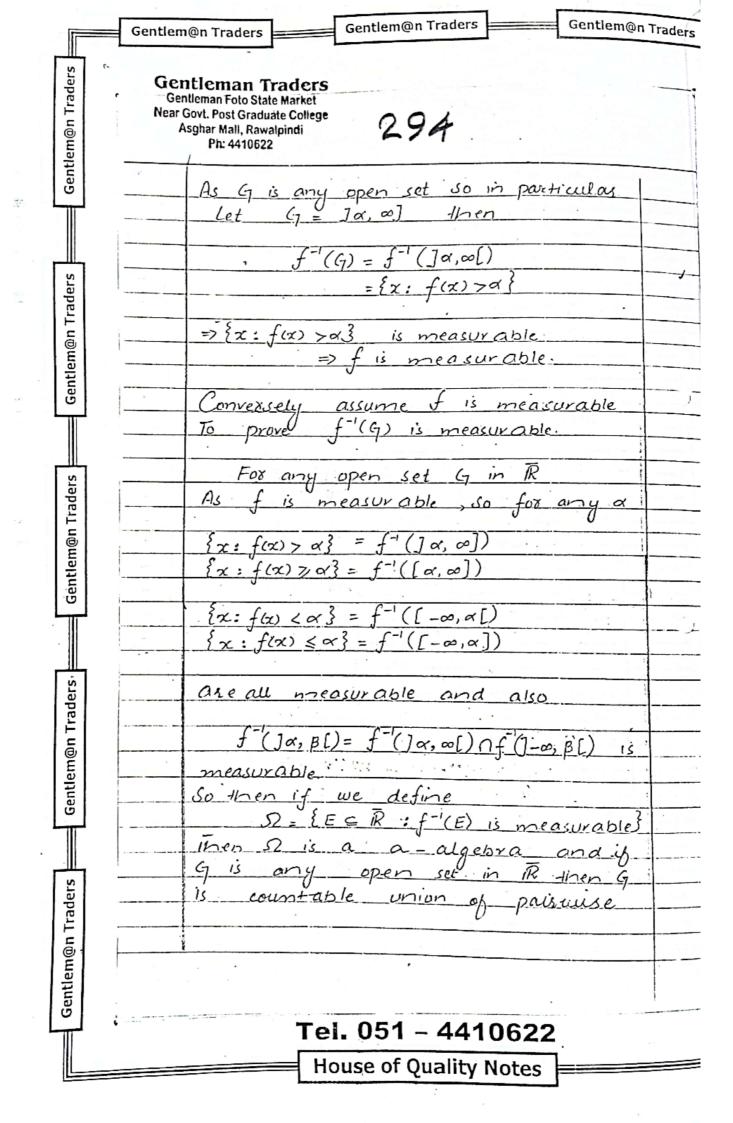


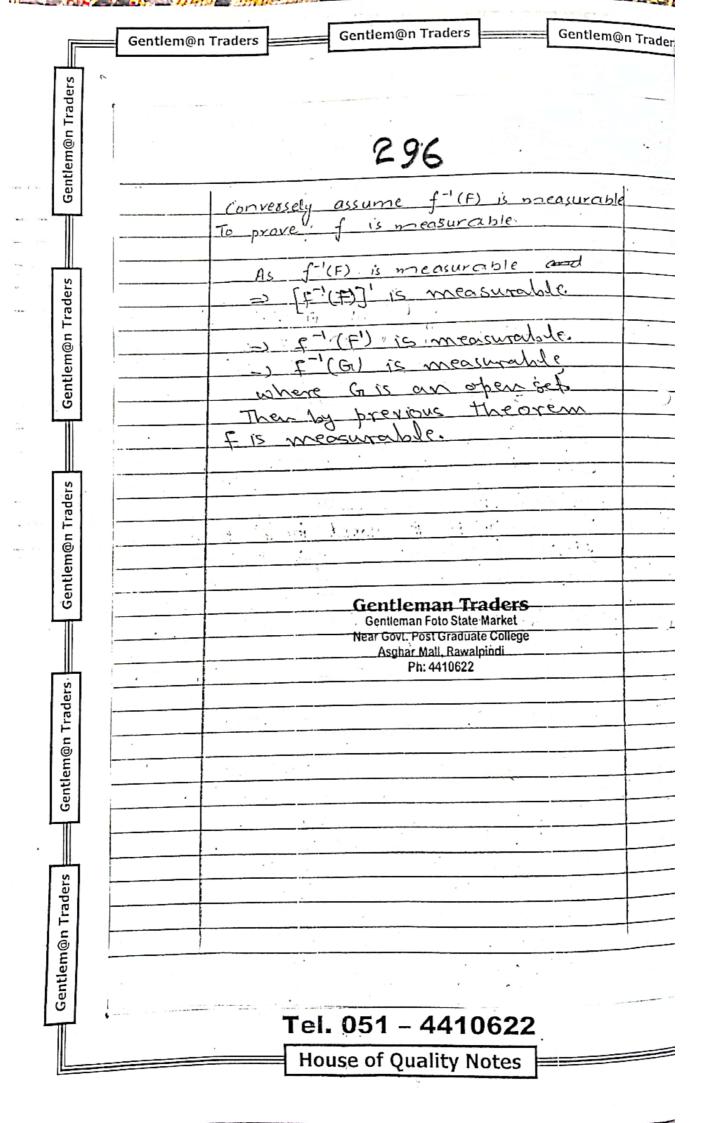
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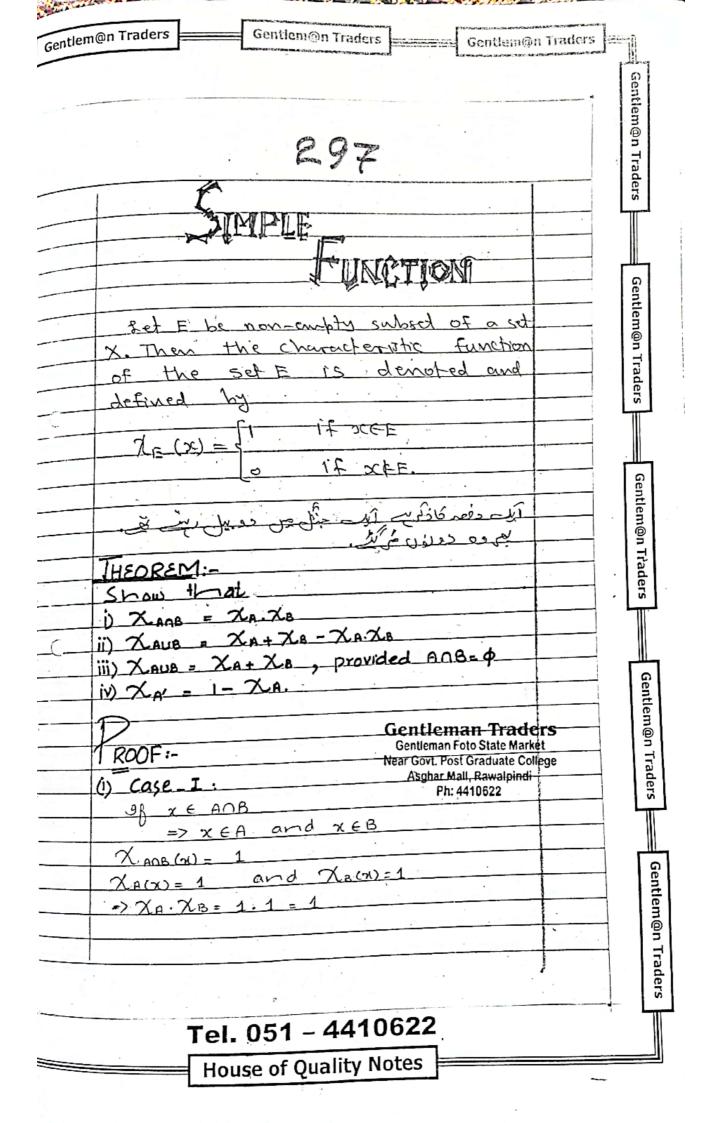
| - 1 | => f-1(6) 100(1-1) |
|-------------------|--|
| - | $\Rightarrow f^{-1}(G) = \bigcup_{n=1}^{\infty} \left\{ f^{-1}(J-\infty,b_n[) \cap f^{-1}(Ja_n,\infty[) \right\}$ |
| | $m \in \mathcal{L}_{\infty}(\Omega_{n}, \infty)$ |
| | $= 0 \left[\left\{ x : f(x) < b_n \right\} \cap \left\{ x : f(x) > a_n \right\} - 0 \right]$ |
| | $\frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} \frac{1}{\sqrt$ |
| | |
| | Since Pull |
| | Since R.H.s is measurable so is LiHis |
| | 7-13 (-1-1) |
| | => f-1 (G) is measurable. |
| | |
| | Conversely assume (-1/1) |
| | Conversely assume f-1(G) is measura- -ble. To prove f(G) is measurable. |
| | 16) is measurable. |
| | As G is and |
| | As G is any open set so in pax- -ticular if G= Ja, of then |
| | God of God on then |
| | f-1 (G) = f-1(Ja, or [) |
| | |
| - | $= \{x: f(x) > \alpha \}$ |
| | |
| $C \rightarrow L$ | As given $f^{-1}(G)$ is measurable. $\Rightarrow \frac{9}{3}x: f(x) > \alpha \frac{3}{3}$ is measurable |
| | \Rightarrow $\{x: f(x) > \alpha\}$ is measurable |
| | => f is measure his |
| | => f is measurable. |
| - | |
| | KEMARK: |
| - | VVENIAKK. |
| | Above theosem is valid if f is |
| | Above theorem is valid if f is an extended real valued function. |
| | |
| | PROOF: Suprace fox any open set G in R |
| | PROOF: Suppose fox any open set G in R |
| <i>f</i> | (G) is measurable to prove of |
| | -able. |
| | Gentleman Traders |
| | Gentleman Foto State Montan |
| | Near Govt. Post Graduate College |

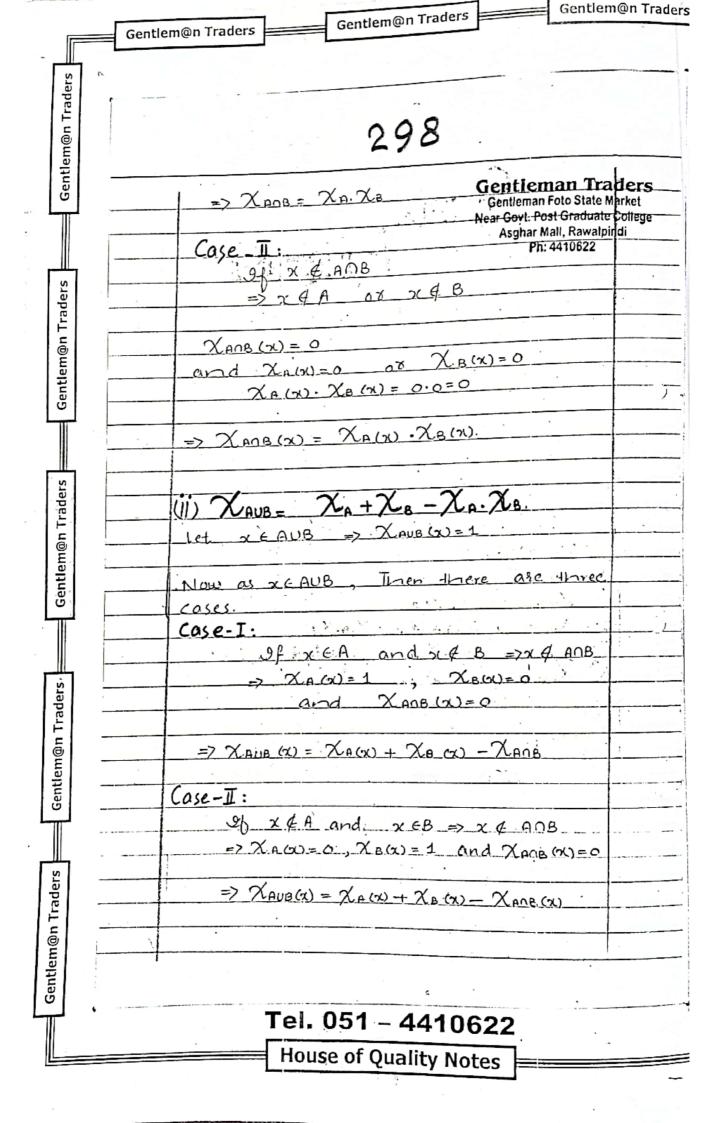
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GINTERMAN TRAIDINGS IF TO Stationers



Laser Fotostat



Colour Fotostat



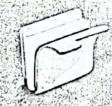
Map Coloui Fotocopy



Ang&Tope Binding



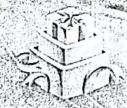
MapBlack& While Folcopy



Transparency



Sports Items



Gifi Items
Mobile Cards
& Accessories



International Fax



Lamination & Covering

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